

Block Interleaved Frequency Division Multiple Access for Power Efficiency, Robustness, Flexibility and Scalability

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Abstract—The multiple access solution in an IMT-Advanced mobile radio system has to meet challenging requirements such as high throughput, low delays, high flexibility, good robustness, low computational complexity and a high power efficiency, especially in the uplink. In this paper a novel multiple access scheme for uplinks denoted as B-IFDMA is presented. We show that this scheme is able to provide equal or better error rate performance than the Single-Carrier Frequency Division Multiple Access (SC-FDMA) schemes IFDMA and LFDMA, when considering realistic channel estimation performance at the receiver and no reliable channel state information at the transmitter. We also show that B-IFDMA provides better amplifier efficiency than OFDMA and can provide better end-to-end energy efficiency than IFDMA and LFDMA. Moreover, the scheme shows a promisingly high robustness to frequency-offsets and Doppler spread. Thus, this scheme can be regarded as a promising solution for the uplink of future mobile radio systems.

I. INTRODUCTION

Future mobile communication systems need to efficiently support fully packet-based services with largely different requirements on data rates, ranging from a few kbps to hundreds of Mbps, and largely varying Quality of Service (QoS) requirements. The systems need to flexibly support deployment in various propagation scenarios ranging from isolated hot spots to wide area cellular, including support for high speed trains. In addition, they need to support deployment in various spectrum allocation scenarios with system bandwidths up to 100 MHz at a carrier frequency of several GHz, cf. [1]–[5]. These system requirements imply that the multiple access solution in an IMT-Advanced mobile radio system has many challenges to meet.

It has been shown feasible to implement a fully synchronous network, [6], [7]. Thus, resources can be allocated based on a chunk concept, where a chunk is a time-frequency resource unit. With multiple antennas, spatial reuse of chunks is enabled and denoted as chunk layers [2], [4], [5], [8], [9]. The chunk concept is adopted in 3GPP Long Term Evolution (LTE), where a chunk is denoted as Resource Block. The chunk size is chosen in such a way that it experiences essentially flat fading in its time-frequency extent, also in largely frequency selective channels and for users at vehicular speeds.

With channel quality information (CQI) available at the transmitter it is possible to adapt to the small-scale fading of the chunk resources, so-called frequency-adaptive (FA) transmission [9]. Adaptive Orthogonal Frequency Division Multiple

Access (OFDMA) with a chunk based Time Division Multiple Access (TDMA) component is such an FA multiple access scheme [9]. Adaptive TDMA/OFDMA can provide a large increase in the system capacity, also in presence of channel prediction errors due to gains in multi-user scheduling and chunk-wise link adaptation [10], [11]. This is very important for high cell load situations. FA transmission is best suited for scenarios with favorable channel conditions such as high Signal to Interference and Noise Ratios (SINR), and reasonably low speeds [10]. FA is especially suited for transmission of rather large data volumes and high instantaneous data rates for low service latency. However, the FA scheme must be accompanied by a robust diversity based transmission mode, since FA transmission without reliable CQI can deteriorate.

The diversity-based scheme, here denoted as non-frequency-adaptive (NFA) transmission, should efficiently support users in all other usage scenarios, such as low SINR, high user equipment (UE) velocities, small and delay critical packet transfers, broadcasting that cannot benefit from a retransmission scheme, as well as for multicast transmission to multiple users with widely varying channels. In these scenarios a diversity based scheme has the potential to be more robust, more spectrally efficient and also more energy efficient.

Various relaying concepts are also considered in future wireless systems, [2]–[5]. However, multi-hop relaying increases the end-to-end delay in the Radio Access Network (RAN). Thus, an important requirement of the multiple access solution is to support a very low delay. This requirement also enables FA transmission at vehicular speeds even with a several GHz carrier frequency. It furthermore enables the use of retransmissions also for delay constrained services such as voice. However, such a low delay requirement implies a very short frame duration with very limited time diversity. Thus, the diversity for the NFA transmission scheme must come from the frequency domain and/or the spatial domain.

Below we summarize important requirements that we have identified for the NFA multiple access scheme.

- *Robustness to small-scale fading without time diversity*
- *Tuneable degree of frequency-diversity*
- *Need to support high energy efficiency in the transmitters and the receivers*
- *Robustness to carrier frequency offsets and large Doppler spread*

- Support for widely varying packet sizes
- Enable efficient resource allocation
- Be of use for in-band control signals
- Enable efficient co-existence with adaptive TDMA/OFDMA
- Facilitate low complexity transmitter in UE

To define a scheme that optimally fulfills all of these requirements at the same time is challenging, and a trade-off is needed. In addition, the trade-off would look different in different deployment and usage scenarios. Thus a flexible scheme is desirable that can be adjusted towards a good trade-off in each scenario.

In this paper, we present a novel multiple access scheme denoted as Block-Interleaved Frequency Division Multiple Access (B-IFDMA), which is intended to fulfill the above requirements and also to provide a good trade-off between them for NFA transmission in uplinks. We have briefly introduced the scheme in [12]. B-IFDMA is based on OFDMA. In B-IFDMA equidistantly frequency-separated blocks, each consisting of a few subcarriers, are allocated to each user. A Discrete Fourier Transform (DFT) precoding step is performed on each Orthogonal Frequency-Division Multiplexing (OFDM) symbol before transmission. In addition, a short TDMA component is introduced within the chunks. B-IFDMA is a generalization of DFT precoded OFDMA with interleaved subcarrier allocation, as described in [13], also denoted as Interleaved Frequency Division Multiple Access (IFDMA) in the original paper [14]¹ or Single-Carrier Frequency Division Multiple Access (SC-FDMA) with distributed mapping [15], [16]. B-IFDMA is also a generalization of Localized Frequency Division Multiple Access (LFDMA) [17], also denoted as Localized DFTS-OFDM or SC-FDMA with localized mapping, [15], [16]. In this paper we use the acronym IFDMA for SC-FDMA with distributed mapping and LFDMA for SC-FDMA with localized mapping. In contrast to IFDMA, B-IFDMA can assign adjacent subcarriers in the blocks, and in contrast to LFDMA multiple non-contiguous subcarriers can be assigned, see illustration in Fig. 1.

The IFDMA scheme has been considered in the uplink of the LTE standard, but LFDMA was adopted [15], [16] in LTE Release 8. In LTE, with rather flat fading Resource Blocks (RBs), link adaptation and multiuser diversity gains can be obtained whenever reliable CQI is available. Some frequency-diversity collected over multiple slots can be obtained when needed through frequency-hopping, but at the cost of higher delay and delay jitter. To maintain a low RAN delay in a multi-hop relaying scenario, frequency hopping is less attractive.

Our evaluations in this paper of the B-IFDMA scheme towards the identified requirements for NFA transmission are focused on the *error rate performance*, *energy efficiency* and *robustness* of the scheme compared to OFDMA, IFDMA and LFDMA. We investigate the properties of the scheme under close to real conditions such as realistic pulse shaping and realistic power amplifiers, correlated Multiple Input Multiple Output (MIMO) mobile radio channels, realistic channel estimation

¹Some authors distinguish between DFT precoded OFDMA and the original IFDMA scheme as the frequency domain generation and the time domain generation approaches, and regard them as different schemes with different performance by assuming that spectrum shaping is made in the corresponding domain. Here we regard the two schemes as equivalent.

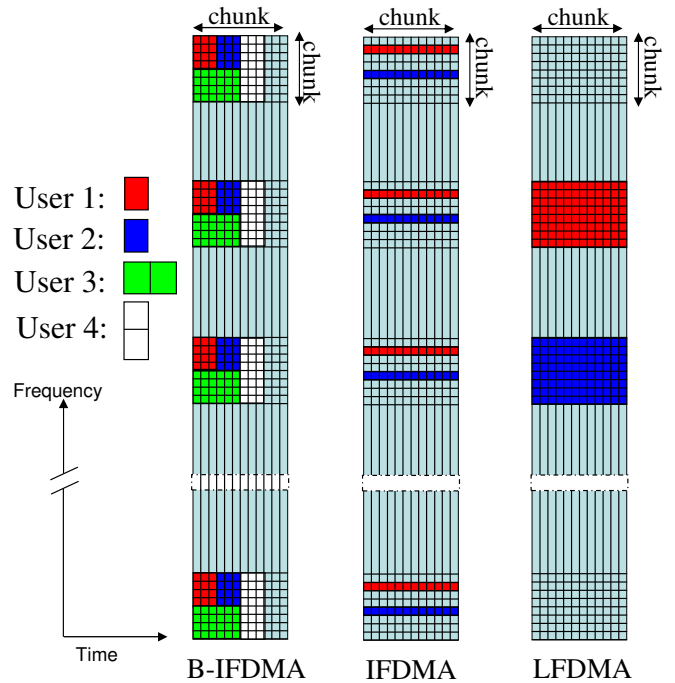


Fig. 1. Illustration of B-IFDMA using $M = 4$ subcarriers and $N_t = 3$ OFDM symbols per subcarrier block within a time-frequency resource denoted as chunk. SC-FDMA with localized mapping (LFDMA) and SC-FDMA with distributed mapping (IFDMA) are shown for comparison. In B-IFDMA, high rate users are allocated more blocks within the chunks in either the time or the frequency direction. (A similar illustration is included in [12].)

performance under constraints set by a low pilot overhead loss and a realistic frame structure. Such a system is hard to analyze theoretically, but for application in IMT Advanced systems such a property analysis is of interest. Thus, the performance investigations in this paper are performed with simulations.

The investigations show that in an IMT-Advanced scenario, B-IFDMA provides equal or better error rate performance than the Single-Carrier Frequency Division Multiple Access (SC-FDMA) schemes IFDMA and LFDMA, when considering realistic channel estimation performance at the receiver and no reliable channel state information at the transmitter. We also show that B-IFDMA provides better amplifier efficiency than OFDMA and can provide better end-to-end energy efficiency than IFDMA and LFDMA. Moreover, the scheme shows a promisingly high robustness to frequency-offsets (CFOs) and Doppler spread (DS). Thus, this scheme can be regarded as a promising solution for the uplink of future mobile radio systems.

This paper is organized as follows: We start in Section II

²The B-IFDMA scheme has been adopted for the NFA uplink in the WINNER system concept [2], [4], [5]. A scheme similar to B-IFDMA denoted as Block Equidistant Frequency Division Multiple Access (B-EFDMA) has also been proposed for NFA downlinks [4], [5], [18]. The difference to B-IFDMA is that the DFT precoding step is not included, since the benefit of DFT precoding is lost in the multiple signal multiplexing in the downlink. The other benefits are similar as for B-IFDMA, including the possibility to time localize the transmission in the base station (BS) in low load situations, in order to save energy in both the BS and the UE. The B-EFDMA scheme has been adopted for the WINNER NFA downlink.

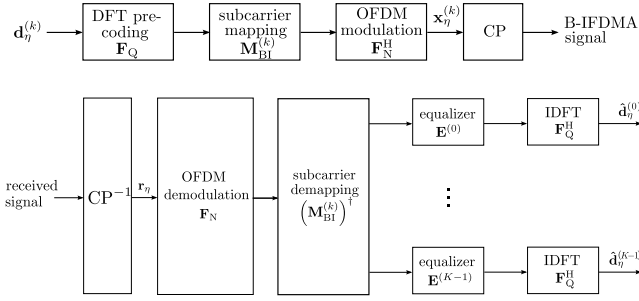


Fig. 2. B-IFDMA transceiver, transmitter (top) and receiver (bottom). In case the same amount of resources are allocated per user, for each user k out of K uplink user terminals, Q out of N subcarriers are allocated by the subcarrier mapping matrix $\mathbf{M}_{\text{BI}}^{(k)}$. The allocated subcarriers consist of L blocks, each containing M adjacent subcarriers.

with a detailed definition of B-IFDMA. Then, in Section III we investigate the error rate performance of B-IFDMA with perfect and non-perfect channel estimation at the receiver. These investigations show the capability of B-IFDMA to collect large diversity gains under realistic assumptions on channel estimation performance, also for rather low data rates, without using time-diversity. We proceed in Section IV with the energy efficiency of B-IFDMA w.r.t. to High Power Amplifier (HPA) performance and end-to-end energy efficiency. These investigations motivate the use of a DFT precoding step, and the integration of the TDMA component within the B-IFDMA scheme. These results also motivate the regular subcarrier allocation in B-IFDMA. In Section V we investigate the robustness of B-IFDMA to carrier frequency offsets and to Doppler spreads. These results show that B-IFDMA offers the possibility to combine robustness and provision of frequency diversity. In Section VI we summarize our investigation results, and we comment on the suitability of B-IFDMA to meet our identified list of requirements above on the NFA uplink scheme. In Section VII we conclude the paper.

II. SYSTEM MODEL

As an introduction to B-IFDMA, the resource allocation for B-IFDMA is illustrated in Fig. 1 along with IFDMA and LFDMA for comparison, assuming the Frequency Division Duplex (FDD) chunk size in [19]. The scheme is defined in detail in the subsequent sections.

A. Signal Definition

In this section, a transmitter signal model for B-IFDMA is given, following the block diagram in Fig. 2. In the following, all signals are represented by their discrete time equivalents in the complex baseband. Upper case bold letters denote matrices and lower case bold letters denote column vectors. Further on, $(\cdot)^\dagger$ denotes the pseudo-inverse and $(\cdot)^H$ the Hermitian of a matrix and $(\cdot)^T$ the transpose of a vector or a matrix, respectively. Finally, $[\cdot]_{l,m}$ denotes the element of a matrix in the l -th row and m -th column.

An uplink transmission system with K users with user index k , $k = 0, \dots, K-1$ is considered. Let $c_\nu^{(k)}$, $\nu \in \mathbb{Z}$, denote a sequence of data symbols of user k at symbol rate $1/T_s$ taken from the alphabet of an arbitrary bit mapping scheme applied after channel encoding and bit interleaving.

At first, the data symbols $c_\nu^{(k)}$ are grouped into data symbol vectors

$$\mathbf{d}_\eta^{(k)} = [d_{\eta,0}^{(k)}, \dots, d_{\eta,Q-1}^{(k)}]^T \quad (1)$$

with Q elements $d_{\eta,q}^{(k)} = c_{\eta \cdot Q + q}^{(k)}$, $q = 0, \dots, Q-1$, $\eta \in \mathbb{Z}$. For sake of simplicity, throughout this section it is assumed that the number Q is the same for all users. However, note that for B-IFDMA also different numbers Q can be assigned to the users, cf. [20]. Each data symbol vector $\mathbf{d}_\eta^{(k)}$ is pre-coded by a DFT represented by a $Q \times Q$ matrix \mathbf{F}_Q with elements

$$[\mathbf{F}_Q]_{p,q} = \frac{1}{\sqrt{Q}} \cdot e^{-j\frac{2\pi}{Q}pq}, \quad p, q = 0, \dots, Q-1. \quad (2)$$

After DFT pre-coding, the Q elements of the vector $\mathbf{F}_Q \cdot \mathbf{d}_\eta^{(k)}$ are mapped to a set of Q out of $N = K \cdot Q$ subcarriers available in the system. The mapping is performed in a block-interleaved manner. Let M denote the number of subcarriers in each subcarrier block, L denote the numbers of subcarrier blocks and let $Q = M \cdot L$. The block-interleaved mapping can be described by an $N \times Q$ matrix $\mathbf{M}_{\text{BI}}^{(k)}$ with elements

$$[\mathbf{M}_{\text{BI}}^{(k)}]_{n,q} = \begin{cases} 1 & n = l \cdot \frac{N}{L} + m + kM \\ 0 & \text{else} \end{cases}, \quad (3)$$

where $l = 0, \dots, L-1$, $m = 0, \dots, M-1$, and $q = m + l \cdot M$. After subcarrier mapping, OFDM modulation is applied. The OFDM modulation is performed by an N -point Inverse DFT (IDFT) represented by matrix \mathbf{F}_N^H with elements

$$[\mathbf{F}_N^H]_{n,\mu} = \frac{1}{\sqrt{N}} \cdot e^{j\frac{2\pi}{N}n\mu}, \quad n, \mu = 0, \dots, N-1. \quad (4)$$

The η -th B-IFDMA-modulated data vector

$$\mathbf{x}_\eta^{(k)} = [x_{\eta,0}^{(k)}, \dots, x_{\eta,N-1}^{(k)}]^T \quad (5)$$

of user k with elements $x_{\eta,n}^{(k)}$, $n = 0, \dots, N-1$, at sampling rate N/T_s is, thus, given by

$$\mathbf{x}_\eta^{(k)} = \mathbf{F}_N^H \cdot \mathbf{M}_{\text{BI}}^{(k)} \cdot \mathbf{F}_Q \cdot \mathbf{d}_\eta^{(k)}. \quad (6)$$

From (6), it follows that B-IFDMA can be considered as OFDMA with block-interleaved subcarrier allocation and DFT pre-coding of the data symbols before OFDMA modulation. For the special case $M = 1$, i.e. for one subcarrier per block in the allocated OFDM symbols, B-IFDMA is equivalent to IFDMA [14], [21]. For the special case $L = 1$, i.e. for one block of subcarriers, B-IFDMA is equivalent to LFDMA [17]. Thus, B-IFDMA can be understood as a generalization of these schemes. In the Appendix we show that a B-IFDMA signal can be efficiently generated in the time domain, i.e. without the DFT operation.

B. Receiver Structure

In the following a B-IFDMA receiver is described for an uplink scenario, following the block diagram in Fig. 2. Let

$$\mathbf{h}_\eta^{(k)} = (h_{\eta,0}^{(k)}, \dots, h_{\eta,L_p-1}^{(k)}, 0, \dots, 0)^T \quad (7)$$

denote the $N \times 1$ vector representation of a multi-path channel of user k . Let further $h_{\eta,l}^{(k)}$, $l = 0, \dots, L_p-1$, denote the L_p non-zero channel coefficients at sampling rate N/T_s with $L_p \leq N$.

Before transmission over the channel $\mathbf{h}_\eta^{(k)}$, a Cyclic Prefix (CP) is inserted in between consecutive modulated data vectors $\mathbf{x}_\eta^{(k)}$. At the receiver, the CP is removed before demodulation. For the time interval T required for transmission of vector $\mathbf{x}_\eta^{(k)}$ and the CP, the channel is assumed to be time invariant. Moreover, perfect time and frequency synchronization is assumed. Thus, with $\mathbf{H}^{(k)}$ denoting the circulant channel matrix with vector $\mathbf{h}_\eta^{(k)}$ in its first column [22], the η -th received signal vector \mathbf{r}_η after removal of the CP is given by

$$\mathbf{r}_\eta = \sum_{k=0}^{K-1} \mathbf{H}_\eta^{(k)} \cdot \mathbf{x}_\eta^{(k)} + \mathbf{n}_\eta, \quad (8)$$

where

$$\mathbf{n}_\eta = (n_{\eta,0}, \dots, n_{\eta,N-1})^T \quad (9)$$

denotes an Additional White Gaussian Noise (AWGN) vector with samples $n_{\eta,n}$, $n = 0, \dots, N-1$ at sampling rate N/T_s .

At the receiver, after removal of the CP, an N -point DFT is applied to the received signal \mathbf{r}_η . Subsequently, the signal is user specifically demapped. After demapping, for each user k the impact of the channel is compensated by an equalizer and the DFT pre-coding is compensated by a Q -point IDFT. In the following, a Frequency Domain Equalizer (FDE) [23], [24] represented by a $Q \times Q$ diagonal matrix $\mathbf{E}^{(k)}$ is considered. Thus, at the receiver, estimates $\hat{\mathbf{d}}_\eta^{(k)}$ of the data symbol vectors $\mathbf{d}_\eta^{(k)}$ for user k are given by

$$\hat{\mathbf{d}}_\eta^{(k)} = \mathbf{F}_Q^H \cdot \mathbf{E}^{(k)} \cdot \left(\mathbf{M}_{\text{BI}}^{(k)} \right)^\dagger \cdot \mathbf{F}_N \cdot \mathbf{r}_\eta. \quad (10)$$

III. ERROR RATE PERFORMANCE

In this section we investigate the error rate performance of B-IFDMA with various block sizes. The aim of these investigations is to show the capability of B-IFDMA to collect large diversity gains under realistic assumptions on channel estimation performance, also for rather low data rates, without using time-diversity. We start in Section III-A by investigating the diversity gains under the assumption of perfect channel estimation at the receiver. Then, in Section III-B we quantify the channel estimation performance for various B-IFDMA block sizes. With these performance results at hand, we proceed in Section III-C by discussing the trade-off between these performance measures for different B-IFDMA block sizes, and we illustrate with quantitative examples.

A. Diversity Gains

As discussed in Section I robustness to small-scale fading based on frequency diversity and/or spatial diversity is needed to satisfy delay critical services, especially in bad channel conditions. Time diversity based schemes are less attractive in order to keep a short delay over the air interface. In this section, we investigate the uplink performance of B-IFDMA with Quadrature Phase Shift Keying (QPSK) modulated and Forward Error Correction (FEC) encoded transmission over a frequency-selective fading wide area mobile radio channel. We show results for single antenna transmission (SISO), two transmit antennas at the UE using Alamouti Space-Frequency Coding [25], [26] with one receive antenna (MISO, Alamouti) and for two transmit antennas at the UE using Alamouti Space-Frequency Coding with two receive antennas at the base station

(BS) applying Maximum Ratio Combining (MIMO, Alamouti and MRC). Each OFDM symbol is formed as described in Section II and a joint FEC encoding and interleaving is performed over the used OFDM symbols in the chunk. All simulation assumptions are listed in Table I.

The coherence time T_c and the coherence bandwidth B_c of the mobile radio channel play an important role. In the literature various different definitions for coherence time and coherence bandwidth are used, but in Table I they are calculated as follows. Let c_0 , f_0 and v denote the speed of light, the carrier frequency and the velocity of a mobile station, respectively. Let further $f_{\text{D,max}} = f_0 \cdot \frac{v}{c_0}$ denote the maximum Doppler frequency for this mobile station. The coherence time T_c can be defined as

$$T_c = \frac{1}{2 \cdot f_{\text{D,max}}} = \frac{1}{B_D}, \quad (11)$$

where $B_D = 2 \cdot f_{\text{D,max}}$ is the well-known Doppler bandwidth.

The coherence bandwidth B_c can be defined as

$$B_c = \frac{1}{\Delta\tau}, \quad (12)$$

where $\Delta\tau$ denotes the time difference between the first and the last received propagation path of the mobile radio channel, usually denoted as the delay spread of the channel.

The Bit Error Rate (BER) performance of B-IFDMA for different numbers M of subcarriers per block is given in Figs. 3, 4 and 5. Perfect channel estimation is assumed and the pilot symbol overhead required for channel estimation is not considered. In these figures the 3 dB antenna gain in the 2 times 2 MIMO cases is removed to simplify the comparison of the diversity gains in the different scenarios.

When the distance of the subcarrier blocks is large compared to the coherence bandwidth, they receive almost independent fading, and thus the frequency diversity is improved. For large numbers Q of subcarriers per user, the distance between the subcarrier blocks is reduced and, thus, the frequency diversity gains are decreased. Regarding the simulation results for MISO and MIMO transmission it can be concluded that even for B-IFDMA exploiting spatial diversity, the differences in frequency diversity are still considerable.

From Figs. 3, 4 and 5 it can also be concluded that for a given data rate, i.e. for a given number Q of subcarriers assigned to a user, the performance of B-IFDMA increases with decreasing number M of subcarriers per block. The reason for that is that for a given number Q with decreasing number M , the number of subcarrier blocks L increases. However, as discussed in Section IV-B and illustrated in Fig. 1, for a given average data rate per frame the number of blocks can be maintained by introducing a TDMA component with increased number of used subcarriers and a correspondingly smaller duty cycle within the chunk. In Fig. 6 we can see that the diversity gain depends mainly on the number of blocks L . Hence the same robustness towards small-scale fading can be maintained also with time-localized transmission to take advantage of the gain in transceiver power efficiency as discussed later in Section IV-B.

B. Channel Estimation

In Section III-A we showed the simulated diversity gains for B-IFDMA with various parameterizations under the assumption

TABLE I
SIMULATION PARAMETERS.

Bandwidth	40 MHz
Total number of subcarriers	1024
Carrier frequency	3.7 GHz
Sampling rate	1/(25 ns)
Guard Interval	3.2 μ s
Modulation	QPSK
Code	Convolutional code, rate 1/2
Code polynomials	133,171
Constraint length	6
Decoder	BCJR [27]
Interleaving	random over 12 OFDM symbols
Channel	WINNER C2 Urban Macro-cell [28]
Scenario	Wide Area
Antenna distance	Tx: $\lambda/2$, Rx: 2λ
User velocity	50 km/h
Coherence bandwidth	550 kHz
Coherence time	2.9 ms
Channel estimation	perfect

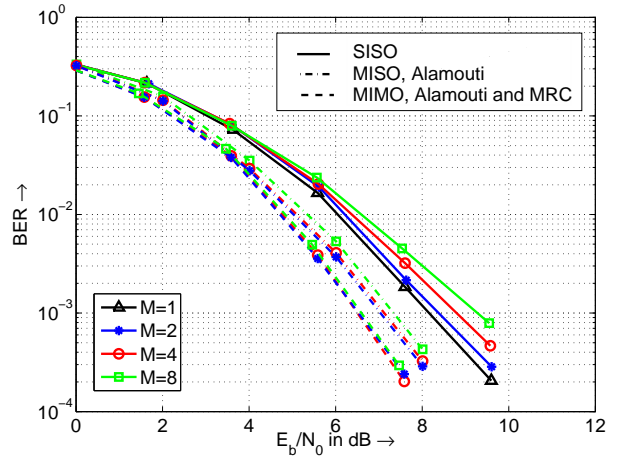


Fig. 5. Coded performance for B-IFDMA with instantaneous data rate 4.44 Mbps, i.e. $Q=128$ subcarriers per user with normalized antenna gain.

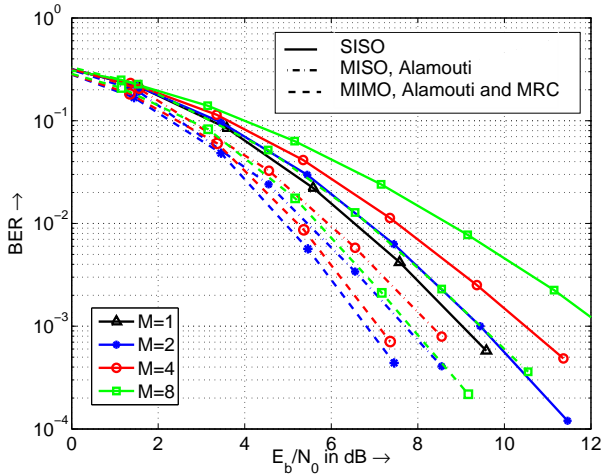


Fig. 3. Coded performance for B-IFDMA with instantaneous data rate 1.11 Mbps, i.e. $Q=32$ subcarriers per user with normalized antenna gain.

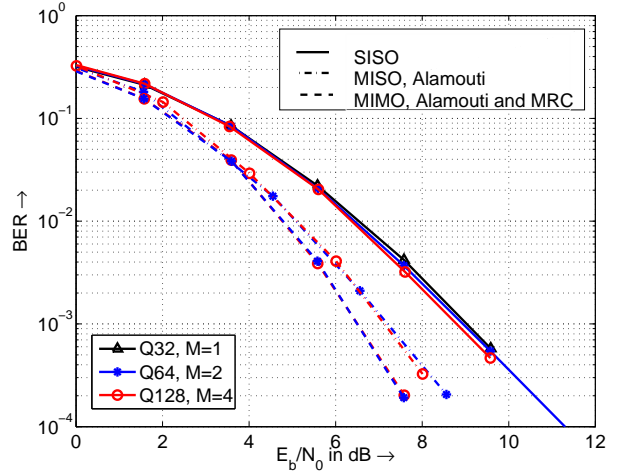


Fig. 6. Coded performance for B-IFDMA with the same number of $L = 32$ blocks per user and with normalized antenna gain.

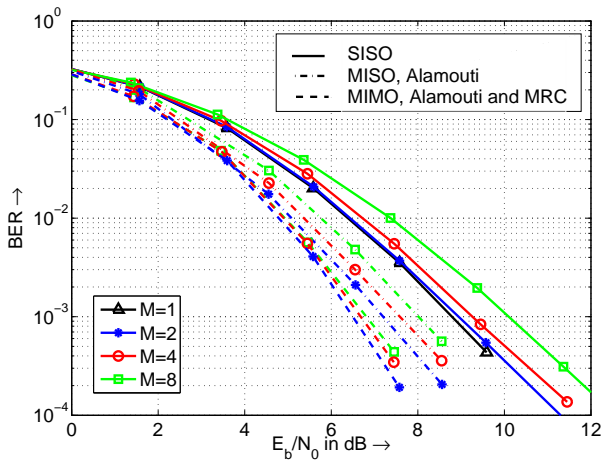


Fig. 4. Coded performance for B-IFDMA with instantaneous data rate 2.22 Mbps, i.e. $Q=64$ subcarriers per user with normalized antenna gain.

of perfect channel estimation. However, in general the less correlation among the subcarriers the better diversity but also the less correlation to be used in the channel estimation scheme over the subcarrier blocks. In addition, with pilot-aided channel estimation it is important to keep the pilot overhead low. Thus, with a given pilot overhead, there is an inherent trade-off to be made between attainable diversity gains and loss due to non-ideal channel estimation performance. In this section, we first define in Section III-B.1 what we mean with pilot overhead, and then in Section III-B.2 we show the attainable performance of memory-based and memory-less pilot-aided channel estimation schemes for various B-IFDMA block sizes.

1) *Pilot Overhead*: In pilot-aided channel estimation [29]–[31], the complex gain of the OFDM subcarriers is estimated at the receiver based on known time-frequency pilot symbols (also denoted as reference symbols) placed within each block. The channel equalization and payload data detection/decoding is then based on inferred complex channel gains at the payload

symbol locations.

With pilot aided channel estimation, there is a pilot overhead loss in both signal-to-noise ratio (SNR) degradation due to the energy put on the pilots and in spectral efficiency due to the channel symbols occupied by the pilot symbols. Below we assume that the pilot symbols are inserted as subcarrier channel symbols with the same energy as the data carrying channel symbols (i.e. no pilot boosting). In this case the SNR loss and the spectral efficiency loss are the same. Assuming that there are P pilots per block and the block size equals M subcarriers times N_t OFDM symbols, the pilot overhead loss becomes $P/(M \cdot N_t)$ and the SNR degradation $\log_{10}(M \cdot N_t / (M \cdot N_t - P))$ dB.

Below in Section III-B.2 we discuss the suitable pilot schemes and corresponding channel estimation performance under the assumption of a constant pilot overhead loss of 1/12 for the different block sizes, i.e. 8.3% loss in spectral efficiency and 0.38 dB in SNR degradation.

2) *Block Size Effect on Channel Estimation:* Because of the variation of the complex gain with frequency (due to the multipath propagation) and with time (due to mobility), the channel at payload positions will in general differ from that at the pilot positions. The coherence time and coherence bandwidth as defined in (11) and (12) respectively give an estimate of the order of the needed sampling interval in time and frequency for the mobile radio channel according to the sampling theorem [32]. However, the channel has to be estimated based on received noisy pilot symbols, and in a packet oriented system the channel resources needed per packet transmission are not very large. Hence, due to the limited number of noisy pilots available for channel estimation, an oversampling factor is typically needed, i.e. a more dense pilot pattern means better estimation performance.

For the considered diversity-based transmission schemes, a problem is then encountered in uplinks: Large blocks will have many embedded pilots and thus good possibilities for interpolation, which is more robust than extrapolation. But if the pilot overhead is to be held fixed, small blocks will contain only one or a few pilot symbols. This effect may partly or completely cancel the effect of frequency diversity.

Good channel estimation performance is achieved by mainly three different strategies:

- *Use pilots from adjacent blocks, to enable interpolation over frequency.* This strategy is possible and recommended in downlinks, but it cannot be used in uplinks, where adjacent blocks are either unused or used by other UEs. Blocks used by the UE itself are in general placed significant distances apart in frequency, with low inter-block channel correlation. They are therefore of limited use for channel estimation.
- *Use pilots from previous blocks.* This can be done in general in downlinks. In uplinks, it becomes possible only if the UE uses the same blocks over multiple frames (persistent scheduling). In the investigation below, we illustrate the potential maximum estimation performance obtainable by using optimal Kalman smoothing that uses an unlimited amount of past payload symbols.
- *Use also data symbols for channel estimation,* by iterative channel estimation. The pilot based channel estimate is then used as a first step. Decoded soft bits are then used in a second step to improve the channel estimates. Iterative

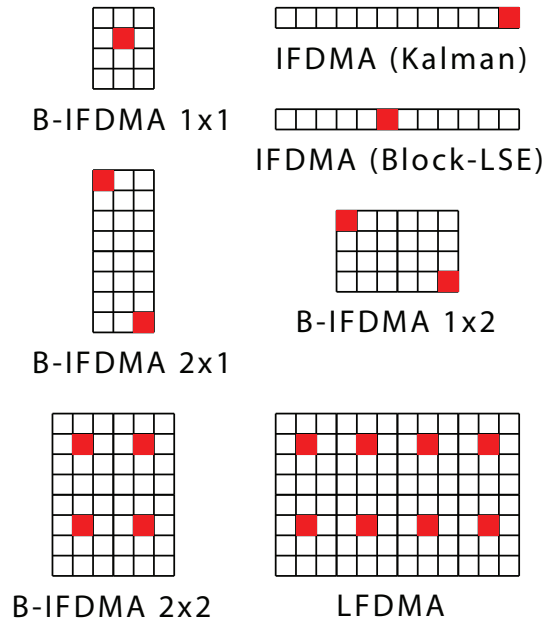


Fig. 7. The pilot patterns used for the investigated block allocations that use combinations of a basic block of 4-subcarriers by 3-OFDM-symbols, with one pilot and 11 payload symbols (i.e. pilot overhead 1/12): B-IFDMA 1x1 ($M = 4$, $N_t = 3$), 1x2 ($M = 4$, $N_t = 6$), 2x1 ($M = 8$, $N_t = 3$), 2x2 ($M = 8$, $N_t = 6$), IFDMA ($M = 1$, $N_t = 12$) and LFDMA ($M = 8$, $N_t = 12$). Time axis is horizontal and frequency axis is vertical in this figure. The pilot positions within blocks have been determined by global optimization of the channel estimation performance of the Block-LSE (Wiener) method, and they differ from those specified for uplinks in [4], [5].

channel estimation has been found to be beneficial for the IMT Advanced scenarios and pilot schemes, see [7] and [33]. It improves upon pilot-based estimates by 1-2 dB in realistic cases. The almost constant offset makes it possible to roughly estimate the accuracy of iterative schemes if the accuracy of the initializing pilot-based estimate is known. We therefore here focus on pilot-based non-iterative schemes.

The channel estimation performance is investigated below for two schemes:

- *Block Least Squares Estimation (Block-LSE):* Least squares estimation based on present but not past pilot data, also often called 2D-Wiener filtering [29], [30].
- Kalman smoothing [34], [35], using present and past pilots from every second time-slot backwards in time.³

The block sizes used in the investigations and the related pilot positions are illustrated by Fig. 7. The choice of these block sizes is related to the frame structure in the FDD mode of [4], [5]. In order to maintain a low radio access delay and to support also high speed trains, one slot (half frame) consists of only 12 OFDM symbols, [4], [5].

³Blocks from odd numbered past time-slots are not used. In half-duplex FDD uplinks they would be used by other UEs. In Time Division Duplex (TDD) systems, they would be used for downlink transmissions. The time-slots (half frames) are assumed to have duration 12 OFDM symbols as in [4], [5], [36].

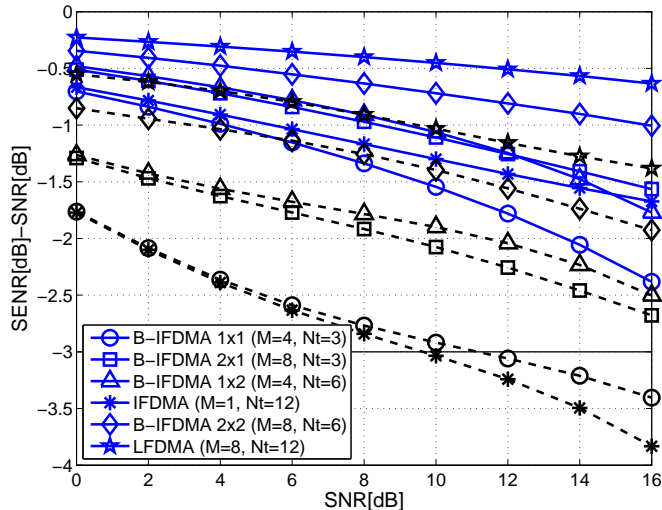


Fig. 8. Performance degradation in dB due to imperfect channel estimation versus ideal SNR. The vertical axis shows the difference between actual perceived signal-to-estimation-error-plus noise ratio (SENR, in dB) and ideal SNR (in dB). The horizontal axis shows the ideal SNR, i.e. assuming perfect channel state information. For example, the value -3 on the vertical axis means that a bit-error-rate curve generated in an idealized setting where perfect channel estimation is assumed should be displaced 3 dB to the right to correctly represent performance when the influence of channel estimation is taken into consideration. Solid curves represent (optimal) smoothed Kalman filter performance. Dashed curves represent Wiener filter performance, where no previous measurements are used by the estimator.

Here we consider uplinks, so neither method uses pilot information from subcarriers outside of the blocks. The results for the two estimation methods for the various block sizes are shown in Fig. 8, for UE velocity 50 km/h at 3.7 GHz carrier frequency as well as all other parameters as in Table I. Please refer to [37] for further details on the channel estimation methods and for additional results for other UE velocities and block sizes.

In [7] it has been shown that the effect of channel estimation errors on various decoder and detection algorithms in OFDM receivers can be well modelled by treating the estimation error as an additional white noise contribution at the receiver, with a variance given by the estimation error variance. Therefore, in Fig. 8 we show the channel estimation results in terms of SNR offset due to channel estimation errors at the receiver. This performance measure makes the results directly comparable to the SNR gains and losses due to different choices of number of subcarriers M per block in Figs. 3, 4 and 5, as discussed further in Section III-C.

It is evident that significant performance gains can be obtained by using Kalman smoothing which takes blocks in previous time-slots into account. Note that in the investigated case assuming half-duplex FDD, every second of the past timeslots cannot be used. The performance gain increases for slower UE velocities as shown in [37]. Full duplex FDD UEs would also benefit from the more dense slot and thus more dense pilot structure in time.

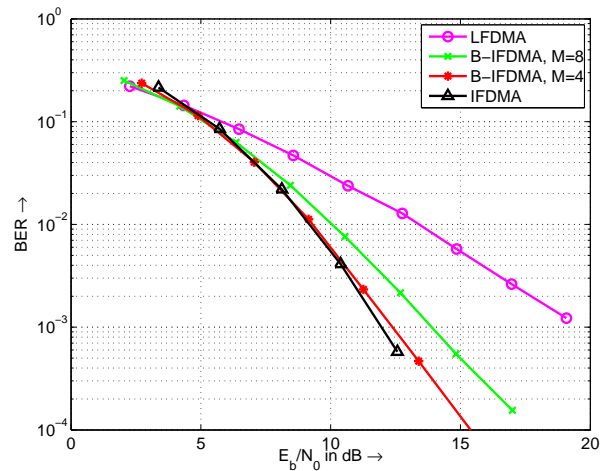


Fig. 9. Coded SISO performance for B-IFDMA, IFDMA and LFDMA with non-perfect channel estimation, and $Q = 32$ subcarriers assigned per user. The Block-LSE channel estimation performance results from Fig. 8 are used. B-IFDMA uses block of sizes ($M = 4, N_t = 6$) or ($M = 8, N_t = 6$).

C. Performance Trade-offs

By analyzing the results in Section III-A and Section III-B, we can quantify the trade-off between frequency diversity gains and channel estimation performance for different B-IFDMA subcarrier block sizes. To this end, we adopt the parameters of the FDD wide area mode in the IMT Advanced capable system concept in [4], [5].

In Fig. 9, we show such an example of combined diversity and channel estimation performance for the SISO case with Block-LSE channel estimation and $Q = 32$ subcarriers assigned per user. As seen, despite the better channel estimation with LFDMA, at this rather low number of Q IFDMA and B-IFDMA are substantially better than LFDMA. With increasing Q , B-IFDMA approaches IFDMA, and B-IFDMA becomes better than IFDMA when the diversity gains saturates in IFDMA. The reason for this is the better channel estimation performance for B-IFDMA, cf. Fig. 8. In particular, making the same comparison as in Fig. 9 but with $Q = 64$ subcarriers, B-IFDMA is better than IFDMA for both $M = 4$ and $M = 8$. At BER 10^{-3} , B-IFDMA with $M = 4$ is 0.5 dB better and B-IFDMA with $M = 8$ is 0.2 dB better than IFDMA. Note also that due to the block length $N_t = 6$ used in B-IFDMA, this performance is achieved with an average data rate over the chunk that is half compared to IFDMA and LFDMA, which is useful for transmission of small packets.

Below we exemplify the diversity versus channel estimation trade-off for B-IFDMA, assuming different block lengths N_t for both Block-LSE and Kalman channel estimation. Since the pilot overhead is the same for all considered schemes, this loss is not included.

Example 1: Referring to Table II, under the assumption that $Q = 32$ subcarriers are assigned to a user, we can see in Fig. 3 that at BER 10^{-3} in the SISO case when going from $M = 8$ to $M = 4$ subcarriers per block, i.e. changing from number of subcarrier blocks $L = 4$ to $L = 8$, there is a diversity gain of 1.9 dB, i.e. a reduction in required SNR from around

TABLE II

OVERALL PERFORMANCE COMPARISON OF SISO B-IFDMA WITH $Q = 32$ OR $Q = 64$ SUBCARRIERS PER USER AND $M = 4$ OR $M = 8$ SUBCARRIERS PER BLOCK WITH $N = 1024$ SUBCARRIERS IN THE SYSTEM.

Gain (dB)	$N_t = 3$		$N_t = 6$	
	Kalman	Block-LSE	Kalman	Block-LSE
B-IFDMA $Q = 32, M = 4$ versus $M = 8$ ($L = 8$ versus $L = 4$)				
Diversity, BER 10^{-3}	1.9	1.9	1.9	1.9
Channel est. 11 dB	-0.5	-0.8	-0.4	-0.5
Total	1.4	1.1	1.5	1.4
B-IFDMA $Q = 64, M = 4$ versus $M = 8$ ($L = 16$ versus $L = 8$)				
Diversity, BER 10^{-3}	0.7	0.7	0.7	0.7
Channel est. 10 dB	-0.5	-0.8	-0.4	-0.5
Total	0.2	-0.1	0.3	0.2

12.4 to 10.5 dB. This gain should be compared to the loss in channel estimation performance in Fig. 8 due to the fewer number of subcarriers per block. With block length $N_t = 3$, the channel estimation loss at the intermediate SNR 11 dB is -1.2 dB for $M = 8$ and -1.7 dB for $M = 4$ subcarriers per block with Kalman filtering. That is, there is an overall gain of $1.9 - 0.5 = 1.4$ dB including channel estimation for using $M = 4$ subcarriers compared to $M = 8$. With Block-LSE, the corresponding overall gain is $1.9 - 0.8 = 1.1$ dB. With the longer blocks having $N_t = 6$ (double mean data rate over the slot for a given number of blocks L) the corresponding gains when going from $M = 8$ to $M = 4$ are $1.9 - 0.4 = 1.5$ dB (Kalman) and $1.9 - 0.5 = 1.4$ dB (Block-LSE).

Example 2: In Table II, we also show the corresponding case with $Q = 64$ subcarriers per user based on the results in Fig. 4 and Fig. 8. Here the two cases with $M = 8$ and $M = 4$ subcarriers per block perform very similar, i.e. the diversity gain with $L = 16$ blocks compared to $L = 8$ blocks is almost completely lost due to the worse channel estimation performance.

Similar trade-off comparisons can be made for the MISO with Alamouti case and the MIMO with Alamouti and MRC case based on the diversity results in Fig. 6 and the channel estimation performance results in Fig. 8, since the results on channel estimation performance in Fig. 8 are directly applicable to uplinks with multiple UE antennas. Pilots are then placed at different time-frequency positions for different antennas, and these positions are not used by payload data at the other antennas to limit interference. Therefore, the pilot overhead increases, but the channel estimation accuracy stays unchanged. Due to the additional spatial diversity gains, fewer blocks L are typically needed, down to $L = 2$ to 4.

IV. ENERGY EFFICIENCY

In this section we aim to quantify the end-to-end energy efficiency of B-IFDMA. The aim of these investigations is to motivate the use of a DFT precoding step, and the advantage of the TDMA component within the B-IFDMA scheme. To this end, we start in Section IV-A by characterizing the envelope properties of B-IFDMA in terms of popular envelope variation metrics. These metrics are commonly used in the literature

to characterize the signal envelope variations and to give an indication of the efficiency of a generic High Power Amplifier (HPA). These results also motivate the regular subcarrier allocation in B-IFDMA. In order to give a quantitative measure of the energy efficiency with a representative HPA, we continue in Section IV-B by showing the HPA efficiency with different B-IFDMA parameterizations and different HPA operation modes for a real HPA. These investigations enable us to quantify the energy efficiency gains of DFT precoded schemes compared to OFDMA. In addition, they allow us to characterize the gains with time-localized transmission, and to quantify the end-to-end energy efficiency with various B-IFDMA parameterizations.

A. Envelope Properties

It is well known that for increasing envelope fluctuations of the transmit signal, the cost of a typical commercial HPA in the UE increases and the power efficiency decreases. Thus, especially in the uplink, the provision of low envelope fluctuations is important for the transmitted signal. In this section we investigate the envelope properties of B-IFDMA, and we predict the efficiency of the HPA based on an amplifier model. For that purpose, a signal model including oversampling, pulse shaping and windowing is assumed, all according to [38]. The oversampling factor is $S = 8$ and the pulse shaping filter is chosen such that an OFDM-like rectangular spectrum of the B-IFDMA signal is provided. Furthermore, a Raised-Cosine window with a roll-off region that is 5% of the symbol duration is applied.

In Fig. 10, the envelope of the B-IFDMA transmit signal is investigated in terms of the well-known Peak-to-Average Power Ratio (PAPR) [39] for $N = 1024$ subcarriers in the system and $Q = 64$ subcarriers assigned to a user using QPSK modulation. As references, the PAPR of two signals are given that differ from the B-IFDMA in the following properties: The first signal does not use DFT pre-coding and the second signal uses a random allocation of the subcarrier blocks instead of a regular one. From Fig. 10 it can be clearly seen that *both DFT pre-coding and regular allocation* of the subcarrier blocks is required in order to provide a low PAPR. B-IFDMA provides a mean PAPR that is 1.2-1.5 dB lower than the mean PAPR of the corresponding scheme without DFT pre-coding. Compared to a scheme with random allocation of the subcarrier blocks with DFT pre-coding, the PAPR gain of B-IFDMA is greater than 3 dB for a number $L = 64$ subcarrier blocks, i.e., for the special case of IFDMA. The gain decreases to ≈ 0.7 dB for $L = 4$ subcarrier blocks. For $L = 2$, the regular and the random allocation of the subcarrier blocks are equivalent except for the distance of the subcarrier blocks and, thus, the mean PAPR is similar.

Fig. 11 analyzes the envelope of the B-IFDMA transmit signal based on different metrics. In addition to the PAPR, the well-known Raw Cubic Metric (RCM) as defined in [40, eq. (15)], which is related to the 3GPP Cubic Metric (CM) in [41], is regarded. The motivation for the CM and RCM are the fact that the primary cause of distortion is the third order nonlinearity of the amplifier gain characteristic. Moreover, the HPA power efficiency is predicted. For that purpose, a non-linear amplifier is assumed that produces increased out-of-band radiation due to non-linear distortions dependent on the envelope of the input signal. The power efficiency of the given HPA depends on the

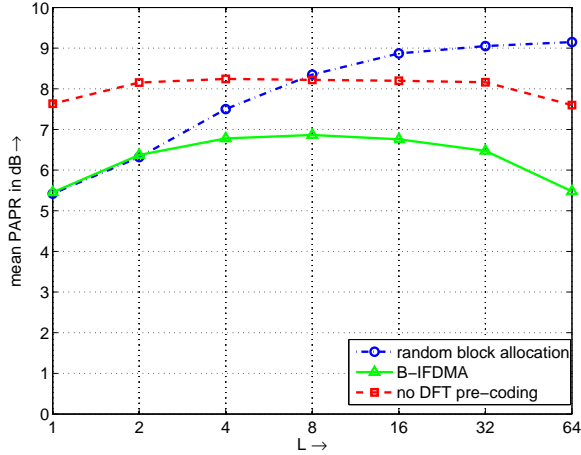


Fig. 10. Mean PAPR of B-IFDMA transmit signals with $Q = 64$ as a function of number of blocks L compared to the corresponding schemes without DFT pre-coding and schemes with random allocation of the subcarrier blocks.

power back-off (BO) that is required to meet a given spectral mask for the transmit signal. Thus, for investigation of the impact of the envelope fluctuations on the power efficiency, also the required BO is analyzed. In the following, for the HPA, the well-known Rapp model [39] with Rapp-parameter $p = 2$ is used which represents the model of a power amplifier with high non-linearities. The spectrum requirement mask is representative for IMT Advanced systems, and is given in [38].

The results for the different metrics are summarized in Fig. 11. Again, $N = 1024$ subcarriers is assumed in the system, with $Q = 64$ subcarriers per user and QPSK modulation. A scheme without DFT precoding is regarded as a reference. It can be concluded that, regardless of the number L of subcarrier blocks, for B-IFDMA, the envelope fluctuations are significantly lower compared to the scheme without DFT pre-coding. The mean PAPR and the RCM have a minimum for $L = Q$ and $L = 1$, i.e., for LFDMA and for IFDMA, where B-IFDMA can be interpreted as a single-carrier scheme and have a maximum for $L = 8$. However, even at the maximum, the envelope fluctuations of B-IFDMA are considerably lower than for a corresponding scheme without DFT pre-coding. In difference to the mean PAPR and the RCM, the required BO increases with decreasing number L of subcarrier blocks. The reason for that is that in addition to the envelope of the signal also the shape of the spectrum changes and the side-lobes are increased. However, for the special case of $L = 1$, i.e., for LFDMA, the side-lobes are significantly reduced. Thus, in this case, the spectral mask is less relevant, and results for $L = 1$ are omitted.

From Fig. 11 it can be concluded that the effects shown in Fig. 10 can be considered to be almost independent of the metric that is used. Thus, B-IFDMA can be considered to provide a higher power efficiency and lower envelope fluctuations compared to schemes without DFT pre-coding and without regular subcarrier allocation, respectively.

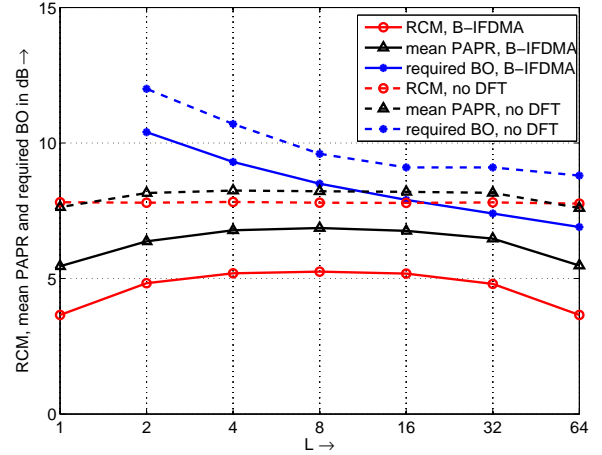


Fig. 11. Results for the analysis of the envelope fluctuations of B-IFDMA transmit signals with $Q = 64$ ("with DFT") compared to signals without DFT pre-coding for different numbers L of subcarriers per block using different metrics.

B. Gain with Time Localized Transmission

In Section IV-A, we characterized the envelope properties of B-IFDMA according to different metrics. In this section we make an analysis of the energy efficiency of B-IFDMA with a real amplifier. The aim of this investigation is to correlate the HPA energy efficiency with the prediction by the metrics in Section IV-A. The aim is also to show and quantify the gain by optimizing the operation point of the power amplifier, in order to motivate the benefit of the TDMA component within the B-IFDMA scheme.

1) *HPA Efficiency*: The efficiency of an HPA is best described by the *overall efficiency*, defined as

$$\eta_A = \frac{P_{\text{Out}}}{P_{\text{DC}} + P_{\text{In}}}, \quad (13)$$

where P_{In} is the power at the input of the HPA, and P_{Out} is the resulting output power. P_{DC} is the power at the DC input of the amplifier, computed as the product between the DC voltage and the DC current, $P_{\text{DC}} = V_{\text{DC}} \cdot I_{\text{DC}}$. For a given V_{DC} , the efficiency is a function mainly of the desired output power; the general trend is that the efficiency is higher for high output powers. However, by varying the drive voltage V_{DC} , the efficiency curve of the amplifier can be changed. In Fig. 12, we illustrate the overall efficiency as a function of output power for different drive voltages V_{DC} , when the input signal is an *unmodulated carrier* signal, using the HPA in [42].

Fig. 12 shows that the efficiency of the amplifier is highest when its output power is close to the maximum attainable output power, i.e. when it is driven close to saturation. However, due to the signal dynamics and other system considerations such as power control, it is in general not possible to drive the amplifier in its most efficient mode at all times. In situations when we need a lower average output power, we can see that by lowering the

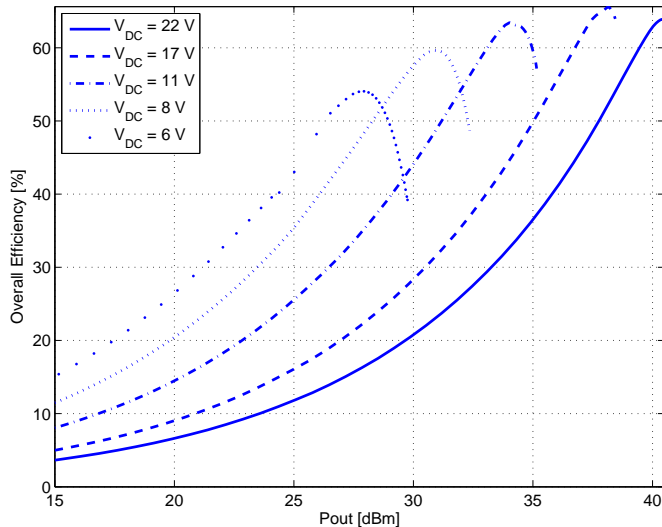


Fig. 12. Illustration of overall efficiency as a function of output power for different amplifier drive voltages V_{DC} using the HPA in [42], where $V_{DC} = 22$ V is the highest possible drive voltage.

(constant) drive voltage we can get an improved efficiency⁴, but the overall efficiency is still lower than when its output power is close to the maximum attainable output power.

We have evaluated the overall efficiency of several different amplifiers, when driven at different constant V_{DC} and with different *modulated* signals. The constant V_{DC} drive voltage has been chosen for maximum overall efficiency, and the following modulated input signals have been used: OFDM, IFDMA, LFDMA and B-IFDMA with different numbers of blocks (L) and pulse shaped as in Section IV-A.

To compute the overall efficiency of the HPA, we use the measured characteristics of the HPA in terms of required P_{DC} for a given P_{in} and desired P_{out} of each signal sample, and then we perform a weighted averaging over the consumed and transmitted powers using the desired output power histograms for the modulated signal. Thus, ideal predistortion of the signals is assumed, and the operation point is chosen such that maximum 1% of the samples are above the saturation point, which is generally regarded as an acceptable level of signal distortion. The results are shown in Table III. As can be seen:

- Due to the different amplitude distributions of these signals, they lead to different power efficiencies.
- In accordance with the envelope metric results in Section IV-A, and compared to the TDMA-OFDM system, the various DFT-precoding based schemes perform better both w.r.t. the overall efficiency and w.r.t. the maximum output power (not shown in Table III). This can potentially be used for increasing the cell size and/or larger data rates at a given path loss, provided regulations on maximum transmit power are not violated. The better HPA efficiency also implies less heat dissipation in the UE, which simplifies the design and can cut other supporting component costs.

⁴The optimal way of driving the amplifier would be to jointly vary the drive and Radio Frequency (RF) power for maximum efficiency [42], but this is not generally regarded as practical to implement today.

TABLE III

OVERALL EFFICIENCY η_A IN % OF THE HPA IN [42] WITH CONSTANT DRIVE VOLTAGE OPERATION WITH V_{DC} CHOSEN FOR MAXIMUM OVERALL EFFICIENCY FOR DIFFERENT INPUT SIGNALS, ALL USING QPSK SYMBOL CONSTELLATIONS AND A SYSTEM WITH $N = 1024$ SUBCARRIERS.

Const V_{DC}	Max efficiency	Max eff. -6 dB	30 dBm	24 dBm	18 dBm
TDMA-OFDM	40% @ 26 dBm	34% @ 20 dBm	39% @ 30 dBm	39% @ 24 dBm	29% @ 18 dBm
IFDMA Q=32	49% @ 30 dBm	43% @ 24 dBm	49% @ 30 dBm	43% @ 24 dBm	29% @ 18 dBm
B-IFDMA Q,M=32,4	47% @ 28 dBm	38% @ 22 dBm	45% @ 30 dBm	41% @ 24 dBm	29% @ 18 dBm
B-IFDMA Q,M=64,4	46% @ 28 dBm	38% @ 22 dBm	45% @ 30 dBm	41% @ 24 dBm	29% @ 18 dBm
B-IFDMA Q,M=128,4	46% @ 28 dBm	38% @ 22 dBm	45% @ 30 dBm	41% @ 24 dBm	29% @ 18 dBm
LFDMA Q=32	48% @ 28 dBm	38% @ 22 dBm	47% @ 30 dBm	42% @ 24 dBm	29% @ 18 dBm

- The difference in efficiency of the various DFT precoded schemes is very small, including the B-IFDMA scheme. In particular, these differences are smaller than predicted by the envelope metric results in Section IV-A.

The results in Table III were obtained using the class E Laterally Diffused Metal Oxide Semiconductor (LDMOS) amplifier in [42]. However, to verify the qualitative conclusions we have also repeated the experiments with a class D LDMOS and a class E Gallium Nitride (GaN) amplifier. We have also studied other designs in the literature, e.g. [43], and other classes of operation, such as class A, AB or B. The overall conclusion is that the qualitative results are the same as above regardless of the amplifier.

2) *Efficient HPA Operation*: From the results in Table III we see that there is a gain to be made if the power amplifier as often as possible can operate close to its optimal operation point. However, in order to limit the Multiple Access Interference (MAI) from different users in a multi-carrier based uplink due to imperfections in transmitter hardware, synchronization and Doppler spread, it is important to have some kind of power control to limit the difference in received power spectral density from different users. Thus, if all users were allocated the same number of subcarriers, with a constraint on maximum received power spectral density, there would be situations when the HPA has to operate at a low and suboptimal transmit power level. In these scenarios HPA efficiency would benefit from an increase in the number of allocated subcarriers in a given OFDM symbol, because then the UE could transmit during a shorter time, i.e. on a lower number of OFDM symbols, for a given average data rate. One possibility to do this would be to decrease the subcarrier separation in an IFDMA scheme, but that would imply a larger channel estimation overhead due to the low correlation among the subcarriers as shown in Section III-B. With a short frame duration, aiming at low delays, this overhead would be prohibitive. In addition, it would limit the possibility for co-existence with adaptive TDMA/OFDMA as discussed in [9].

In order to quantify the HPA efficiency with and without time localized transmission, we assume that the choices are to

either a) transmit at full power 25% of the time, and turn off the transmitter for 75% of the time, or b) to transmit at 25% of full power all the time. Thus, in scenario b) the amplifier is backed-off 6 dB compared to scenario a). In a BS, the amplifier is usually optimized for a high output power, while in the UEs the amplifier works at a low power level most of the time, e.g. 21 – 46 dBm for BSs and 21 – 24 dBm for UEs depending on the deployment scenario ranging from local area to wide area, [19].

As seen in Table III maximum overall efficiency is obtained when operating the HPA close to the maximum output power level. Thus scenario a) leads to higher efficiency in all cases. E.g. assume the same number of well separated blocks L . If the options are to use IFDMA in the full duration of a chunk with 32 subcarriers at a constant output power level of 18 dBm, we get an overall HPA efficiency of 29% (Table III row 2, column 5), whereas if we use B-IFDMA with $Q = 128$ subcarriers and $M = 4$ subcarriers per block (i.e. $L = 32$ blocks) one quarter of the frame duration and an instantaneous output power level of 24 dBm, we get an overall HPA efficiency of 41% (Table III row 5, column 4). The corresponding difference is smaller when the average transmit power is closer to the maximum efficiency. E.g. at 24 dBm average transmit power the corresponding overall efficiencies are 43% (Table III row 2, column 4) for IFDMA and 45% (Table III row 5, column 3) for B-IFDMA. Thus, there is a large benefit to introduce a TDMA component in the B-IFDMA scheme in order to allow a shorter transmit duration than a full frame with a larger instantaneous data rate, except in case the required overall data rate is already close to the maximum supported. With time-localized transmission and reception, we also introduce the additional possibility of micro-sleep mode within scheduled frames. The feasibility and potential of micro-sleep mode is discussed in [12].

C. End-to-end Energy Efficiency

By combining the results in Section IV-A and Section IV-B with the results in Section III, we can quantify the end-to-end energy efficiency for different B-IFDMA parameterizations. Below we illustrate this trade-off, by building on the examples in Section III-C, assuming a target BER of 10^{-3} .

Example 1 revisited: Similar to the mean PAPR results for $Q = 64$ subcarriers in Fig. 10, the mean PAPR for B-IFDMA with $Q = 32$ subcarriers is very similar for $M = 4$ ($L = 8$) and $M = 8$ ($L = 4$). In addition, not shown in this paper, the mean PAPR values of B-IFDMA have been found to correlate well with the overall HPA efficiency values. Thus, with SISO using $Q = 32$ subcarriers, the scheme with $L = 8$ blocks with $M = 4$ subcarriers each seems to provide the best trade-off also considering end-to-end energy efficiency.

Example 2 revisited: The HPA efficiency for $Q = 64$ predicted by the mean PAPR as shown in Fig. 10 is very similar also for $L = 16$ blocks compared to $L = 8$. Thus, also w.r.t. end-to-end energy efficiency the two cases with $M = 4$ and $M = 8$ subcarriers per block seem to perform very similar. If instead the HPA efficiency is predicted by the required power backoff to satisfy a spectrum mask, the results for required BO in Fig. 11 apply. In this case, the end-to-end energy efficiency seems to be around 0.5 dB better with $L = 16$, i.e. for $M = 4$ subcarriers per block.

TABLE IV

END-TO-END ENERGY EFFICIENCY COMPARISON OF SISO B-IFDMA USING BLOCK SIZE $M = 4$, $N_T = 3$ AND $Q = 128$ SUBCARRIERS PER USER AT TWO DIFFERENT HPA OUTPUT POWER LEVELS VERSUS B-IFDMA USING BLOCK SIZE $M = 1$, $N_T = 12$ AND $Q = 32$ SUBCARRIERS PER USER AT -6 DBM LOWER HPA OUTPUT POWER LEVEL. IFDMA USES 4 TIMES LONGER BLOCKS. $L = 32$ IN BOTH CASES AND THERE ARE $N = 1024$ SUBCARRIERS IN THE SYSTEM.

Gain (dB)	30 dBm		24 dBm	
	Kalman	Block-LSE	Kalman	Block-LSE
B-IFDMA $M = 4$, $N_t = 3$, $Q = 128$ versus $M = 1$, $N_t = 12$, $Q = 32$				
Diversity, BER 10^{-3}	0.24	0.24	0.24	0.24
Channel est. 9 dB	-0.15	0.1	-0.15	0.1
HPA efficiency	0.2	0.2	2.07	2.07
Total	0.29	0.54	2.16	2.41

In the next example, we now make a comparison between B-IFDMA and IFDMA with the same data rate, also taking the end-to-end energy efficiency into account.

Example 3: Let us compare the two options to use IFDMA in SISO at the *same data rate*, e.g. B-IFDMA using $M = 1$, $L = 32$ and $N_t = 12$ having $Q = 32$ subcarriers for the user with B-IFDMA using $M = 4$, $L = 32$ and $N_t = 3$ having $Q = 128$ subcarriers. The data rate is the same since in both cases $M \cdot N_t \cdot L = 384$ symbols are transmitted per slot. To generate the same RF energy, IFDMA would operate with 6 dB less transmit power during 4 times longer duty cycle. Thus, this scenario is especially relevant for the case when the required uplink data rate is below the maximum achievable for the UE at the given channel conditions. Consider the diversity gains in Fig. 6, the channel estimation performance in Fig. 8 and the HPA efficiency for this case in Table III. Using the corresponding HPA efficiency values as discussed in Section IV-B.2, the end-to-end energy efficiency comparison is shown in Table IV for target BER 10^{-3} . As seen in Table IV, there is an overall gain for B-IFDMA with $M = 4$ over the IFDMA case. The gain is more than 2 dB at low output power levels, but there is a substantial gain also at operation closer to the maximum output power level. This gain is achieved without considering additional potential sleep mode gains enabled by the short blocks, as mentioned in Section IV-B.2.

V. ROBUSTNESS

In this section, the robustness of B-IFDMA to carrier frequency offsets (CFOs) and to Doppler spreads (DSs) is analyzed for the uplink dependent on the signal parameters. The aim of this investigation is to show that the block based subcarrier allocation in B-IFDMA enables the possibility to combine robustness and provision of frequency diversity.

In mobile radio applications, CFOs are typically caused by oscillator imperfections due to low cost hardware components or Doppler shifts due to the mobility of the users. The CFOs result in a shift of the spectra of the different users' signals. Hence, the orthogonality of the subcarriers is destroyed and inter-carrier interference (ICI) occurs.

In general, two types of ICI can be distinguished. Regarding a particular user's signal, on the one hand, due to the shift of the

spectrum, interference between the subcarriers of this user occurs. In the following this is denoted as self-interference (SI). On the other hand, in addition interference between the subcarriers of different users occurs. This case is in the following denoted as multiple access interference (MAI).

The DS is caused by the fact that in a mobile radio channel typically the same signal is received from different propagation paths where each path suffers from a different Doppler shift. The superposition of differently shifted replicas of the same signal at the receiver leads to a spread of the subcarriers of the different users' signals. Consequently, also for DSs the orthogonality of the subcarriers is destroyed and ICI occurs. Similar to the effects of CFOs, also for DSs two types of ICI, namely SI and MAI can be distinguished.

For uplink transmission, the CFOs and the DS for the received signals of different users are different. Thus, if CFOs and DS are known at the receiver, compensation of SI is possible, whereas compensation of MAI can only be obtained by application of joint detection techniques that require a high computational effort.

For the analysis of the robustness of B-IFDMA to CFOs, let

$$\Delta \bar{f}_{\text{CFO}}^{(k)} = \frac{\Delta f_{\text{CFO}}^{(k)}}{\Delta f} \quad (14)$$

denote the relative CFO of user k normalizing the CFO $\Delta f_{\text{CFO}}^{(k)}$ of user k to the subcarrier bandwidth Δf . The relative CFO $\bar{f}_{\text{CFO}}^{(k)}$ is modelled as a random variable that is uniformly distributed in $[-\Delta \bar{f}_{\text{CFO,max}}^{(k)}, \Delta \bar{f}_{\text{CFO,max}}^{(k)}]$ with $\Delta \bar{f}_{\text{CFO,max}}^{(k)}$ denoting the maximum relative CFO of user k that occurs. The CFOs $f_{\text{CFO}}^{(k)}$ are assumed to be known at the receiver. Thus, SI can be perfectly compensated by reversing the CFO $f_{\text{CFO}}^{(k)}$. For the compensation of the MAI, joint detection techniques are required. For this investigation, it is assumed that, due to the high complexity, the compensation of MAI at the receiver is not feasible. In order to analyze the robustness to CFOs independently of the diversity effects, a B-IFDMA transmission over an AWGN channel is regarded.

For the analysis of the robustness of B-IFDMA to DSs, let

$$\Delta \bar{f}_{\text{DS}}^{(k)} = \frac{\Delta f_{\text{DS}}^{(k)}}{\Delta f} \quad (15)$$

denote the relative DS of user k normalizing the DS $\Delta f_{\text{DS}}^{(k)}$ of user k to the subcarrier bandwidth Δf . Similar to the modelling of the CFOs, also the DS $\Delta \bar{f}_{\text{DS}}^{(k)}$ is modelled as a random variable. Assuming that for the different propagation paths the angle of arrival is uniformly distributed in $[0, 2\pi]$, the relative Doppler shift is Jakes distributed in $[-\Delta \bar{f}_{\text{D,max}}^{(k)}, \Delta \bar{f}_{\text{D,max}}^{(k)}]$, where $\Delta \bar{f}_{\text{D,max}}^{(k)}$ denotes the maximum Doppler shift normalized to the subcarrier bandwidth Δf . At the receiver, SI is combatted by application of a linear Minimum Mean Square Error (MMSE) receiver, cf. [44]. For the compensation of the MAI, again, joint detection techniques are required and it is assumed that, due to the high complexity, the compensation of MAI at the receiver is not feasible. In order to separate the effect of the Doppler spread from frequency selective fading effects that are also caused by multi-path propagation, a Doppler spread channel according to [44] is regarded, i.e., the different propagation

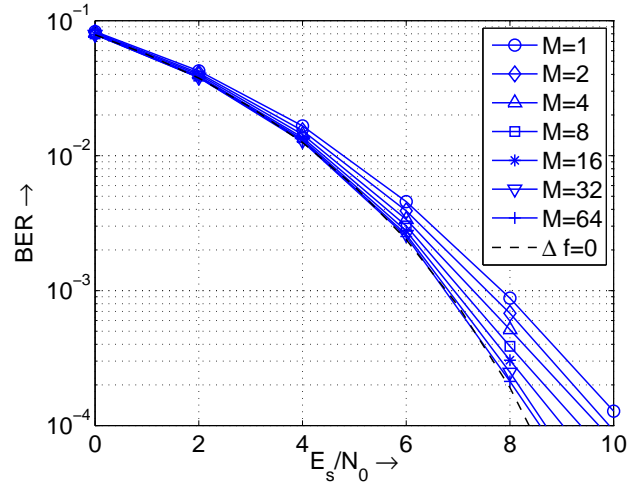


Fig. 13. Performance for $\Delta \bar{f}_{\text{CFO}}^{(k)} = 10\%$ maximum relative CFO for different numbers M of subcarriers per block, assuming $N = 1024$ subcarriers and $Q = 64$ subcarriers per user.

paths are assumed to arrive at the receiver at the same time. The channel is distorted by AWGN and the received signals from the different propagation paths suffer from mutually independent relative Doppler shifts.

Fig. 13 depicts the performance results without coding for the robustness investigations to CFOs assuming $N = 1024$ subcarriers in the system, $Q = 64$ subcarriers per user, $K = 16$ users and $\Delta \bar{f}_{\text{CFO}}^{(k)} = 10\%$ for all users. From Fig. 13 it can be concluded that, for B-IFDMA, the robustness to CFOs increases with an increasing number M of subcarriers per block. The reason for that is that the strongest inter-carrier interference is caused by neighboring subcarriers. Thus, increasing the number of neighboring subcarriers belonging to the same user increases the robustness to MAI at the expense of additional SI that, however, can be compensated. Note, that already for low numbers M of subcarriers per block the robustness of B-IFDMA to CFOs is significantly improved.

Fig. 14 depicts the performance results for the robustness investigations to DS assuming the same parameters as in Fig. 13 and $\Delta \bar{f}_{\text{D,max}}^{(k)} = 15\%$ for all users. The value for $\Delta \bar{f}_{\text{D,max}}^{(k)}$ represents the maximum relative Doppler shift for a system with $\Delta f = 10$ kHz and a carrier frequency of 5 GHz with a user velocity of 315 km/h and, thus, represents a high mobility scenario, e.g., for high speed trains.

From the results in Fig. 14 it can be concluded that also the robustness of B-IFDMA to DS increases with an increasing number M of subcarriers per block. The reason is the same as for the improved robustness to CFOs. Again, already for small numbers M a significant robustness gain is provided. The increased robustness to CFOs and DSs of B-IFDMA with $M > 1$ makes B-IFDMA suitable for high speed users and systems with limited frequency synchronization.

VI. DISCUSSION OF RESULTS

In this section we summarize and comment on the investigations made in Section III, Section IV and Section V. In Section I, we identified the following important requirements for the diver-

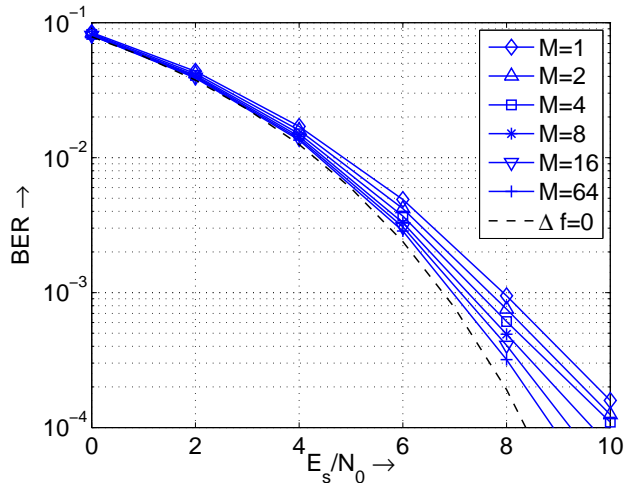


Fig. 14. Performance for Doppler Spread with $\Delta \bar{f}_{\text{CFO}}^{(k)} = 15\%$ relative carrier frequency offset per path for different numbers M of subcarriers per block, assuming $N = 1024$ subcarriers and $Q = 64$ subcarriers per user.

sity based multiple access scheme, which should complement the FA multiple access scheme in an IMT Advanced capable system. Below we comment on the suitability of B-IFDMA to meet these requirements.

- *Robustness to small-scale fading without time diversity:* The results in Section III showed that B-IFDMA can be defined based on a rather few number of subcarriers per block also with realistic channel estimation performance. Thus, also at rather low data rates, i.e. rather few subcarriers assigned to a user per slot, a large frequency diversity can be obtained.
- *Tuneable degree of frequency-diversity:* As shown in Section III-C and Section IV-C rather small blocks, also with a sub-slot duration, can provide a good error rate performance. Thus, for a given data rate additional blocks can be allocated either well-separated in frequency to provide additional frequency-diversity, or adjacent in time or frequency (i.e. in same chunk cf. Fig. 1), if enough diversity is already obtained from the frequency and/or spatial domain.
- *Need to support high energy efficiency in the transmitters and the receivers:* We showed in Section IV that B-IFDMA including pulse shaping can provide similar HPA efficiency as IFDMA and LFDMA, which is substantially better than for TDMA-OFDM without DFT precoding. In addition, whenever the UE is not power limited, in Section IV-C a substantial overall gain of more than 2 dB is shown with time localized transmission in a fraction of the time slot, also when including realistic channel estimation performance and disregarding potential sleep mode gains.⁵
- *Robustness to carrier frequency offsets and large Doppler spread:* This property was evaluated in Section V and the conclusion is that already for small numbers of subcarriers per block a significant robustness gain against carrier CFOs as well as against Doppler spreads is provided compared to IFDMA. This property could provide a significant gain in

⁵These results are valid also for a downlink scenario using the B-EFDMA scheme.

certain scenarios, like for deployment in frequency bands using a several GHz carrier frequency. Another scenario is to support high-speed trains, and/or to deploy a system with rather narrow subcarrier bandwidth.

- *Support for widely varying packet sizes:* Due to the good error rate performance of B-IFDMA with few number of subcarriers, transmission of rather small blocks perform well by using the TDMA component. Large packets can use the full chunk duration. The benefit of configuration flexibility motivates the introduction of a small basic block consisting of e.g. $M = 4 \times N_t = 3$ (subcarriers \times OFDM symbols) in B-IFDMA as a building block to enable adaptive block allocation in different deployment and usage scenarios, as illustrated in Fig. 1, see [5], [45] for further discussion.
- *Enable efficient resource allocation:* As discussed in [45] just a few different block allocations should be sufficient in a cell. The regular block allocation is beneficial for low addressing overhead, and it was shown in Section IV-A to also be beneficial for lowering the envelope variations.
- *Be of use for in-band control signals:* This is possible due to the efficient support for small packets as discussed above. In addition, the short TDMA component in B-IFDMA is useful to support precise timing of control messages for FA transmission, cf. [9].
- *Enable efficient co-existence with adaptive TDMA/OFDMA:* Since B-IFDMA also is based on OFDM with the same parameters, these two schemes are compatible. With well-separated regular block allocations in frequency, adaptive TDMA/OFDMA resources can be interlaced as shown in e.g. Figure 2 in [9].
- *Facilitate low complexity transmitter in UEs:* The good envelope properties of B-IFDMA enables the use of a less complex HPA and predistortion unit. In the Appendix we show that a B-IFDMA signal can be efficiently generated in the time domain, i.e. without the DFT operation.

VII. CONCLUSIONS

In this paper we have shown that B-IFDMA, which is a generalization of the SC-FDMA concept, is a power efficient, flexible and scalable multiple access scheme that can serve as a robust complement to future adaptive IMT Advanced capable wireless systems. Based on the included investigations, we have shown that B-IFDMA is able to provide equal or better error rate performance than IFDMA and LFDMA, when considering realistic channel estimation performance at the receiver and no reliable channel state information at the transmitter, also for rather low data rates, and without using time-diversity.

We also showed that B-IFDMA provides better amplifier efficiency than OFDMA and can provide better end-to-end energy efficiency than IFDMA and LFDMA. These investigations motivated the use of the DFT precoding step, and the integration of the TDMA component within the B-IFDMA scheme. These results also motivated the use of a regular subcarrier allocation in B-IFDMA.

Then, we showed that B-IFDMA offers the possibility to combine robustness against carrier frequency offsets and Doppler spread with provision of frequency diversity. This property could provide a significant gain in certain scenarios,

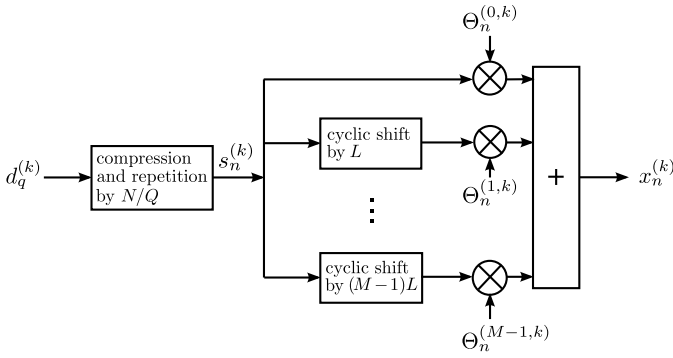


Fig. 15. B-IFDMA time domain modulation.

like for deployment in frequency bands using a several GHz carrier frequency. Another scenario is to support high-speed trains, and/or to deploy a system with rather narrow subcarrier bandwidth.

Finally, we argued for that B-IFDMA has the capability to fulfill and provide a good trade-off between the requirements envisioned for the robust transmission mode in the uplink of future IMT Advanced capable wireless systems.

APPENDIX TIME DOMAIN REPRESENTATION

In this appendix, the samples of the B-IFDMA time domain signal are analyzed. For sake of simplicity, throughout this appendix, the index η is omitted. Combining the pre-coding, the user specific block-interleaved subcarrier mapping and the OFDM modulation, the elements $x_n^{(k)}$, $n = 0, \dots, N - 1$, of the modulated data vector $\mathbf{x}^{(k)}$ in (6) can be written as

$$x_n^{(k)} = \sum_{\mu=0}^{M-1} d_{(n+\mu L) \bmod Q}^{(k)} \cdot \Theta_n^{(\mu,k)} \quad (16)$$

with

$$\Theta_n^{(\mu,k)} = \frac{L}{\sqrt{QN}} e^{j \frac{2\pi}{N} nkM} \sum_{m=0}^{M-1} e^{-j2\pi m (\frac{n}{Q} - \frac{n}{N} + \frac{\mu}{M})} \quad (17)$$

for $\mu = 0, \dots, M - 1$. The derivation can be found in [46]. Eq. (16) is illustrated in Fig. 15.

The sequence $d_{(n+\mu L) \bmod Q}^{(k)}$ in (16) can be interpreted as a compression of the sequence of data symbols $d_q^{(k)}$, $q = 0, \dots, Q - 1$, in time by factor N/Q , a subsequent N/Q -fold repetition and, finally, a cyclic shift of the N elements of the resulting sequence by $n + \mu L$, as illustrated in Figure 3 in [46]. Thus, B-IFDMA can be considered as a superposition of M single carrier signals weighted by different complex numbers $\Theta_n^{(\mu,k)}$.

The expression $e^{j \frac{2\pi}{N} nkM}$ in (17) represents a user specific frequency shift by kM . For $M = 1$ the expression $\Theta_n^{(\mu,k)}$ reduces to

$$\Theta_n^{(\mu,k)} = \sqrt{\frac{Q}{N}} e^{j \frac{2\pi}{N} kn}. \quad (18)$$

and (16) simplifies to compression and repetition of the data symbols, subsequent user specific frequency shift and a normalization to $\sqrt{Q/N}$. This is equivalent to the generation of

an IFDMA signal [14] which is a single carrier signal, i.e. a serially modulated carrier. Note that also for the special case $M = Q$, an expression is obtained that is equivalent to a single carrier signal because for this case the expression from (16) is equivalent to the time domain samples of an LFDMA signal that are described in [47].

Since the coefficients by (17) are independent from the data symbols, they can be calculated offline. Thus, (16) also represents an alternative implementation for B-IFDMA modulation that does not require N and Q to be powers of 2 as it would be the case for an implementation of B-IFDMA modulation according to (6), if the Fast Fourier Transform (FFT) algorithm is used.

Similar to the modulation, also the B-IFDMA demodulation can be reformulated as follows. The elements $\rho_q^{(k)}$, $q = 0, \dots, Q - 1$ of the demodulated B-IFDMA signal

$$\rho_q^{(k)} = \mathbf{F}_Q^H \cdot \left(\mathbf{M}_{\text{BI}}^{(k)} \right)^\dagger \cdot \mathbf{F}_N \cdot \mathbf{r} \quad (19)$$

can be expressed as

$$\rho_q^{(k)} = \sum_{\nu=0}^{N/L-1} r_{(q+\nu L) \bmod N} \cdot \Psi_{(q+\nu L) \bmod N}^{(\nu,k)} \quad (20)$$

with

$$\Psi_n^{(\nu,k)} = \left(\Theta_n^{(-\nu \bmod M,k)} \right)^* ; \quad n = (q + \nu L) \bmod N. \quad (21)$$

The derivation of the demodulator can be found in [46] with an illustration in Figure 4 in [46]. It can be regarded as a generalization of the demodulation for IFDMA described in [14].

ACKNOWLEDGMENT

This work has partly been performed in the framework of the IST project IST-4-027756 WINNER II, which was partly funded by the European Union. The authors would like to acknowledge the contributions of their colleagues in WINNER II, although the views expressed are those of the authors and do not necessarily represent the project.

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