# Transiting exoplanets from the CoRoT space mission<sup>\*,\*\*</sup>

# XXVII. CoRoT-28b, a planet orbiting an evolved star, and CoRoT-29b, a planet showing an asymmetric transit

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#### ABSTRACT

*Context.* We present the discovery of two transiting extrasolar planets by the satellite CoRoT.

Aims. We aim at a characterization of the planetary bulk parameters, which allow us to further investigate the formation and evolution of the planetary systems and the main properties of the host stars.

Methods. We used the transit light curve to characterize the planetary parameters relative to the stellar parameters. The analysis of HARPS spectra established the planetary nature of the detections, providing their masses. Further photometric and spectroscopic ground-based observations provided stellar parameters (log g,  $T_{\text{eff}}$ ,  $v \sin i$ ) to characterize the host stars. Our model takes the geometry of the transit to constrain the stellar density into account, which when linked to stellar evolutionary models, determines the bulk parameters of the star. Because of the asymmetric shape of the light curve of one of the planets, we had to include the possibility in our model that the stellar surface was not strictly spherical.

Results. We present the planetary parameters of CoRoT-28b, a Jupiter-sized planet (mass  $0.484 \pm 0.087 M_{Jup}$ ; radius  $0.955 \pm 0.066 R_{Jup}$ ) orbiting an evolved star with an orbital period of  $5.20851 \pm 0.00038$  days, and CoRoT-29b, another Jupiter-sized planet (mass  $0.85 \pm 0.20$   $M_{Jup}$ ; radius  $0.90 \pm 0.0012$  $0.16 R_{Jup}$ ) orbiting an oblate star with an orbital period of 2.850 570 ± 0.000 006 days. The reason behind the asymmetry of the transit shape is not understood at this point.

Conclusions. These two new planetary systems have very interesting properties and deserve further study, particularly in the case of the star CoRoT-29.

Key words. planetary systems - techniques: photometric - techniques: radial velocities - techniques: spectroscopic

# 1. Introduction

Spaceborne surveys of transiting extrasolar planets like CoRoT (Baglin et al. 2006) or Kepler (Borucki et al. 2010) have provided crucial evidence of the interactions between stars and planets and their common evolution. In this paper we report the discovery and characterization of two systems with interesting properties.

\*\* Appendices are available in electronic form at http://www.aanda.org

CoRoT-28b is a hot Jupiter orbiting an evolved star. We investigated the stellar and planetary properties, in particular the rotation and metallicity of the star, and found a lithium abundance higher than expected for its evolutionary state.

CoRoT-29b is a bit of a riddle. The transit discovered by CoRoT is significantly asymmetric, a signature that the host star could have a non-spherical shape. The asymmetry measured by CoRoT has been confirmed by ground-based observations at several observatories. We developed a code that successfully models the transit light curve assuming that the star is oblated. The deformation of the star implied by our model, however, is far too large compared to our current understanding of stellar interiors. Other possible scenarios are bands of stellar spots on the surface of the star, which if properly placed, could also reproduce the transit light curve measured. We show the observational evidence and our modelling efforts, but we leave open the question of the origin of the asymmetry.

## 2. CoRoT observations and data reduction

#### 2.1. General description

The satellite CoRoT observed the field LRc08 (pointing coordinates 18h 28m 34.7s, 5°36'0.0") in 2011 between 6 July

<sup>\*</sup> The CoRoT space mission, launched on December 27th 2006, was developed and is operated by CNES, with the contribution of Austria, Belgium, Brazil, ESA (RSSD and Science Programme), Germany, and Spain. Based on observations obtained with the Nordic Optical Telescope, operated on the island of La Palma jointly by Denmark, Finland, Iceland, Norway, and Sweden, in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofisica de Canarias, in time allocated by OPTICON and the Spanish Time Allocation Committee (CAT). The research leading to these results has received funding from the European Community's Seventh Framework Programme (FP7/2007-2013) under grant agreement number RG226604 (OPTICON). This work makes use of observations from the LCOGT network.



Fig. 1. Second Palomar Observatory Sky Survey (POSS II, Reid et al. 1991) image around the CoRoT-28 (*left*) and CoRoT-29 (*right*) targets. We have over-plotted the CoRoT masks used in the observations and we give identification labels for the brightest, closest background stars. The mask of CoRoT-28 shows the subdivision in the three submasks, named from north to south: red, green, and blue.

Table I.	IDs,	coordinates,	and	magnitudes	of	CoRoT-28	and
CoRoT-29.							

CoRoT name	CoRoT-28b	CoRoT-29b
window ID	LRc08 E2 0275	LRc08 E2 3502
CoRoT ID	652180991	630831435
USNO-A2 ID	0900-13187173	0900-13220969
USNO-B1 ID	0955-0374996	0964-0373597
2MASS ID	18344520+0534254	18353650+0628467
Coordinates		
RA (J2000)	18h 34m 45.21s	18h 35m 36.50s
Dec (J2000)	5°34'25.72"	6°28′46.99″
Magnitudes		
Filter	Val	ues
$B^a$	$14.994 \pm 0.033$	$16.704 \pm 0.105$
$V^a$	$13.775 \pm 0.022$	$15560\pm0.069$
		$15.500 \pm 0.009$
$r'^a$	$13.246 \pm 0.012$	$15.090 \pm 0.009$ $15.090 \pm 0.060$
r' <sup>a</sup> i' <sup>a</sup>	$\begin{array}{c} 13.246 \pm 0.012 \\ 12.627 \pm 0.036 \end{array}$	$15.090 \pm 0.009$ $15.090 \pm 0.060$ $14.515 \pm 0.025$
$r'^a$ $i'^a$ $J^b$	$13.246 \pm 0.012 \\ 12.627 \pm 0.036 \\ 11.601 \pm 0.023$	$\begin{array}{c} 15.500 \pm 0.009 \\ 15.090 \pm 0.060 \\ 14.515 \pm 0.025 \\ 13.565 \pm 0.021 \end{array}$
$r'^{a}$ $i'^{a}$ $J^{b}$ $H^{b}$	$13.246 \pm 0.012 \\ 12.627 \pm 0.036 \\ 11.601 \pm 0.023 \\ 11.143 \pm 0.025$	$\begin{array}{c} 15.500 \pm 0.009 \\ 15.090 \pm 0.060 \\ 14.515 \pm 0.025 \\ 13.565 \pm 0.021 \\ 13.120 \pm 0.021 \end{array}$
$r'^a$ i $'^a$ J $^b$ H $^b$ K $^b$	$13.246 \pm 0.012 12.627 \pm 0.036 11.601 \pm 0.023 11.143 \pm 0.025 11.032 \pm 0.025$	$\begin{array}{l} 15.300 \pm 0.000 \\ 15.090 \pm 0.060 \\ 14.515 \pm 0.025 \\ 13.565 \pm 0.021 \\ 13.120 \pm 0.021 \\ 13.048 \pm 0.031 \end{array}$
$r^{ra}$ $i'^a$ $J^b$ $H^b$ $K^b$ $W1^c$	$13.246 \pm 0.012 12.627 \pm 0.036 11.601 \pm 0.023 11.143 \pm 0.025 11.032 \pm 0.025 10.912 \pm 0.022 $	$\begin{array}{l} 15.300 \pm 0.000 \\ 15.090 \pm 0.060 \\ 14.515 \pm 0.025 \\ 13.565 \pm 0.021 \\ 13.120 \pm 0.021 \\ 13.048 \pm 0.031 \\ 12.974 \pm 0.030 \end{array}$
$r^{Ja}$ $i'^{a}$ $J^{b}$ $H^{b}$ $K^{b}$ $W1^{c}$ $W2^{c}$	$13.246 \pm 0.012 12.627 \pm 0.036 11.601 \pm 0.023 11.143 \pm 0.025 11.032 \pm 0.025 10.912 \pm 0.022 10.987 \pm 0.022$	$\begin{array}{l} 15.300 \pm 0.060 \\ 15.090 \pm 0.060 \\ 14.515 \pm 0.025 \\ 13.565 \pm 0.021 \\ 13.120 \pm 0.021 \\ 13.048 \pm 0.031 \\ 12.974 \pm 0.030 \\ 13.064 \pm 0.036 \end{array}$
$r^{Ja}$ $i'^{a}$ $J^{b}$ $H^{b}$ $K^{b}$ $W1^{c}$ $W2^{c}$ $W3^{c}$	$13.246 \pm 0.012 12.627 \pm 0.036 11.601 \pm 0.023 11.143 \pm 0.025 11.032 \pm 0.025 10.912 \pm 0.022 10.987 \pm 0.022 11.866 \pm 0.314$	$\begin{array}{l} 15.300 \pm 0.060 \\ 15.090 \pm 0.060 \\ 14.515 \pm 0.025 \\ 13.565 \pm 0.021 \\ 13.120 \pm 0.021 \\ 13.048 \pm 0.031 \\ 12.974 \pm 0.030 \\ 13.064 \pm 0.036 \\ 12.088 \pm 0.295 \end{array}$

**Notes.** <sup>(a)</sup> Provided by ExoDat (Deleuil et al. 2009); <sup>(b)</sup> from 2MASS catalogue; <sup>(c)</sup> WISE photometry from Wright et al. (2010).

and 30 September. The CoRoT data for the run LRc08 has been public since 7 June 2013 and can be obtained through the IAS CoRoT Archive<sup>1</sup>.

The coordinates, identification labels, and magnitudes of the stars CoRoT-28 and CoRoT-29 are given in Table 1. CoRoT-28 is a relatively bright target and it was assigned an observing cadence rate of 32 s from the start of the observations, collecting 225 087 measurements with a chromatic mask. CoRoT-29 is a fainter target and was assigned the cadence rate of 512 s. When the first transits were discovered by the Alarm Mode,



**Fig. 2.** Raw light curve of CoRoT-28. The original data points, sampled at 32 s, are shown in blue. We have binned the data to 512 s bins to guide the eye.

the target was assigned a sampling rate of 32 s, collecting in total 121 288 measurements with a monochromatic mask. The region around both targets, indicating the position of the nearest contaminants and the orientation of the masks, is shown in Fig. 1. For an overview of the CoRoT observing modes, please refer to Boisnard & Auvergne (2006), Barge et al. (2008), Auvergne et al. (2009).

#### 2.2. CoRoT-28b

The raw light curve of CoRoT-28 is shown in Fig. 2. We treated the EN2 level<sup>2</sup> light curve of CoRoT-28 observed by CoRoT in its version 3.0. The removal of the influence of instrumental systematics and stellar variability is a necessary step before obtaining the planetary parameters from the light-curve fit. Standard methods consist in the subtraction of a low-level polynomial (in our case, a parabola) to an interval around each transit with a length of a few transit durations (in our case, three). This method

http://idoc-corot.ias.u-psud.fr/

 $<sup>^2</sup>$  For more information about the CoRoT data products, please see Baudin et al. (2006).

was applied successfully with the light curve of CoRoT-28, and we then proceeded to the modelling of the planetary parameters as described in Sect. 4.1.

# 2.3. CoRoT-29b

In the case of CoRoT-29, the standard reduction procedures described in Sect. 2.2 revealed a feature with the shape of non-zero slope in the bottom of the transit shape, which is otherwise expected to be reasonably flat. The slope of the bottom part of the transit is non-zero with 95% confidence level in the 32 s sampled data by CoRoT, and only non-zero with 1 $\sigma$  significance in the 512 s sampled data set. But at the same time, CoRoT-29 is a fainter star than CoRoT-28 and its light curve has more noise at the timescales comparable with the transit length. We therefore decided to use a more robust filtering for this light curve.

We followed the procedure described in Alapini & Aigrain (2009), which iteratively fits the planetary parameters, subtracts the planetary model from the data, creates a model of the stellar variability, then subtracts the stellar variability model from the original data, and then fits the planetary parameters again until the method converges to a final set of planetary parameters and stellar activity pattern. In the first iteration, we used a sliding time window of 0.5 days in length to deal with the variations due to activity. For the interpolation, we removed the points measured during the transit. But for the next iteration steps we divided the light curve in intervals of 0.5 days and fitted each interval with a Legendre polynomials of order 5. This was chosen because a sliding window with short timescales might have an influence on sharp features in the light curve, such as the transit ingress or egress, and the method might fail to converge (see also the discussion in Bonomo et al. 2012).

We tried with intervals from 0.5 to 1.5 days in steps of 0.1 days and though the removal of the systematics is not equally satisfactory for each interval, the non-zero slope in the bottom transit of CoRoT-29b remained. A Legendre polynomial of order 5 within a 0.5 day window provides a smooth fit to the data and it is able to remove the contributions from the out-oftransit, spot-induced stellar activity and low-frequency instrumental systematics present in the data. The regions of the light curve sampled at 512 s and at 32 s were treated as independent data sets. Our method converged after three iterations (one with the sliding window and two with the Legendre polynomials, see Fig. 3).

#### 2.4. Background correction of CoRoT-29b

Comparing the transits of the section of the CoRoT light curve sampled at 512 s and at 32 s, we were able to identify a change in the observed transit depth, which required further study (see Fig. 4). Auvergne et al. (2009) described the photometric capabilities of the CoRoT satellite in detail. However some of those capabilities have slightly degraded with the ageing of the instrument. One effect is the increase of the dark current of the CCD, which has an important impact on the on-board photometry. The dark current of the CCD was modelled as a uniform value calculated in 196 (14  $\times$  14) windows distributed along the CCD: 3/4 of them sampled at 512 s and 1/4 of them sampled at 32 s. The correction applied to the 32 s and 512 s light curves was the median value of the 32 s and 512 s background windows, respectively, to mitigate the impact of hot pixels and cosmic ray impacts. However, with the ageing of the CCD, the uniform model for the dark current is no longer a faithful description of the phenomenon. We observed a gradient along the Y axis of the CCD



**Fig. 3.** Iterative filtering applied to the light curve of CoRoT-29b, converging in three steps (labelled A, B, and C). *Top* of each panel shows the light curve (normalized flux vs. CoRoT Julian Date, which is  $HJD - 2\,451\,545.0$ ), the *bottom figures* on each panel show the folded light curves (normalized flux vs. orbital phase).

whose slope has increased with time. Moreover, the distribution of background windows sampled at 512 s and 32 s is not uniform, which introduces an additional bias in the background correction. The median background level at 32 s sampling is calculated in a region of the CCD that has in average a lower Y value than the average of the windows sampled at 512 s, which introduces a visible difference in the mean level of the light curve

 $\begin{array}{c} \begin{array}{c} 0.998\\ 0.997\\ 0.996\\ 0.995\\ 0.994\\ 0.993\\ 0.992\\ \hline \\ -0.04 \\ -0.02 \\ 0.00 \\ 0.00 \\ 0.02 \\ 0.04 \\ time (phase) \end{array}$ 

512s sampling

32s sampling

1.002

1.001

1.000

**Fig. 4.** Change in the transit depth of CoRoT-29b observed in the light curves sampled at 512 s and 32 s (version 3.0 of the data).

at the two different sampling rates. This effect is common to all light curves on the CCD during this particular run, but it cannot be seen in the light curve of CoRoT-28, as this target was only sampled at the 32 s cadence. This effect can be mitigated by modifying the corresponding background correction for each star as a function of its position on the CCD, a feature that will be introduced in future releases of CoRoT data.

The CoRoT pipeline is currently implementing an improved background correction to mitigate this effect. We used the data of this improved pipeline (version  $3.5^3$ ). However, the final planetary parameters determined when using the previous (version 3.0) or the new data (version 3.5) are not significantly different. Our modelling fits the background contamination as a free parameter, and can deal with the residuals left by the background correction from the pipeline. The incomplete background correction pipeline dilutes the transit signal as if there was an additional contribution of light from a background star, a well-known effect that can be corrected with standard procedures.

# 3. Ground-based observations

The main objective of ground-based photometric follow-up is to check whether the observed transit features occur on the target star or might arise on a nearby eclipsing-binary system (Deeg et al. 2009). Then, ideally, low-resolution spectroscopic measurements characterize the nature of the stellar target before high-resolution radial velocity measurements independently confirm the planetary nature of the target providing a value of its mass (Moutou et al. 2009). This section describes the ground-based observations carried out to characterize these CoRoT targets.

# 3.1. Photometric measurements

#### CoRoT-28b

Photometric follow-up of CoRoT-28b was performed with the IAC80 (Tenerife) and the Euler (La Silla) telescopes. Photometric data were acquired at the 80 cm telescope of the IAC on Tenerife (IAC80). Measurements during the transit (on) obtained on 9 October 2011 and out-of-transit (off) data

![](_page_3_Figure_12.jpeg)

**Fig. 5.** Superposition of the transits of CoRoT-29b observed by CoRoT (small gray points) in 2011 and the transit observed by FTN in 2012 (large blue points). This is not a fit. In this figure we just superpose the FTN and the CoRoT data corrected from the contamination measured in the light curve. The contamination value was obtained exclusively from the fit to the CoRoT data. See text for discussion.

taken on 25 October 2011 showed an on-off brightness variation of 0.3%, but at a low level of confidence. Each observing run lasted 33 minutes. Conversely, relevant brightness variations could be excluded with high confidence on the neighboring stars (stars 2, 3, 6, 13, and 16 in Fig. 1). A star some 17"SSW of the target, on which photometry was performed, was found to be 5.8 mag fainter than the target and hence too faint to cause a false alarm; the recognizable stars that were closest to the target were even fainter (about 4"N and 5"S; no photometry could be performed on them). In the data from the Euler telescope, taken in 2011 on 29 August (on) and on 2 September (off), no eclipses were found, neither on-target nor on any nearby stars. Given that the uncertainty in the ephemeris at the time of both observations was only 4 minutes, we can therefore conclude that the transits must occur on the target.

# CoRoT-29b

Photometric follow-up observations of CoRoT-29b were performed on several occasions. A full transit was obtained on 28 May 2012 with the 2m Faulkes Telescope North (FTN). The analysis of this data showed a clear transit on CoRoT-29 itself. There are several nearby stars which fall within the same point spread function (PSF) and aperture in the CoRoT data, contaminating flux of the mask of CoRoT-29. Most of this contamination is due to a similarly bright star at a distance of 10"NW which can be well separated in the ground based images. Therefore the real depth of the transit, as it is observed from ground is 1.5% (measured from FTN observations) instead of the 0.6% in the CoRoT light curve, because the contaminating star accounts for about 50% of the flux in the CoRoT mask (see Table 6). The FTN observations show also the non-flat feature at the bottom of the transit observed by CoRoT (see Fig. 5). Given the on-target detection of the transit, contamination from eclipsing binaries at distances larger than 2" could be excluded as a source of false alarm.

Further ON-OFF photometry undertaken by the 3.5 m CFHT on 10 May 2013 also showed an on-target transit with a depth of  $1.4 \pm 0.3\%$ .

A full transit of CoRoT-29b was observed with IAC80 in the night of 14 July 2014. The transit centre time, at BJD 2 456 853.435  $\pm$  0.005, was used to refine the ephemeris

<sup>&</sup>lt;sup>3</sup> The version 3.0 of the data is already publicly accessible through the IAS CoRoT Archive (http://idoc-corot.ias.u-psud.fr/). The version 3.5 of the data will be publicly available in coming months.

![](_page_4_Figure_1.jpeg)

**Fig. 6.** Superposition of the transits of CoRoT-29b observed by CoRoT (small gray points) in 2011 and the transit observed by IAC80 in 2014 (large blue points). Same conditions as in Fig. 5.

in Table 6. It also shows some degree of asymmetry, though it is difficult to assess it with the same confidence level as for FTN data (see Fig. 6). The ingress is partially missing, complicating the assessment of any possible out-of-transit slope, either caused by stellar activity or by residuals of the data reduction (airmass correction, instrumentals, etc.).

#### 3.2. Radial velocity measurements

#### CoRoT-28b

Radial velocity measurements were first obtained with the SOPHIE (Perruchot et al. 2008; Bouchy et al. 2009) spectrograph on the 193 cm telescope at the Observatoire de Haute-Provence (France) and showed variations in phase with the CoRoT ephemeris, establishing the planetary nature of the candidate. A total of 25 radial velocity measurements were acquired in High Efficiency mode (R = 40000) with SOPHIE between 27 August 2011 and 17 August 2012. An additional seven measurements between 7 July 2012 and 10 August 2013 were performed using the HARPS spectrograph in standard HAM mode  $(R = 115\,000)$  (Mayor et al. 2003) mounted on the 3.6 m ESO telescope at La Silla Observatory (Chile) as part of the ESO large program 188.C-0779. Finally, ten spectra of CoRoT-28 were taken at different epochs between June and July 2012 using the FIbre-fed Échelle Spectrograph (FIES; Frandsen & Lindberg 1999; Telting et al. 2014) mounted at the 2.56-m Nordic Optical Telescope (NOT) of Roque de los Muchachos Observatory (La Palma, Spain). We employed the high-res fibre, which provides a resolving power of  $R = 67\,000$  in the spectral range 3600-7400 Å.

The SOPHIE and HARPS spectra were extracted using the respective pipelines. The radial velocities were then computed following a technique of weighted cross-correlation of the spectra using a numerical G2 star mask. This technique is described by Baranne et al. (1996) and Pepe et al. (2002). The spectral orders with low signal-to-noise ratio (S/N) were discarded to perform the computation to reduce the dispersion of the measurements. We eliminated the two bluest and five reddest orders for SOPHIE (39 in total), the ten bluest and the two reddest for HARPS (72 in total). The cross-correlation function of CoRoT-28b shows a single peak with FWHM of 9.9 km s<sup>-1</sup> with SOPHIE and 7.6 km s<sup>-1</sup> with HARPS. Also, SOPHIE and

![](_page_4_Figure_8.jpeg)

**Fig. 7.** Radial velocity measurements and best solution for CoRoT-28. Offsets have been subtracted according to the values given in Table 6.

![](_page_4_Figure_10.jpeg)

Fig. 8. Bisector span as a function of radial velocities for CoRoT-28. We subtracted the systemic velocities in the x axis. The uncertainties in the bisector span is assumed to be twice the uncertainties in the radial velocities. The bisector span shows no correlation with the radial velocities.

HARPS radial velocities obtained with different numerical spectral masks (F0, G2 and K5) show the same behaviour, suggesting that the radial velocity variations cannot be explained by a blend scenario with different spectral type stars.

For the FIES data, we adopted the same observing strategy described in Buchhave et al. (2010), i.e. we split each epoch observation into three consecutive exposures of 1200 s to remove cosmic rays hits, and we acquired long-exposed ThAr spectra in "sandwich-mode" to trace the RV drift of the instrument. We reduced the data using a customized IDL software suite, which includes bias subtraction, flat fielding, order tracing and extraction, and wavelength calibration. We obtained radial velocity measurements performing a multi-order cross-correlation with the RV standard star HD 182572, observed with the same instrument set-up as the target object, and for which we adopted an heliocentric radial velocity of  $-100.350 \text{ km s}^{-1}$ , as measured by Udry et al. (1999).

The radial velocity measurements with the best orbital solution are shown in Fig. 7, assuming the period and transit epoch determined by the CoRoT light curve. Finally, the crosscorrelation function bisector span shows no correlation with the radial velocities (see Fig. 8), reinforcing the conclusion that the radial velocity variations are not due to a blending effect. Radial

![](_page_5_Figure_1.jpeg)

**Fig. 9.** Radial velocity measurements and best solution for CoRoT-29. Offsets were subtracted according to the values given in Table 6.

velocities, their errors, and bisector span are listed in Tables A.1 to A.3.

For CoRoT-28b, we fit SOPHIE, HARPS, and FIES data together while fixing the ephemeris derived from the lightcurve analysis (see Table 6). The rest of the orbital parameters (orbital eccentricity, argument of periastron, radial velocity semi-amplitude, and systemic velocities) were derived using the modelling procedure and Markov Chain Monte Carlo module from PASTIS (Díaz et al. 2014). The priors used for the orbital parameters were non-informative (uniform priors) except for the period and the transit epoch that were fixed. The results are summarized in Table 6.

#### CoRoT-29b

Because of its faintness (V = 15.6), CoRoT-29 radial velocity follow-up could only be performed with HARPS in the EGGS mode to improve the throughput. Compared to the HAM mode, which was used to follow up CoRoT-28, the EGGS mode of HARPS has a larger fiber (1.4" compared to 1") and no scrambler. The spectral resolution is therefore reduced ( $R = 80\,000$ ) but the throughput is twice as large. We obtained 20 measurements between 19 June 2012 and 10 August 2013, showing that the radial velocity variations were in agreement with the CoRoT ephemeris and establishing the planetary nature of CoRoT-29b (see Fig. 9). The same cross-correlation technique with a G2 spectral type numerical mask allowed us to derive the radial velocities. As for CoRoT-28, the ten bluest and the two reddest orders were discarded. We obtained a 7.1 km s<sup>-1</sup> single peak cross-correlation function. Also, cross-correlation with other masks (F0 and K5) show no discrepancies in the radial velocity variations. Moreover, the cross-correlation function bisector span shows no correlation with the radial velocities (see Fig. 10). This suggests that the probability to have a blending effect is very low. The radial velocity measurements are represented in Fig. 9 and are listed with their errors and bisector spans in Table A.4.

We also fit CoRoT-29b HARPS data while fixing the ephemeris as described above for CoRoT-28b and the results are also summarized in Table 6.

#### 3.3. Spectroscopic characterization

To derive the stellar parameters from the spectroscopic data, we used the Spectroscopy Made Easy (SME) package (version 5, February 2014). The development and structure and

![](_page_5_Figure_11.jpeg)

Fig. 10. Bisector span as a function of radial velocities for CoRoT-29. We subtracted the systemic velocities in the x axis. The uncertainties in the bisector span is assumed to be twice the uncertainties in the radial velocities. The bisector span shows no correlation with the radial velocities.

performance of SME is described in Valenti & Piskunov (1996) and in e.g. Valenti & Fischer (2005). Briefly, this code uses a grid of stellar models to which is fitted the observed spectrum. This is done by calculating a synthetized spectrum and minimizing the discrepancies through a non-linear, least-squares algorithm. The analysis is based on the latest generation of MARCS model atmospheres (Gustafsson et al. 2008) and the ATLAS12 models (Kurucz 2005). The models calculate the temperature and pressure distribution in radiative and hydrostatic equilibrium, assuming a plane-parallel stellar atmosphere.

The SME is developed so that, by matching synthetic spectra to observed line profiles, one can extract the information in the observed spectrum and search among stellar and atomic parameters until the best fit is achieved. The SME utilizes automatic parameter optimization using a Levenberg-Marquardt  $\chi^2$  minimization algorithm. Synthetic spectra are calculated on the fly, by a built-in spectrum synthesis code, for a set of global model parameters and specified spectral line data. Starting from userprovided initial values, synthetic spectra are computed for small offsets in different directions for a subset of parameters defined to be "free". The model atmospheres required for this are calculated through interpolating the grid of models mentioned above.

We used as input data the high-resolution spectra taken with HARPS (see Sect. 3.2). In the observed spectra, we use a large number of spectral lines, e.g. the Balmer lines (the extended wings are used to constrain  $T_{\text{eff}}$ ), Na I D lines, Mg I b, and Ca I (for  $T_{\text{eff}}$  and log g) and a large number of metal lines (to constrain the abundances). For CoRoT-28, we obtained a Li I equivalent width of 31 mÅ at 6708 Å.

After finding the  $T_{\rm eff}$  from the Balmer line wings (e.g. Fuhrmann et al. 1998), we use the calibration of Bruntt et al. (2010) to fix the micro- and macro-turbulence parameters before finding other parameters. The quoted errors are  $1\sigma$  standard deviation errors in SME and thus a measure of how well the generation of the synthetic spectrum has succeeded. We know (Fridlund et al., in prep.) that when we apply SME to our (only) known source, the Sun, we find somewhat larger errors such as  $a \pm 100$  K difference in  $T_{\rm eff}$ , and  $a \pm 0.1$ dex in [Fe/H] (as proxy for metallicity) depending on the choice of model grid being used (e.g. Atlas12 or MARCS 2012). The mass, radius, and age of the star are calculated using stellar evolution tracks from Hurley et al. (2000) and the constraints from the analysis of the light curve (see Sect. 4). They are reported in Table 6.

Table 2. Parameters of the fit to the transit light curve of CoRoT-28b.

Parameter	Value and uncertainty			
	in blue	in green	in red	in white
$a/R_{\rm s}$	$7.1 \pm 1.7$	$6.7 \pm 2.7$	$7.40\pm0.68$	$7.29 \pm 0.16$
$k = R_{\rm p}/R_{\rm s}$	$0.0614 \pm 0.0073$	$0.0600 \pm 0.0107$	$0.0581 \pm 0.0033$	$0.0551 \pm 0.0004$
b	$0.43 \pm 0.36$	$0.54 \pm 0.47$	$0.30 \pm 0.26$	$0.24 \pm 0.09$
$u_+$	$0.42 \pm 0.32$	$0.71 \pm 0.40$	$0.43 \pm 0.39$	$0.78 \pm 0.11$
$u_{-}$	$0.32 \pm 0.62$	$0.18 \pm 0.59$	$0.40 \pm 0.58$	$0.37 \pm 0.22$
Contamination [%]	$6.2 \pm 3.0$	$6.4 \pm 3.0$	$2 \pm 1$	$3 \pm 1$
$\chi^2_{\rm red}$	1.24	1.28	1.20	1.32

Additionally, we estimated the interstellar extinction  $A_v$  and spectroscopic distance d to CoRoT-28 and CoRoT-29 following the method described in Gandolfi et al. (2008). We simultaneously fitted the available ExoDat, 2MASS, and WISE colours (Table 1) with synthetic theoretical magnitudes derived by *NextGen* low-resolution model spectra (Hauschildt et al. 1999) having the same photospheric parameters as the stars. We excluded the  $W_3$  and  $W_4$  WISE magnitudes because of the low S/N. Assuming a normal extinction ( $R_v = 3.1$ ), we found that CoRoT-28 and CoRoT-29 are at 560 ± 70 pc and 765 ± 50 pc from the Sun, and suffer an interstellar extinction of  $A_v =$  $0.75 \pm 0.20$  mag and  $A_v = 0.85 \pm 0.15$  mag, respectively. The dereddened B-V excess of the stars is  $0.98\pm0.06$  and  $0.87\pm0.03$ mag, respectively.

#### 3.4. Spectral typing

A spectral type was derived for CoRoT-28 from a spectrum taken on 24 July 2012, with the low-resolution spectrograph  $(\frac{\lambda}{\lambda d} \approx$ 1000) at the Nasmyth focus of the 2m telescope in Tautenburg. A slit width of 1" and the V200 grism were used covering the wavelength range 360-935 nm. The S/N of the spectrum is about 180. The spectrum was reduced and extracted with IRAF (Tody 1986, 1993) in the standard way, including subtraction of the bias and the background as well as flat-field and extinction correction. Wavelengths were calibrated using sky lines in the longslit spectra and exposures of He and Kr gas discharge lamps. The spectral type of CoRoT-28 was obtained following Gandolfi et al. (2008) and Sebastian et al. (2012). Briefly, we fitted the observed low-resolution spectrum using template spectra from the library by Valdes et al. (2004) in combination with the photospheric parameters derived by Wu et al. (2011). Although a best match was attained for G8/G9V templates, we also found matching templates with spectral classes G5-K0 and luminosity classes IV and III. The luminosity class is not well defined by the low-resolution spectrum. For the reasons explained above and considering the transit parameters, we consider that the star is slightly evolved and classify it as G8/9IV. For CoRoT-29, considering the effective temperature, we choose a spectral type K0V following Kenyon & Hartmann (1995).

#### 4. Planetary parameters

#### 4.1. CoRoT-28b

For the transit analysis and final planetary parameter determination of CoRoT-28b, we used the light curve that was filtered for stellar variability, as explained in Sect. 2.2, and the information from the spectral analysis described in Sect. 3. Since no significant transit timing variations (TTVs) were found, we folded the light curve using the ephemeris in Table 6. The folded light curve was then modelled with the *Transit Light Curve Model* code, described in Csizmadia et al. (2011). Each chromatic light curve (red, green, blue, and white, see Sect. 2.1) was treated in the same way. For the transit light-curve fit, we used the Mandel & Agol (2002) model. The optimization process consists of two steps. First, the best solution is found with a Harmony Search analysis genetic algorithm (Geem et al. 2001). Second, the uncertainties of the parameters are obtained via simulated annealing around the best solution found by the genetic algorithm.

The free parameters are the scaled semi-major axis  $(a/R_s)$ , where a is the semi-major axis and  $R_s$  is the stellar radius), the planet-to-stellar radius ratio ( $k = R_p/R_s, R_p$  is the planetary radius), the impact parameter b, where  $b = a \cos i \sqrt{1 - e^2/R_s(1 + e^2)/R_s)}$  $e \sin \omega$ ), *i* is the inclination, *e* is the eccentricity, and  $\omega$  is the argument of the periastron. Values of e and  $\omega$  are known from the radial velocity analysis, and their uncertainties were propagated allowing them to vary between their  $\pm 1\sigma$  uncertainties during the optimization procedure. The epoch could also vary within the uncertainties reported in Table 6. Following Csizmadia et al. (2013), limb darkening coefficients were fitted as free parameters. We took the results of Brown et al. (2001) and Pál & Kocsis (2008) into account, fitting the combinations  $u_{+} = u_{a} + u_{b}$  and  $u_{-} = u_{a} - u_{b}$  rather than the linear and quadratic coefficients of  $u_a$  and  $u_b$  individually. A quadratic limb darkening law provided a reasonable fit to the data.

The fit is shown in Fig. 11 and the results can be seen in Table 2. The fits obtained in different colours are in agreement with each other. Note that because of the non-axisymmetric chromatic PSF of CoRoT, the contamination factors are not additive, so contamination in white is not equal to the sum of contaminations in different colours. The white light curve results were used to establish the planetary parameters given in Table 6 because they have the smallest uncertainties because of the higher S/N.

#### 4.2. CoRoT-29b

As described in Sect. 2.3, the light curve of CoRoT-29b has a non-flat, mid-transit shape.

The CoRoT data sets sampled at 512 s and 32 s cadence were treated separately because of the background correction issue described in Sect. 2.4. The slope of the bottom part of the transit is non-zero with 95% confidence level in the 32 s sampled data by CoRoT, and only non-zero with 1 $\sigma$  significance in the 512 s sampled data set. It is also non-zero with 99% confidence level in the ground-based data from FTN, and non-zero with 95% confidence level in the CoRoT data and in the ground-based data are compatible with each other within 1 $\sigma$  uncertainties, though the data from ground and from space were taken in slightly different wavelengths and suffer from different kind of systematic effects.

![](_page_7_Figure_1.jpeg)

Fig. 11. The folded light curve of CoRoT-28b together with the best fit in the different chromatic light curves observed by CoRoT. Blue points are the observed data; the orange curves represent the individual fits.

We have not been able to identify any systematic residual in the CoRoT data, which could account for the asymmetry of the transit; neither identified any other target in the CoRoT data set with a similar asymmetry. Ground-based observations are affected by correlated noise, which can produce asymmetries in the transit shape (see, for example, Hebb et al. 2010; Dittmann et al. 2010; Mancini et al. 2013). But in this case, despite the inherent limitations of the ground-based photometric observations that we present (see Sect. 3.1), we consider that the asymmetry observed by CoRoT is confirmed by the ground-based observations, and therefore it could have an astrophysical origin.

Possible interpretations for the asymmetry of the transit are given in the next Sect. 4.3, if the 2 sigma detection is assumed to be significant. The model that better reproduces the data is that including the gravity darkening produced by an oblate star (see Sect. 4.3.1). We have taken those values as the reference planetary parameters (see Table 6).

#### 4.3. Interpretations of the transit light curve of CoRoT-29b

#### 4.3.1. Stellar oblateness

We could interpret the shape of the light curve as the result of the transit of the planet above a non-spherical stellar surface. A spherical surface becomes ellipsoidal, in a first approximation, when it is deformed by its rotation, by its internal mass distribution, or by the tidal influence of a massive companion. Consequently, the stellar poles are closer to the centre of the star than the equator, thus the absorption rate of photons from the stellar interior is different. Additionally, the effective gravitational acceleration is higher at the poles than at the equator, where the centrifugal force reaches its maximum. The decrease of the effective gravitational acceleration at the equator affects the stellar atmospheric scale height, which in turn changes the stellar temperature layering. All these effects cause a pole-toequatorial variation in the stellar flux, which is called gravity darkening, because this temperature latitudinal variation is characterized by the effective surface gravity g at a certain latitude band with a gravity darkening exponent  $\beta$ ,

$$T(b) = T_{\text{pole}} \left(\frac{g(b)}{g_{\text{pole}}}\right)^{\beta}$$
(1)

The gravity darkening effect was studied by von Zeipel (1924), Lucy (1967), Claret (1999, 2012) from theoretical point of view. In the context of transiting extrasolar planets, this effect was studied in depth by Barnes (2009). Important observational results, in eclipsing binary stars and transiting extrasolar planets, have been published by Rafert & Twigg (1980), Nakamura & Kitamura (1992), Djurašević et al. (2003), Szabó et al. (2011), Morris et al. (2013), Barnes et al. (2013), Zhou & Huang (2013).

As is shown hereafter, we successfully explained the observed transit light-curve shape of CoRoT-29b with the assumption that the asymmetry of the light curve is caused by gravity darkening effect. We modelled this effect with our own code, which we briefly describe next, and which will be describe in detail in a future publication (Csizmadia, in prep.). The optimization method is identical to the one described before (see Sect. 4.1). For this fit, we used the spectroscopic constraints for the  $v \sin i$  and  $T_{\rm eff}$  from the spectroscopic analysis of the star. We allowed these parameters to vary between  $3.5 \pm 0.5 \,\rm km \, s^{-1}$  and  $5260 \pm 70 \,\rm K$ , respectively. Here  $T_{\rm eff}$  is the surface temperature of the star averaged for the visible hemisphere.

The stellar shape is defined by V = constant equipotential surfaces. We use the quadrupolar approach (e.g. Zahn et al. 2010) instead of the simple ellipsoidal approximation of Barnes (2009),

$$V = -\frac{GM_{\rm s}}{R(b)} \left( 1 - J_2 \left( \frac{R_{\rm s,eq}}{R(b)} \right)^2 P_2(\sin b) \right) - \frac{1}{2} \Omega_{\rm rot}^2 R^2(b) \cos^2 b.$$
(2)

This equation can be rewritten in a dimensionless form as

$$\Psi = \frac{VR_{\rm s,eq}}{GM_{\rm s}} = -\frac{1}{r(b)} \left( 1 - \frac{J_2}{r(b)^2} P_2(\sin b) \right) - \frac{1}{2} \frac{w^2 r(b)^2 \cos^2 b}{(a/R_{\rm s,eq})^3}$$
(3)

Here we used the following notations:

- $R_{s,eq}$ , equatorial radius of the star,
- *G*, gravitational constant,
- $M_{\rm s}$ , mass of the star,
- $r(b) = R(b)/R_{s,eq}$ , the normalized radius of the star at latitude *b*,
- $w = P_{\text{orb}}/P_{\text{rot}}$ , a rotational parameter, namely the ratio of the orbital period of the planet and the rotational period of the star,
- $a/R_{s,eq}$ , the scaled semi-major axis where *a* is the semi-major axis of the planet,
- $J_2$ , the second (or quadrupole's) gravitational momentum of the star,
- $P_2$ , the second Legendre-polynomial.

The free parameters are  $J_2$ ; the gravity darkening exponent  $\beta$ ; the planet to stellar radius ratio  $k = R_p/R_s$ ; the stellar inclination angle  $i_s$  (the obliquity of the star, as defined in Barnes 2009, is  $\varphi = 90 - i_s$ ;  $\Omega_s$ , the sky projected angle of the stellar spin axis ( $\lambda$  in the notation of Fabrycky & Winn 2009);  $i_p$ , the inclination of the planetary orbit; the limb darkening coefficients  $u_{+}$ and  $u_{-}$ ; the epoch of the transit  $T_{0}$ ; the temperature of the star at the pole  $T_{\text{pole}}$ ; and the scaled semi-major axis  $a/R_{\text{s,eq}}$  (see also Figs. B.1 and 12). The rotational parameter w was calculated iteratively from the known orbital period and from  $v \sin i$ , assuming a certain average radius of the star. We chose a stellar radius of 1 solar radius as initial value. After the first fit, we calculated the density parameter  $M^{1/3}/R_{s,eq} = (3\pi (a/R_{s,eq})^3/GP_{orb}^2)^{1/3}$  for the star. We searched stellar models by Hurley et al. (2000), which provide this density parameter at the effective surface temperature of the star (within the uncertainties), and this yielded a new estimate for the stellar radius. With this new stellar radius, we repeated the fit until convergence (see Fig. B.1).

The stellar parameters define the value of  $\Psi$ . A Newton-Raphson iterative process yielded the value of r and the actual value of the surface gravity  $g = \nabla V$  for every latitude and longitude. Then we calculated the effective surface temperature as well as the intensity assuming a simple black-body radiation for the star. A numerical integration procedure provided the unobscured flux of the star with a freely chosen gravity darkening exponent and limb darkening coefficients. As is well known, the limb darkening coefficients are functions of the effective stellar surface temperature. If the temperature varies over the surface, different limb darkening coefficients will be valid at each surface point. Since the theoretical limb darkening tables are not

**Table 3.** Parameters of the fit to the transit light curve of CoRoT-29b with a model accounting for gravity darkening.

Fitted parameters	Value and uncertainty
$J_2$	$0.028 \pm 0.019$
Gravity darkening exponent $\beta$	$0.89 \pm 0.25$
$k = R_{\rm p}/R_{\rm s}$	$0.1028 \pm 0.0043$
$i_{\rm s} [\circ]^{a}$	$46 \pm 19$
$\Omega_{ m s}$ [°] <sup>b</sup>	$256 \pm 40$
<i>i</i> <sub>p</sub> [°]	$87.3 \pm 2.7$
$\dot{u}_+$	$0.62 \pm 0.15$
$u_{-}$	$0.58 \pm 0.14$
$T_0$ [s]	$-200 \pm 31$
$T_{\rm pole}[{ m K}]$	$5341 \pm 266$
$a/R_{\rm s,eq}$	$9.22 \pm 0.19$
Contamination factor [%]	$54 \pm 4$
Derived parameters	
$f = R_{\rm s,pole}/R_{\rm s,eq}$	$0.94 \pm 0.02$
$w = P_{\rm orb}/P_{\rm rot}$	$0.26 \pm 0.06$
$\chi^2$	71
$\chi^2_{red}$	1.4
BIC	120

**Notes.** <sup>(a)</sup> The obliquity of the star, as defined in Barnes (2009), is  $\varphi = 90 - i_s = 47^{\circ}$ . <sup>(b)</sup> The sky projected angle of the stellar spin axis;  $\lambda$  in the notation of Fabrycky & Winn (2009). <sup>(c)</sup> Sixty-two fitted points and 12 free parameters.

![](_page_8_Figure_20.jpeg)

Fig. 12. Angle convention used in the gravity darkening model.

always in agreement with each other and they have not been validated observationally, it is hard to accept that an interpolation of these tables will provide the appropriate description of the limb darkening coefficients for every surface point. In addition, a rotating stellar atmosphere can be different from a static atmosphere, whereas most limb darkening tables use non-rotating stellar atmospheric models. Therefore, we left the limb darkening coefficients free and used a quadratic law hoping that this will be a better approximation of reality in this particular case. For further details about the difficulties of limb darkening handling, see Csizmadia et al. (2013). Our code also includes the rotational beaming effect.

The planet's position was projected on the sky and when it crossed the apparent stellar disc, we calculated the amount of the blocked stellar emission in a small-planet approximation (Mandel & Agol 2002). Then we adjusted the free parameters until we had a convergence in the  $\chi^2$ -values, using the optimization methods described before (Sect. 4.1). The results of our

![](_page_9_Figure_1.jpeg)

**Fig. 13.** Binned and folded light curve of CoRoT-29b together with the best fit accounting for gravity darkening fit. See text.

**Table 4.** Parameters of the fit to the transit light curve of CoRoT-29b using a spherically symmetric model for the star.

Parameter	Value and uncertainty
$a/R_{\rm s}$	$10.49 \pm 0.72$
$R_{\rm p}/R_{\rm s}$	$0.0838 \pm 0.0070$
b	$0.08 \pm 0.27$
$u_+$	$0.89 \pm 0.33$
$u_{-}$	$-0.49 \pm 0.38$
$\chi^2$	103
$\chi^2_{\rm red}{}^a$	1.87
BIC	132

**Notes.** We discarded this model as a correct explanation of the measured light curve, as explained in the text. <sup>(a)</sup> Sixty-two fitted points and seven free parameters.

modelling are shown in Table 3 and in graphical form in Fig. 13. The final planetary parameters are also shown in Table 6.

#### 4.3.2. Spherical star model

If we decide to ignore the non-flat shape of the transit and try to model the light curve of CoRoT-29b with the same techniques used in the case of CoRoT-28b (see Sect. 4.1), we obtain a fit solution significantly worse than using the more sophisticated analysis including gravitational darkening. The results are summarized in Table 4 and in graphical form in Fig. 14. Notice the remarkable distribution of the binned points relative to the fit. After the ingress, the observed points are systematically below the fit, and later, during the mid-eclipse and just before the egress phase they are systematically over the best match of the spherical star fit. We conclude that we cannot ignore the asymmetry of the light curve in the observed data set.

#### 4.3.3. Spot-occulting model

Stellar spots occulted by transiting planets can have a significant impact in the measured transit light curve. This phenomenon has been widely studied in the literature and has been confirmed by several observations (Silva 2003; Wolter et al. 2009 and references therein; Sanchis-Ojeda et al. 2012, etc.). We require from a spot-occulting solution to reproduce the observed light curve with a stellar spot coverage, which is consistent with our knowledge of the stellar properties. Typically, the parameters used for

![](_page_9_Figure_12.jpeg)

**Fig. 14.** Binned and folded light curve of CoRoT-29b together with the best fit using a spherically symmetric model of the star. We discarded this model as a correct explanation of the measured light curve as explained in the text.

this models are the stellar temperature and rotational period and the spot temperature, size, lifetime, and distribution.

In particular, the typical lifetime of a spot is  $\sim 2$  weeks for the Sun, but other stars have both shorter and longer lifetimes, up to several months in some cases (Queloz et al. 2001). In our case, comparing the identical CoRoT and the FTN observations (see Sect. 3.1 and Fig. 5), we require a spot lifetime larger than one year.

Secondly, as all planetary transits observed by CoRoT in 2011 are indistinguishable with the current precision level, and they are also indistinguishable from FTN data from 2012 and IAC80 ground-based observations from 2014, we must conclude that the planet transits every 2.85 days above the same spot. This requires an exact synchronization between the stellar rotational period and the planetary orbital period, with exactly the same phase in a baseline larger than three years.

On the one hand, if the observed asymmetry is related to an equatorial or mid-latitude stellar spot, then the stellar rotational period should be equal to the orbital period of the planet, otherwise we cannot observe the spot always in phase with the planetary transits. However, we do not see a signature of such a spot as a modulation of the light curve in phase with the stellar rotational period. Moreover, we require the star to have a rotational period identical to the orbital period, which is not consistent with the stellar parameters derived from spectroscopy (in particular, with the  $v \sin i$ ).

On the other hand, if the spot is polar and the rotational axis of the star is perpendicular to the orbital plane of the planet, then we could not observe an asymmetric light curve. A spotcaused asymmetry requires an off-position of the spot from the apparent stellar disc. This scenario has the advantage that the signature of the spot is diluted in the light-curve signal, and we could not infer from the modulation of the light curve the stellar rotational period. Additionally, if the spot is centred on the pole and the stellar rotation axis has the right orientation, the planet could always cross the same location of the spotted region. This requires no prior assumptions on the stellar rotation period (see Fig. 15).

If we accept the polar spot scenario, however, which a priori cannot be ruled out as easily as the equatorial spot model, then we must require that the polar spot does not change its apparent position during the baseline of the observations. In this model, the rotational axis of the star is very different from the angular momentum of the vector of the planet, or in other words,

![](_page_10_Figure_1.jpeg)

**Fig. 15.** Visualization of the CoRoT-29 system according to the spot model. The scale is in stellar radii. The orange area is the spotted area, while the horizontal line shows the sky-projected planetary orbit. The positions of the planet at different orbital phases are shown; the size of the circles correspond to the planetary radius in this scale. The pole of the star is denoted by a small green cross.

the planetary orbit is misaligned with the equatorial plane of the star. The spot cannot be at the centre of the apparent stellar disc because of the asymmetry of the light curve. According to the light curve, the planet crosses the unspotted surface of the star first, producing a deeper transit, and later the spotted surface, when the lower brightness temperature of the spot produces a shallower transit. The apparent size of the spot should be much larger than the apparent size of the planet because we observe a continuous change in the transit depth and not a step-like event.

Polar spots in active stars are a common phenomenon and in some cases they can survive for long intervals of time. Or at least, active regions continuously producing spots at similar latitudes have been observed for several years in some young active stars like V410 Tau (Hatzes 1995; Rice et al. 2011). But these polar spots are on very active, young stars that are rapidly rotating (V410 Tau has a  $v \sin i$  of 75 km s<sup>-1</sup>). Long-lived polar spots have never been seen, to our knowledge, on more slowly rotating stars like CoRoT-29. Moreover, these spots should produce signatures on the stellar spectrum (Ca II emission, distortion in the line profiles, flat-bottomed line profiles), which are not observed in our data set (see Sect. 3).

Although it is unlikely that a spot can survive for such a long period without evolving on the surface of a main-sequence star, we used this assumption in our modelling with a spherical star, a spherical planet, and a circular spot on the surface of the star, with an arbitrarily oriented stellar rotational axis and arbitrary initial spot properties. We use a quadratic limb darkening law, as before. The results are given in Table 5 and shown in graphical form in Fig. 16.

We obtain a polar spot with a tilted stellar rotational axis. This tilt means here that the projected rotational axis of the star and the projected angular momentum of the planet do not coincide. The planet is on "pole-on" orbit because it orbits the star in such a way that its projected orbit crosses the polar region of the star. The mutual inclination between the stellar equator and planetary orbital plane is practically 90 degrees. Note that such an orbit is very stable against perturbations.

From the measured  $v \sin i$  and from the fitted stellar inclination for the spotted case (assuming  $R_s \sim 0.9 R_{\odot}$ ), we find that the stellar rotational period should be between 0.7–8.4 days. The spectroscopically measured  $v \sin i \sim 3.5$  km s<sup>-1</sup> would yield  $v_{eq} \sim 10$  km s<sup>-1</sup> with  $i_s \approx 20^\circ$ , where the inclination of stellar rotational axis comes from the spot fit.

**Table 5.** Parameters of the fit to the transit light curve of CoRoT-29b using a spherically symmetric model for the star and a stellar spot.

Parameter	Value and uncertainty
$a/R_{\rm s}$	$10.32 \pm 0.24$
$R_{\rm p}/R_{\rm s}$	$0.0948 \pm 0.0031$
i <sub>p</sub>	$90.7 \pm 0.8$
$\dot{u}_+$	$0.90 \pm 0.19$
$u_{-}$	$-0.26 \pm 0.28$
$T_{\rm s}$ [K] (fixed)	5260
$T_{\rm spot}$ [K]	$1600 \pm 400$
b <sub>spot</sub> [°]	$-56 \pm 21$
$l_{\text{spot}}$ [°]	$209 \pm 45$
$\hat{d_{\text{spot}}}$ [°]	$39 \pm 13$
<i>i</i> <sub>s</sub> <sup>[°]</sup>	$-42 \pm 20$
$\Omega_{\rm s}$ [°]	$211 \pm 39$
Contamination factor [%]	$45 \pm 3$
$\chi^2$	84
$\chi^2_{\rm red}$ a	1.75
BIC	133

**Notes.** The parameters  $b_{spot}$ ,  $l_{spot}$  and  $d_{spot}$  are the astrographic latitude, longitude, and diameter of the spot in degrees. The stellar angles are chosen in the same way as in Fig. 12. We discarded this model as a correct explanation of the measured light curve, as explained in the text. <sup>(a)</sup> Sixty fitted points and 12 free parameters.

![](_page_10_Figure_11.jpeg)

**Fig. 16.** Binned and folded light curve of CoRoT-29b together with the red line being the best fit using a spherically symmetric model for the star and a stellar spot. For comparison, the solid green curve is because of the unspotted light curve model (we set  $T_{spot} = T_s$  in the fitting routine). We discarded this model as a correct explanation of the measured light curve, as explained in the text.

The comparison of the Bayesian Information Criterion (BIC) of the spot fit and the gravity darkening fit makes a clear choice which fit is better. The spot fit yielded BIC = 133, whereas the gravity darkening fit produces BIC = 120. This BIC difference corresponds to a Bayes factor of around 665 for the gravity darkening model (i.e. if the prior probabilities for each model are the same, then the gravity darkening is 665 times more probable than the spot model). Moreover, to explain the observational evidence we are obliged to put requirements on the size and temporal evolution of the spot, which are completely ad hoc. We consider that there is enough evidence to discard the spotted star as a reasonable interpretation of the data.

An alternative to the single polar spot would be a band of spots with short lifetimes, but continuously appearing during the baseline of our observations in the same latitudes, relaxing one of the requirements of the scenario. One possibility is that if the spots were conveniently appearing at different

# **Table 6.** Planetary and stellar parameters.

	CoPoT 28h	CoPoT 20b
Fnhemeris	C0K01-260	COR01-290
Planet orbital period P [days]	$520851 \pm 0.00038$	2 850570 + 0 000006
Transit epoch T. [HID-2450 000]	$57558466 \pm 0.0029$	$5753\ 115 \pm 0.000000$
Transit duration $d_{rr}$ [h]	$5.70 \pm 0.09$	$2.19 \pm 0.04$
		2.17 2 0.0 1
Results from radial velocity observations		
Orbital eccentricity e	$0.047^{+0.055}_{-0.038}$	$0.082 \pm 0.081$
Argument of periastron $\omega$ [°]	$126^{+140}_{-61}$	$87^{+210}_{-49}$
Radial velocity semi-amplitude $K [m s^{-1}]$	$56.4 \pm 4.9$	$125 \pm 17$
Systemic velocity $V_r$ (HARPS) [ km s <sup>-1</sup> ]	$76.7081 \pm 0.0051$	$64.1907 \pm 0.0012$
O-C residuals (HARPS) $[m s^{-1}]$	$6.4^{+7.0}_{-4.8}$	$11 \pm 11$
Systemic velocity $V_r$ (Sophie) [ km s <sup>-1</sup> ]	$76.7549 \pm 0.0082$	
U-C residuals (Sopnie) [m s <sup>-1</sup> ]	$32.8 \pm 0.4$	
Systemic velocity $V_r$ (FIES) [ km s <sup>-1</sup> ]	$70.8042 \pm 0.0074$	
U-C residuais (FIES) [ III s ]	$0.3 \pm 0.3$	
Fitted transit parameters		
Scaled semi-major axis $a/R_{s,eq}$	$7.29 \pm 0.16$	$9.22 \pm 0.19$
Radius ratio $k = R_{\rm p}/R_{\rm s}$	$0.0551 \pm 0.0004$	$0.1028 \pm 0.0043$
Quadratic limb darkening coefficients <sup><i>a</i></sup> $u_+$	$0.78 \pm 0.11$	$0.62 \pm 0.15$
<i>u</i> _	$0.37 \pm 0.22$	$0.58 \pm 0.14$
Impact parameter <sup>b</sup> b	$0.24 \pm 0.09$	-
Orbital inclination $i_p$ [deg]	-	$87.3 \pm 2.7$
Stellar rotational axis inclination $i_s [\circ]$	-	$46 \pm 19$
Stellar rotational axis orientation $\Omega_{\rm s}$ [°]	-	$256 \pm 40$
Gravity darkening exponent $\beta$	-	$0.89 \pm 0.25$
$J_2$ for the star Contamination factor [07.]	- 2 + 1	$0.028 \pm 0.019$
	5 ± 1	J4 ± 4
Deduced transit parameters		
Stellar radius ratio $f = R_{s,pole}/R_{s,eq}$	1 (fixed)	$0.94 \pm 0.02$
$M_{\rm s}^{1/3}/R_{\rm s}$ [solar units] <sup>c</sup>	$0.58\pm0.02$	$1.09\pm0.02$
Stellar density $\rho_{\rm s}$ [ kg m <sup>-3</sup> ]	$270 \pm 6$	$1825 \pm 38$
Impact parameter <sup><math>b</math></sup> b	_	$0.43 \pm 0.44$
Orbital inclination $i_p$ [deg]	$88.1 \pm 0.8$	-
Spectroscopic parameters		
Effective temperature $T_{\rm eff}$ [K]	$5150\pm100$	$5260 \pm 100$
Stellar surface gravity $\log q [cgs]$	$3.6 \pm 0.2$	$4.3 \pm 0.2$
Metallicity [Fe/H] [dex]	$0.15 \pm 0.10$	$0.20 \pm 0.10$
Stellar rotational velocity $v \sin i  [\mathrm{km}\mathrm{s}^{-1}]$	$3.0 \pm 0.5$	$3.5 \pm 0.5$
Microturbulence velocity $V_{\rm mic}$ [ km s <sup>-1</sup> ]	$0.9 \pm 0.1$	$0.9 \pm 0.1$
Macroturbulence velocity $V_{\text{mac}}$ [ km s <sup>-1</sup> ]	$3.3 \pm 0.3$	$1.2 \pm 0.3$
Lithium equivalent width [mÅ]	31	no Li at 6708 Å
Spectral type	G8/9IV	K0 V
Stellar and planetary physical parameters from com	bined analysis	
Star mass $[M_{\odot}]^c$	$1.01 \pm 0.14$	$0.97 \pm 0.14$
Star radius $[R_{\odot}]^{c}$	$1.78 \pm 0.11$	$0.90 \pm 0.12$
Stellar surface gravity log $q$ [cgs]	$3.94 \pm 0.12$	$4.52 \pm 0.19$
Age of the star t [Gyr]	$12.0 \pm 1.5$	1 - 8
Distance of the system [pc]	$560 \pm 70$	$765 \pm 50$
Interstellar extinction $A_v$ [mag]	$0.75\pm0.20$	$0.85 \pm 0.15$
Orbital semi-major axis (Kepler's law) a [AU]	$0.0590 \pm 0.0027$	$0.0390 \pm 0.0020$
Orbital semi-major axis (light curve) a [AU]	$0.0603 \pm 0.0050$	$0.0386 \pm 0.0059$
Planet mass $M_{\rm p} \left[ M_{\rm Jup} \right]^d$	$0.484 \pm 0.087$	$0.85 \pm 0.20$
Planet radius $R_{\rm p} [R_{\rm Jup}]^a$	$0.955 \pm 0.066$	$0.90 \pm 0.16$
Planet density $\rho_p [g \text{ cm}^{-3}]$	$0.69 \pm 0.27$	$1.45 \pm 0.74$
Planet surface gravity log g [cgs]	$3.12 \pm 0.14$	$3.42 \pm 0.19$

**Notes.** <sup>(a)</sup>  $I(\mu)/I(1) = 1 - \mu + u_a\mu + u_b(1 - \mu)^2$ , where I(1) is the specific intensity at the centre of the disc and  $\mu = \cos \gamma$ ,  $\gamma$  being the angle between the surface normal and the line of sight;  $u_+ = u_a + u_b$  and  $u_- = u_a - u_b$ . <sup>(b)</sup>  $b = a \cos i \sqrt{1 - e^2}/R_s(1 + e \sin \omega)$ . <sup>(c)</sup> Radius and mass of Sun taken as 695 500 km and  $1.9891 \times 10^{30}$  kg, respectively (Lang 1999). <sup>(d)</sup> Radius and mass of Jupiter taken as 71 492 km and  $1.8992 \times 10^{27}$  kg, respectively (Lang 1999).

longitudes, the condition of the synchronous rotation could also be relaxed. Including more spots will improve the modelling results at the cost of increasing the number of free parameters. Although plausible, it is finally also an ad hoc solution for the problem. This hypothesis could be falsified, however, if observations of the Rossiter–McLaughlin effect would show a small spin-orbit angle.

#### 4.3.4. Planetary oblateness

A possible wind-driven oblated shaped of the planet can cause asymmetries in the light curve, but the observable amplitude is about 100 ppm (Barnes et al. 2009; Zhu et al. 2014), which is about 200 times smaller than the observed effect in our case, therefore we reject this explanation.

Other examples of star-planet interaction do not provide satisfactory answers in our case because they have typically different amplitudes and timescales (i.e. Jackson et al. 2012; Esteves et al. 2013; Faigler & Mazeh 2015).

#### 4.3.5. Other scenarios

A disc around the star could produce an asymmetric transit, but there are no signs of such disc in the light curve or in the infrared emission of the star. A moon around the planet could produce an asymmetric transit, but dynamically there is no room for a moon around a planet so close to its star. A second planet in the system transiting simultaneously could produce an asymmetric transit, but not every time that the transit is observed, and there are no signs of this planet in the radial velocity. We conclude that none of these scenarios provides a satisfactory explanation of the data.

# 5. Discussion

5.1. Stellar properties

#### CoRoT-28

CoRoT-28 is a G8/9IV evolved star with a radius of approximately 1.8 solar radii. With an age of approximately 12 Gyr, we expect from gyrochronology a rotational period around 70 or 80 days and a  $v \sin i$  around  $1.2 \text{ km s}^{-1}$  or smaller (Barnes 2007). The  $v \sin i$  value from spectroscopy is almost three times larger, giving an expected rotational period of about 30 days. The autocorrelation function (ACF) of the light curve (see McQuillan et al. 2013) does not show any evident periodicity at all, but if there is any sign, it is for periods larger than the 85 days observed by CoRoT (see Fig. 17).

There is an inconsistency between the  $v \sin i$  determined by spectroscopy, which is consistent with a relatively fast rotational period, and the stellar parameters derived from the models, which suggest an old star with a slow rotation rate. From our analysis of the light curve we cannot decide between the two scenarios. The  $v \sin i$  has a relatively large uncertainty, but seems to be consistent with the higher rotation rate. It is possible that the stellar models fail to reproduce the actual age of the star. The range proposed by the models is  $12.0 \pm 1.5$  Gyr, close to the old end of the distribution of stellar populations, which is consistent with the evolved stellar radius from the models  $(1.78 \pm 0.11 R_s \text{ for an effective temperature of } 5150 \pm 100 \text{ K})$ . This range, however, is perhaps not as consistent with the metallicity [Fe/H] =  $0.15 \pm 0.05$  dex, which is quite a robust observational result.

There is also an apparent inconsistency between the age and the Li I abundance in the atmosphere of the star. We estimated

![](_page_12_Figure_13.jpeg)

Fig. 17. Autocorrelation function of the light curve of CoRoT-28.

![](_page_12_Figure_15.jpeg)

Fig. 18. Autocorrelation function of the light curve of CoRoT-29.

 $\log N(\text{Li})$  using Table 2 of Soderblom et al. (1993) given the equivalent width of 31 mÅ. For a dwarf with an effective temperature of 5150 K, we obtained  $\log N(\text{Li}) = 1.4$ . This is in line with an age of a few hundred Myrs according to Sestito & Randich (2005). However, stars of this effective temperature with ages of few hundred Myrs have already reached the main sequence, which is not compatible with the surface gravity measured from spectroscopy or with the transit duration, which indicates that the star has a radius larger than the Sun. Moreover, we would expect a significant degree of stellar variability and a faster rotation period, which is also not supported by the observations. The abundance of lithium and its relationship with age, especially for stars hosting planets (see, for example, the recent discussions by Liu et al. 2014; Adamów et al. 2012), is still debated. Therefore we do not consider lithium as a reliable age indicator for CoRoT-28. On the other hand, it is known that a small amount of LiI can also be present in evolved stars, for example lithium can be regenerated by the Cameron-Fowler mechanism (Cameron & Fowler 1971).

We consider that observational evidence speaks in the case of CoRoT-28 in favour of an evolved star with a higher lithium content and  $v \sin i$  value than what would be expected for its age and evolutionary status.

# CoRoT-29

CoRoT-29 is a K0 main-sequence star with a radius of approximately 0.9 solar radii. Its age is not well constrained from the analysis of the stellar models and the autocorrelation function of

![](_page_13_Figure_1.jpeg)

**Fig. 19.** Shape of the stellar surface of CoRoT-29 in the gravity darkening model (thick line) compared with a spherically symmetric star (thin line).

the light curve (see Fig. 18) does not help to constrain the rotational period. In any case, the analysis of the ACF in the case of CoRoT-29 can be debated, as  $\sim$ 50% of the flux within the mask comes from a contaminant.

It is however interesting that the analysis of the light curve (Sect. 4.3) shows that the orbital plane of the planet could be misaligned with respect to the equatorial plane of the star. The gravity darkening model allows us to measure the relative inclination of the spin axis of the star, a parameter that typically cannot be constrained with photometric measurements.

The alignment between the vector normal to the planetary orbital plane and the stellar spin axis is considered one of the key observables constraining planetary formation and evolution (for a recent discussion, see Dawson 2014, and references therein). It has been proposed that the alignment, or misalignment, is related to the dynamical interaction between the star and the planet, which in turn depends on the internal distribution of matter inside the star. Cold, convective stars have different dissipation timescales than hot, radiative stars (see Albrecht et al. 2012). CoRoT-29 with a  $T_{\rm eff}$  of 5260 K and with a misalignment angle<sup>4</sup> of  $\Omega_s = 301 \pm 30^\circ$  would be right between the outliers of the distribution HAT-P-11 and HD 80606 in Fig. 20 of Albrecht et al. (2012). It is however worth mentioning that the tidal dissipation timescale of CoRoT-29b is 1000 times faster than for HAT-P-11, using Eq. (2) from the same paper. As mentioned, the dissipation timescale strongly depends on the internal structure of the star, which deserves further attention in the case of CoRoT-29

The shape of the transit light curve of CoRoT-29b has a strong contribution from the gravity darkening, orders of magnitude larger than in other examples found (i.e. Szabó et al. 2011; Zhou & Huang 2013). The contributions are only comparable in the case of the pre-main-sequence star PTFO 8-8695 (Barnes et al. 2013). However, the origin of the gravity darkening effect in PTFO 8-8695 is the fast rotation of the star, a M dwarf with a radius of  $1.4 R_{\odot}$ , a rotational period of 10 h, and a  $v \sin i$  of  $80 \text{ km s}^{-1}$ . For CoRoT-29b, the origin of the extreme pole to equatorial radius difference is not as easily understood (see Fig. 19). The spectroscopically measured  $v \sin i$  and the resulted stellar inclination (43°) yield  $v_{eq} = 5.1 \pm 1.8 \text{ km s}^{-1}$  and that corresponds to a stellar rotational period of 4–13 days.

To lowest order, and in the assumption of uniform rotation, the stellar shape is defined by the surface of constant total potential as defined in Eq. (2). It shows the balance between the contribution to the local gravitational potential of the stellar rotation  $\Omega_{\rm rot}$  and the quadrupole moment term dominated by  $J_2$ . Actually, we should have included in the balance the contribution from the tidal distortion caused by the planet, and account for the misalignment between the rotation axis of the star and the angular momentum of the orbit. But when comparing the tidal and rotational contributions to the distortion (see Eq. (3) of Ragozzine & Wolf 2009 or A.21 of Leconte et al. 2011), it turns out to be a couple orders of magnitude less important, and so we neglect it. Note also that in Eq. (2) the contribution from rotation is negligible compared to the contribution of the  $J_2$  term. This means that in our modelling the rotation rate is constrained mainly by the  $v \sin i$  value. The model can measure the deformation and the orientation of the star, but not its rotation rate. The results of Sect. 4.2 show that for CoRoT-29, the quadrupole moment has a contribution 2 orders of magnitude larger than rotation. Actually, the quadrupole moment of CoRoT-29 measured from the gravity darkening is far too large,  $J_2 = 0.028 \pm 0.019$ , compared to the Sun,  $J_2^{\odot} = (1.7 \pm 0.4) \times 10^{-7}$  (Lang 1999). Other authors have claimed large  $J_2$  values for fast-rotating stars, such as WASP-33 ( $J_2 = 3.8 \times 10^{-4}$ , Iorio 2011), but not as large as for CoRoT-29.

The value of the quadrupolar moment depends on the distribution of matter inside the star. When the star is in uniform rotation, this quadrupolar moment is closely related to the Love number<sup>5</sup>  $k_2$  in the linear approximation. Indeed, once  $k_2$ is known, the external potential and the shape that a body exhibits in response to any perturbing potential can be computed (see, for example, Leconte et al. 2011). The Love number is a measure for the level of central condensation of an object:  $k_2$  decreases as the degree of central condensation increases. A homogeneous incompressible ideal fluid body has  $k_2 = 3/2$ . For a star like CoRoT-29, the value of  $k_2$  can be estimated from canonical stellar models (see, for example, Claret & Gimenez 1995). Considering the *v* sin *i* value and the mass and orbital distance of the companion, the expected value of  $k_2$  for CoRoT-29 would produce a modest distortion, resulting in a  $J_2$  that would be 3 to 4 orders of magnitude smaller than our estimated value. In other words, the star is not rotating fast enough and the planetary companion is neither massive enough nor close enough to significantly distort the stellar shape. However, it is expected that the flattening may assume high values when the star is rotating differentially, with the angular velocity decreasing outwards (Jackson et al. 2004; Zahn et al. 2010). In turn, in the assumption of shellular rotation, a stellar rotation regime where the angular velocity is constant on level surfaces but varying in depth, (Zahn et al. 2010) has shown that  $J_2$  also increases compared to the case of uniform rotation. Assuming an internal differential rotation with a centre-to-surface ratio of 4 in angular velocity, the  $J_2$ of a 7  $M_{\odot}$  rapidly rotating star like Archenar can exceed 0.01, which is about twice the value it assumes under the hypothesis of uniform rotation. It is not straightforward to infer how such a result could be extrapolated to a much less massive star and with slow surface rotation such as CoRoT-29. The star seems to be distorted and it is apparently a robust result, observed from space and independently confirmed from ground. The gravity darkening model provides the most accurate and reasonable explanation, although a dedicated modelling out of the scope of this paper would be required.

<sup>&</sup>lt;sup>4</sup>  $\Omega_{\rm s}$  is the sky projected angle of the stellar spin axis,  $\lambda$  in the notation of Fabrycky & Winn (2009). In the notation of Albrecht et al. (2012), it would be  $\lambda = 180 - \Omega_{\rm s}$ .

<sup>&</sup>lt;sup>5</sup> Note that  $k_2$  is twice the apsidal motion constant, often indicated with the same symbol as in, e.g. Claret & Gimenez (1995).

![](_page_14_Figure_1.jpeg)

**Fig. 20.** Evolution of the period of rotation of the star in days. The red curve is the orbital period of the hypothetical falling planet. Initial semi-major axis as indicated. Initial eccentricity: e = 0.10. Initial rotation periods: 2, 5, and 12.8 days.

#### 5.2. Star-planet interaction

In the previous section, we have mentioned that the stars seem to rotate faster than expected for their evolutionary stage. In the case of CoRoT-29, for example, if magnetic braking is acting in this KOV star, and it is expected to be, the rotation should be slower. So, either the system is very young, or we have to find a mechanism to speed up the stellar rotation One way to speed up rotation is tidal interaction between the star and the planet. But the planets CoRoT-28b and CoRoT-29b may not be very efficient for that reason because of their orbital properties and, in the case of CoRoT-29b, for the high inclination of its orbit over the stellar equator (for a review of star-planet interaction in the CoRoT context, see Pätzold et al. 2012).

One hypothesis is that a second planet was present that accelerated the stellar rotation before falling into the star. Under this assumption, two planets formed simultaneously far away from the star (from the current position of the transiting planet). Planet-planet scattering could have moved then one planet in an inner orbit, very close to the star, and an outer planet in a larger, eccentric orbit. Tidal interactions would have made the inner planet fall into the star, accelerating its rotation rate and enriching its atmosphere with heavier elements such as lithium, while the outer planet would have subsequently circularized its orbit until the conditions that we see today.

To assess the viability of this kind of a scenario, we investigated the behaviour of such a hypothetical planet in the neighbourhood of the star. Although it is impossible to find observational evidence for this former planet, it is still useful to explore plausible mechanisms that can explain the current properties of CoRoT-29.

To reduce the number of free parameters, we assumed that the planet was a twin of CoRoT-29b in a low-eccentricity orbit. Figure 20 shows the evolution of the orbit of such a planet and the rotation of the star under the joint action of the magnetic braking of the star and the tides on the star caused by the planet. Regardless of the initial rotational rate of the star, all simulations show that the stellar rotation quickly increases to 15 to 20 days. At the same time, the semi-major axis of the planet is decreasing. At some point the tidal torque of the planet on the star becomes important and this accelerates the stellar rotation rate. By the time the planet has collided with the star, the rotational period has been reduced to a few days. After the collision, the stellar rotation rate brakes to its present value.

The models used in the evolution simulations are magnetic braking as determined by Bouvier et al. (1997) for stars with masses between 0.5 and 1.1  $M_{\odot}$  and a creep tide (Ferraz-Mello 2013) due to a relaxation factor  $\gamma = 10 \text{ s}^{-1}$ . This choice corresponds to the mid of the tidal dissipation range determined from the statistical study of stars hosting hot Jupiters by Hansen (2010) (3–25 s<sup>-1</sup>; see Ferraz-Mello 2013). The great remaining difficulty is to discover how the existing planet CoRoT-29b could exist in same time as its falling sibling. The proximity of both orbits is prone to creating great instability; maybe the high inclination of CoRoT-29b is a consequence of this instability.

#### 6. Summary

We have discovered and characterized two new planetary systems: CoRoT-28b and 29b.

CoRoT-28b belongs to the small population of hot-Jupiters orbiting evolved stars, which is interesting from the point of view of stellar and planetary evolution. It has a mass between that of Saturn and Jupiter and does not seem to be inflated (see the discussion in Enoch et al. 2012). There are a couple of open questions about the characterization of CoRoT-28, in particular regarding its rotation. We have measured a higher than expected v sin i and its lithium content is higher than expected for the star's evolutionary status. These open questions might reveal important information about the past of the system. For example, there is the question of whether there was a former planet that fell into the star and thus accelerated the stellar rotation and enriched its atmosphere with heavy elements. Unfortunately, we cannot confirm this hypothesis because of the lack of observational evidence. We used the method described in Parviainen et al. (2013) to search for planet occultations (secondary eclipses) in the light curves, but we did not find any significant signal. For CoRoT-28b we obtain a maximum star-planet flux ratio of 9.5% (99th percentile of the marginal posterior). This upper limit is not useful for constraining the planet's albedo or brightness temperature in any useful way, since the highest physically feasible value for fis ~2%.

CoRoT-29b is a very interesting system. The strong asymmetry of the transit light curve is only comparable to transits of planets orbiting very young, fast rotating stars, but the star is neither young nor rotating fast. The extreme value of the deformation, compared to stars of its mass range, is not understood and deserves more attention. We have not found at this point a satisfactory answer for the origin of the asymmetry in the transit shape, but we encourage the study of these system with other instruments (CHEOPS, Broeg et al. 2013; PLATO 2.0, Rauer et al. 2014, ground-based surveys) to confirm or disprove CoRoT observations and solve the puzzle.

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# Appendix A: Radial velocity data

**Table A.1.** CoRoT-28 SOPHIE radial velocities, their errors, and bisector spans.

BJD	RV	Error	Bis
	$[km s^{-1}]$	$[\text{km s}^{-1}]$	$[km s^{-1}]$
2 455 801.34001	-76.751	0.023	-0.055
2 455 804.41446	-76.849	0.013	-0.051
2 455 810.35554	-76.782	0.021	0.012
2 455 811.32492	-76.753	0.013	-0.019
2 455 832.30855	-76.723	0.014	-0.016
2 456 063.56528	-76.771	0.029	0.054
2 456 064.54259	-76.820	0.015	-0.086
2456071.54853	-76.714	0.017	-0.049
2456072.57780	-76.718	0.010	-0.035
2 456 100.49337	-76.782	0.012	-0.128
2 456 103.48011	-76.716	0.010	0.006
2 456 121.38285	-76.810	0.024	-0.142
2 456 123.47526	-76.671	0.018	-0.048
2 456 124.46350	-76.593	0.019	0.016
2 456 125.42640	-76.671	0.013	-0.056
2 456 132.46267	-76.844	0.018	0.010
2456133.40017	-76.778	0.011	-0.000
2 456 134.43837	-76.720	0.012	0.023
2 456 135.41925	-76.709	0.018	-0.005
2 456 149.44334	-76.731	0.017	-0.037
2 456 152.42582	-76.797	0.016	-0.083
2 456 153.41986	-76.796	0.010	-0.089
2 456 154.34156	-76.750	0.022	-0.037
2 456 156.34663	-76.732	0.016	-0.058
2456157.37367	-76.765	0.013	-0.031

**Table A.2.** CoRoT-28 HARPS radial velocities, their errors, and bisector spans.

BJD	RV	Error	Bis
	$[km s^{-1}]$	$[km s^{-1}]$	$[km s^{-1}]$
2 456 116.75525	-76.7574	0.0070	-0.018
2 456 118.75516	-76.6534	0.0076	0.013
2 456 152.54246	-76.775	0.013	-0.034
2 456 158.59125	-76.7564	0.0085	-0.008
2 456 159.50759	-76.7094	0.0088	-0.005
2 456 161.49239	-76.6614	0.0083	-0.057
2 456 514.54510	-76.6742	0.0085	-0.028

 Table A.3. CoRoT-28 FIES radial velocities, their errors, and bisector spans.

BJD	RV	Error	Bis
	$[\text{km s}^{-1}]$	$[\rm km  s^{-1}]$	$[\rm km  s^{-1}]$
2 456 103.51866	-76.800	0.018	0.004
2 456 104.55555	-76.862	0.022	0.001
2 456 105.56260	-76.914	0.017	-0.033
2 456 107.54147	-76.844	0.020	-0.032
2 456 117.47300	-76.893	0.011	-0.008
2 456 118.42105	-76.810	0.017	-0.012
2 456 119.50754	-76.831	0.015	-0.009
2 456 120.55636	-76.888	0.015	-0.034
2 456 121.42907	-76.897	0.021	-0.015
2 456 122.40610	-76.876	0.021	-0.020

 Table A.4. CoRoT-29 HARPS radial velocities, their errors, and bisector spans.

BJD	RV	Error	Bis
	$[\text{ km s}^{-1}]$	[ km s <sup>-1</sup> ]	$[\text{ km s}^{-1}]$
2 456 097.73381	-64.131	0.052	-0.014
2 456 098.70664	-64.371	0.046	0.022
2 456 099.63447	-64.199	0.103	0.030
2 456 101.81698	-64.303	0.035	-0.064
2 456 102.80688	-64.097	0.056	-0.177
2 456 115.66034	-64.302	0.077	0.105
2 456 116.71144	-64.186	0.026	-0.076
2 456 117.67788	-64.083	0.021	-0.041
2 456 119.61671	-64.151	0.051	-0.091
2 456 149.61905	-64.255	0.080	-0.130
2 456 150.63533	-64.213	0.037	-0.095
2 456 151.63052	-64.105	0.045	0.059
2 456 154.57617	-64.053	0.038	-0.082
2 456 159.55259	-64.096	0.056	0.008
2 456 161.53567	-64.274	0.037	-0.087
2 456 455.87546	-64.189	0.102	-0.230
2 456 460.77835	-64.325	0.099	-0.130
2 456 508.68337	-64.239	0.041	0.017
2 456 511.54785	-64.228	0.031	-0.130
2 456 514.68026	-64.315	0.048	-0.145

Appendix B: Flow chart for gravity darkening modelling

![](_page_18_Figure_2.jpeg)

Fig. B.1. Flow chart for the gravity darkening modelling process of CoRoT-29b.