

Radiation emission from braided electrons in interacting wakefields

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The radiation emission from electrons wiggling in a laser wakefield acceleration (LWFA) process, being initially considered as a parasitic effect for the electron energy gain, can eventually serve as a novel X-ray source, which could be used for diagnostic purposes. Although several schemes for enhancing the X-ray emission in LWFA has been recently proposed and analyzed, finding an efficient way to use and control this radiation emission remains an important problem. Based on analytical estimates and 3D particle-in-cell simulations, we here propose and examine a new method utilizing two colliding LWFA patterns with an angle in between their propagation directions. Varying the angle of collision, the distance of acceleration before the collision and other parameters provide an unprecedented control over the emission parameters. Moreover, we reveal here that for a collision angle of 5° , the two wakefields merge into a single LWFA cavity, inducing strong and stable collective oscillations between the two trapped electron bunches. This results in an X-ray emission which is strongly peaked, both in the spatial and frequency domains. The basic concept of the proposed scheme may pave a way for using LWFA radiation sources in many important applications, such as phase-contrast radiography. © 2017 Author(s). All article content, except where otherwise noted, is licensed under a Creative Commons Attribution (CC BY) license (http:// creativecommons.org/licenses/by/4.0/). [http://dx.doi.org/10.1063/1.4997440]

INTRODUCTION

The radiation emission from electrons, caused by their oscillations during the process of laser wakefield acceleration (LWFA), is a promising mechanism for creating novel X-ray sources with desirable properties such as compact size, tunable spectral characteristics, and short duration.^{1–5} These sources may thus find applications in many areas, from diagnostics in medicine and biology to pump-probe measurements at femtosecond time scales. Several concepts were proposed for controlling and enhancing the X-ray emission, including modifying the wave-front,^{6,7} as well as using clustering gas jets,⁸ ionization injection,⁹ and a curving path of acceleration.¹⁰ Here, we present a new concept based on inducing strong oscillations of the accelerated electron beams by colliding two LWFA patterns. We use 3D particle-in-cell (PIC) simulations and analytical estimates to analyze the concept. Our analysis shows that if the angle between the LWFA pattern propagation directions is small enough, a new type of nonlinear dynamics arises: both patterns merge into one moving plasma cavity and the two pre-accelerated bunches of electrons start to oscillate around its center, producing intense X-ray emissions with a narrow spectral and spatial structure.

Over the past years, LWFA has become a reliable method for creating compact and tunable sources of electrons suitable for producing radiation. Depending on the needed range of photon energies, one can use different basic mechanisms, including Thomson scattering, Betatron and Synchrotron emission, and Compton scattering.^{11,12} Apart from using external fields of undulators and wigglers,¹³ X-ray emission can be also caused by laser fields or induced plasma fields, which can be much stronger. For example, collision with a counter propagating laser pulse^{11,14–18} and electron oscillations in the laserproduced plasma cavity have been previously studied.^{3,10,19,20} Here, we consider inducing electron oscillation by colliding wakefields and use the angle of collision to get a transition between these cases, focusing on the case of small angle collisions. Radiation from small angle colliding wakefields is also interesting from diagnostic reasons, as well as from proving different properties of radiation. We shall see that this includes a broad frequency range and a small angle of emission.

Wakefield systems can experience filamentation instabilities. It is known from experiments that these filaments can in turn interact,²¹ generating what can be considered a precursor to the systematic studies of the wakefield interaction found in the literature. Such an interaction between two laser wakefields has been considered in a number of works in the literature, mostly in the cases of co-propagating wakefields or head-on collisions. Ren et al.²²⁻²⁴ investigate the nonlinear force between two co-propagating wakefields and the dynamics due to this interaction. They find that the oscillations due to the nonlinear interaction are typically of frequency ω_p , the electron plasma frequency of the system, and that the two pulses can coalesce due to radiative cooling. Dong *et al.*²⁵ find a strong radiative emission during beam coalescence from initially co-propagating pulses, perhaps not surprisingly indicating that the such systems can be a source of high frequency radiation. Wu et al.²⁶ discussed the effect of crossed polarisation in a setup similar to the ones above. Sodha and Sharma²⁷ formulated the interaction of copropagating wakefields in terms of the non-homogeneous dielectric function, also including a discussion on collisions. Wen et al.²⁸ investigated how charge loading and electron energy are affected by co-propagating wakefields, as a



possible means for increasing the wakefield current. Yang et al.²⁹ deviated from the limitation of co-propagation and presented PIC simulations for two different angles (5.2° and 8.6°) of collision between the wakefields for the purpose of evaluating the effects of the angle on charge loading and energy spread. The head-on collision between wakefields was considered by Deng et al.,³⁰ using PIC simulations to investigate the wakefield front dynamics and the ensuing electron oscillations. The PIC simulations indicate that the collision results in chaotic electron motion and a transverse escape of electrons from the bubble region. These references show that there are features of interacting wakefields that can make both a quantitative as and a qualitative difference for the system, as compared to single pulse wakefields. However, a systematic view is lacking and therefore also a possibility to use different features of colliding wakefields for possible applications. One such feature is creating a tunable and compact soft X-ray source from such collisions.

In this paper, we do a full parameter scan of collisional angles between wakefields (see Fig. 1), in order to control and optimise the electron dynamics for radiation generation. We investigate the corresponding radiative emissions, using both numerical analysis and analytical estimates. There are two mechanisms that can cause the emitted synchrotron radiation. For larger angles, it is mainly the interaction between the electron bunch of one wakefield with the laser pulse of the other. For small angle collisions, the regions of electron cavitation behind the laser pulses merge and form a joint large region. The accelerated electrons start to oscillate around the center of this region, which triggers their synchrotron emission.

GOVERNING THEORY

We consider the nonlinear regime of LWFA where the laser pulse is of sufficient power to create a region void of electrons. In this "blowout,"³¹ or "bubble,"³² regime, the laser pulse in the front is followed by a bubble-shaped region of non-compensated background ions, with a bunch of electrons accelerated by the charge separation in the rear part of the bubble. Colliding two of these fields at angle θ gives rise to radiation (see Fig. 1). The lateral acceleration giving rise to the radiation can be either due to the laser field or the plasma field. In order for the laser-acceleration regime to be



FIG. 1. Schematic representation of the collision between two wakefields by an angle θ . For small angle collisions ($\theta < 10^{\circ}$), the electron bunches will experience nonlinear oscillations in the merged bubble structure; here, indicated by the two directions in green.

prominent, the electron bunch should pass through the center of the laser pulse, preferably in a head on collision as the effect of the fields is suppressed for the case of co-propagation. This naturally arises for large angle collisions. For the plasmaacceleration to be efficient, the interaction time must be long enough, which is the case for small angle collisions.

Below, we estimate the typical spectra of the radiation in different regimes, by estimating the *effective magnetic field* H_{eff} experienced by the electron bunch. From the experimental setup, we have the maximum field strength of the pulse given by the dimensionless parameter a_0 (relativistic amplitude), and the typical energy of the electrons is given by their Lorentz factor γ . The typical frequency of the emitted radiation can then be estimated by³³

$$\omega_c = \frac{3eH_{\rm eff}}{2mc}\gamma^2.$$
 (1)

TRANSVERSE FIELD STRUCTURE

For the case of two counter-propagating laser pulses, the electron bunch passes through the center of the laser pulse, maximizing the energy and frequency of the radiation. We consider two factors that affect the frequency of the radiation for a collision with an angle θ : (a) how the electric and magnetic fields contribute to $H_{\rm eff}$ and (b) how the distance between the bunch and the pulse center reduces $H_{\rm eff}$.

For (a), we consider the collision between the upper pulse and the lower bunch as seen in Fig. 2. The fields are given by $\mathbf{E} = A\hat{y}$ and $\mathbf{B} = A[\sin(\theta/2)\hat{x} + \cos(\theta/2)\hat{z}]$, where *A* is the amplitude of the fields, and the velocity of the electrons in the opposite bunch is $\mathbf{v} \approx c[\cos(\theta/2)\hat{x} + \sin(\theta/2)\hat{z}]$. Considering the effective magnetic field due to the two terms in the Lorentz force, we get $\mathbf{F} = qA\hat{y}(1 - \cos\theta)$.

For (b), we estimate the electron bunch as located $\sim \lambda_p/2$ behind the laser pulse, where λ_p is the plasma wavelength. The minimum distance between the bunch and the center of the colliding pulse is then given by $L_{\min} = \cos(\theta/2)\lambda_p/2$, and for a Gaussian shaped pulse of duration $\sim \lambda_p/c$ (FWHM for intensity), the maximal *effective* magnetic field experienced by an electron in the bunch is

$$H_{\text{laser}} = A(1 - \cos\theta) \exp\left[-\cos^2(\theta/2)\right], \qquad (2)$$

where A is the pulse's peak amplitude.



FIG. 2. Illustration of the geometry for the collision between the bunch and the laser pulse.

LONGITUDINAL FIELD STRUCTURE

For small angle collisions, the radiation is emitted due to the interaction between the electron bunches and the plasma fields. The interaction starts when the two bubbles overlap. The plasma is mainly pushed around both laser pulses, creating a larger bubble-like region with the electron bunches offset from the center, as seen in Fig. 3. The electron streams through the laser region which can be seen are pushed outwards with time and do not strongly affect our considerations. The bunches are initially offset a distance Rfrom the center, where $R \sim \lambda_p/2$ is the radius of a bubble. It turns out that the effect of one bunch on the other is smaller than the effect of the ions on either bunch, as the bunches are roughly co-propagating and the contribution from the electric and magnetic fields are counteracting.³⁴ The effective force on a bunch at radius r will be due to the ions in the sphere of radius r. For a test particle in the bunch, this is given by $F = 4\pi e^2 n_0 r/3$. The resulting oscillation frequency is $\omega_{\rm osc} = (4\pi e^2 n_0/3\gamma m)^{1/2} = \omega_p/\sqrt{3\gamma}$. We can thus expect an oscillatory motion of the electron bunches, provided that the timescale of the collision is longer than the period time of the oscillation. We can estimate the collision time from the angle of collision and bubble size as

$$T_c = \frac{2R}{c\sin(\theta/2)}.$$
(3)



FIG. 3. Collision of two laser wakefields at 70° (upper panel) and at 5° (lower panel), shown at three different times. The electron density (in the x-z plane, the plane of collision) is plotted in white-green-black in units of the background density, and the laser is plotted in blue-red via the y-component of the electric field, with the polarization of the pulse perpendicular to the plane of collision.

Furthermore, the maximum effective magnetic field due to the plasma field is given by the force at a distance R

$$H_{\text{plasma}} = \frac{4}{3}\pi e n_0 R. \tag{4}$$

METHODS

Simulation setup

We perform 3D PIC simulations of the processes using the code ELMIS3D.³⁵ A linearly polarized laser pulse with an energy of 1 J, a wavelength of $0.81 \,\mu\text{m}$, a diameter of $8 \,\mu\text{m}$, and a duration of 20 fs (both FWHMs in intensity) is passed on a plasma with a density of $N = 9.5 \times 10^{18} \text{ cm}^{-3}$. The normalized laser amplitude is given by $a_0 = 5.6$. Electrons are injected through a density gradient with the plasma having a longitudinal density profile. The density increases linearly from 0 to 3N in 10 μ m and then decreases linearly to N in another $10\,\mu m$, where it is maintained for the reminder of the simulation. The simulation box is $60 \,\mu\text{m} \times 60 \,\mu\text{m} \times 60 \,\mu\text{m}$ on $512 \times 128 \times 512$ cells and is comoving with the pulse. We let the laser wakefield propagate $100\,\mu m$ through the plasma after which we clone the pulse and wakefield and rotate them to collide at different angles, 5° and 10° to 180° in steps of 10° . Both wakefields are rotated an angle $\theta/2$, where θ is the collision angle.

The two wakefields are synchronized in time and are initially a transverse distance of $30\,\mu m$ apart, measured from center to center, and the collisions will thus take place at different longitudinal positions, depending on the angle of collision. An example of this can be seen in Fig. 3 where the process is shown at three different times for the cases of 70° and 5° collision angles. The x-z plane (plane of collision) is shown, with the polarization of the pulses in the perpendicular y-direction. We use a method for determining the high frequency radiation from relativistic particles³⁶ where the electrons are considered to be in instantaneous circular motion due to an efficient magnetic field $H_{\rm eff}$, taking into account the contribution from both the electric- and magnetic fields. We then use a Monte Carlo method to sample from the spectra to emit photons in the direction of propagation of the emitting particle. The recoil of each particle due to emission is calculated as a continuous friction force using the Landau-Lifshitz^{33,37} expression

$$\mathbf{F}_{\text{rad}} = \frac{2}{3} r_0^2 \left\{ \mathbf{E} \times \mathbf{B} + \frac{1}{c} [\mathbf{B} \times (\mathbf{B} \times \mathbf{v}) + (\mathbf{v} \cdot \mathbf{E}) \mathbf{E}] - \frac{\gamma^2}{c} \left[\left(\mathbf{E} + \frac{1}{c} \mathbf{v} \times \mathbf{B} \right)^2 - \left(\frac{\mathbf{E} \cdot \mathbf{v}}{c} \right)^2 \right] \mathbf{v} \right\},$$
(5)

where $r_0 = e^2/m_e c^2$ is the classical electron radius in cgs units.

RESULTS AND DISCUSSION

For large angle collisions, the wakefields make a single pass, as shown in Fig. 3, mostly emitting radiation as the bunch interacts with the colliding pulse. However, for small



FIG. 4. Comparison of the typical collision time and the bunch oscillation period for the simulated wakefield collisions. For small angles, the collision time is long enough for oscillations to occur.

angle collisions, we observe the predicted oscillating electron bunches. In Fig. 4, a comparison of the timescales of bunch oscillation and collision time can be seen, in line with the observed oscillations. The oscillatory motion of the bunches can be seen in Fig. 5, showing a cross section of the simulation box for the full extent of the simulation for the 5° collision. The estimated collision time is ~ 0.5 ps; however, one can see that the bunch oscillations persist longer than so. As the initial wakefields pass, a new larger bubble is formed in which the electron bunches continue to oscillate. This longer interaction time allows for more energy to be emitted as radiation. It is a remarkable fact that the amplitude of the oscillations in Fig. 5 does not decay over time as the electrons radiate. This is a consequence of the relativistic electrons emitting predominantly in the forward direction, so the radiation reaction recoil does not change the direction, only the energy, of the particles.

The spectra of the emitted radiation as a function of the collision angle can be seen in Fig. 6. Here, one can see the two regimes of radiation, with peaks in frequency and total energy of the radiation provided by the collision angles of $\theta \sim 0^{\circ}$ and $\theta \sim 180^{\circ}$. The marks represent the maximum frequency of the radiation, and the lines are given by the estimates of the typical emitted frequencies according to Eqs. (1), (2), and (4). These agree well with the radiation for the large and small angle collisions. The emitted energy for different collision angles can be seen in Fig. 7. This is







FIG. 6. Frequency spectra of the emitted radiation for simulations of collisions for a range of angles. Peak frequencies and frequencies below which 99% of the energy was emitted are marked. The lines provide estimates of the typical frequency of the emitted radiation due to the laser-(blue) or plasma (green) fields for the simulations.

calculated from the start of the collision to a time when the pulses have passed each other and switched position, and thus, the shorter time, the greater the angle of collision. The radiation from the small angle collisions is emitted within a small angle, with some noise at larger angles due to the plasma particles pushed around the laser pulse, which has been excluded from Fig. 7. Angular plots of the emitted radiation can be seen in Fig. 8 for some selected collision angles, and Fig. 9 shows a power spectrum for the same selected angles.

The oscillating electrons and the formation of a joint bubble for small angle collisions provide the possibility of generating radiation from a plasma field with a very long interaction time. One could imagine a situation with balance between the gain of energy due to the wakefield and loss of energy due to radiation for the electrons, resulting in a stable conversion of laser energy into X-rays.

For the described setup, different collisional angles result in different propagation times before the collisions and thus different particle energies. In the following section, we attempt a more general comparison between the two regimes.



FIG. 7. The total emitted radiation as a function of the angle for the simulations, with analytical estimates for the two regimes. The marks show the results from 3D PIC simulations, with estimates of the emission due to acceleration via the laser fields (blue) and the plasma fields (green). The dashed line is a polynomial fit to highlight the mark pattern, and the vertical background color corresponds to respective power spectra in Fig. 7.



FIG. 8. The angular distribution of the emitted photons for the angles 5° , 10° , 40° , 90° , and 180° . We can see the strong collimation of the radiation for the case of a 5° collision.

↓ Plane of collision
 ↔ Polarization direction
 ⊗ CoM propagation direction

Comparison between radiation via laser- or plasma fields

The power of the emitted radiation for an ultrarelativistic electron in a perpendicular field H is³³

$$I = \frac{2e^4 H^2}{3m^2 c^3} \gamma^2.$$
 (6)

Using the estimate of the typical collision time given in Eq. (3), we can make an estimation of the total emitted energy as $E_{\rm rad} = IT_c$. As seen from the simulations, in the small angle regime, the bubbles merge and the oscillations continue longer than the typical collision time. In the simulations, this was increased by a factor of ~10.

For the case of the plasma field, the field strength is given by Eq. (4). We estimate the size of the bubble from the density and intensity according to³⁸ $k_p w_0 \approx k_p R \approx 2\sqrt{a_0}$, where k_p is the plasma wave number, w_0 is the laser spot



FIG. 9. Power spectrum of the emitted radiation for a range of selected collision angles.

size, and *R* is the radius of the bubble. From this, we can get H_{plasma} (4) only depending on the density, as the bubble radius can be expressed as

$$R = \frac{2\sqrt{a_0}c}{\omega_p}.$$
(7)

The normalised field amplitude a_0 is related to the field strength *A* through $a_0 = e|\mathbf{E}|/m_e\omega_0 c = eA/m_e\omega_0 c$, where ω_0 is the frequency of the laser. We can express the efficient magnetic field for the case of laser acceleration as $H_{\text{laser}} \sim a_0 m_e \omega_0 c/e$. Using this, we can estimate the total emitted energy for each regime, shown in Fig. 7, where we have compensated for the longer interaction time for the small angle collisions.

Furthermore, keeping the particle energy the same for both cases, we can compare the field strength for the two regimes, with their ratio given by

$$\frac{H_{\text{plasma}}}{H_{\text{laser}}} = \frac{2}{3a_0^{1/2}}\frac{\omega_p}{\omega_0}.$$
(8)

CONCLUSIONS

In this paper, we propose and examine a new concept for creating a tunable X-ray source based on the small-angle collision of two laser wakefields. The interacting wakefields provide the deflecting forces, acting as a nonlinear undulator, for the bunches of pre-accelerated electrons. As compared to the concepts of head-on collision and stimulated betatron emission in LWFA, the concept provides a unique control over the emission properties. This control is achieved by varying the collision angle, the plasma density, the laser intensity, and the propagation distance before the collision. In such a way, one can create an X-ray source with tunable photon energy, directivity, and beam duration, with a multitude of possible applications.

In this paper, we also identified the nontrivial phenomenon of merging two wakefields into a single one in the case of a sufficiently small angle of collision. This phenomenon provides an opportunity for triggering long-lasting oscillations of the accelerated electron bunches, with an oscillation amplitude as large as the merged bubble size. This scenario can be used for creating a highly efficient converter of the laser pulse energy into X-ray radiation.

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AUTHOR CONTRIBUTION

E.W. performed the numerical simulations. E.W., A.G., and M.M. contributed equally to the analysis, theoretical studies, and writing of the manuscript. A.G. conceived the original idea.

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