Design aspects related to noise in indirect heat pumps

Master’s Thesis within the Sustainable Energy System programme

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Division of Building Services Engineering
CHALMERS UNIVERSITY OF TECHNOLOGY
Göteborg, Sweden 2014
Report No 2014:01
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ABSTRACT

An increased use of heat pumps is one of the measures that can be taken to reduce energy consumption on a large scale, particularly in areas where buildings generally are heated by electrical radiators. For a wider acceptance, and a major heat pump market expansion, it is crucial to develop heat pumps that cause minimal disturbance, especially in densely populated areas.

Results from field measurements made by SP Technical Research Institute of Sweden indicate that the use of so called indirect heat pumps has potential to significantly reduce the noise level of ambient air heat pumps. The noise level caused by such heat pump has been shown to be highly influenced by the design of the air-to-fluid heat exchanger in its outdoor unit.

It has been identified that it is mainly the air flow delivered by the fan and the resulting pressure drop in the air flow across the heat exchanger that together influence the level of noise. Hence, in order to achieve an acceptable noise level, the heat exchanger needs to be of such design that the necessary air flow and resulting pressure drop can be limited to a certain level.

The overall purpose of this study is to propose a design of an air-to-fluid heat exchanger for an indirect ambient air heat pump system that allows for a well performing system as well as a low level of noise and cost. Two different types of heat exchangers, with flat tubes and round tubes, are designed and compared for suitability.

Using relevant data and literature on heat transfer and heat exchangers, the necessary size (height, width and depth) and air flow of the different heat exchangers is calculated using Matlab, including the resulting noise level.

According to the results of the study, a heat exchanger with flat tubes and plain fins is the most suitable out of the studied designs. It is shown that such a unit needs to be 700 mm high, 700 mm wide and 80 mm deep, therefore displacing a volume of around 0.04 m$^3$. An alternative design with flat tubes that instead has wavy fins is practically as suitable. Two round tube heat exchangers were also evaluated and both showed to be significantly less suitable than any of the flat tube heat exchangers, displacing more than twice the volume. The reason the flat tube heat exchangers turned out more suitable is shown to be that the heat transfer resistance on their tube side is significantly lower, while the resistance on the outside still is comparable to that of the round tube heat exchangers.

Key words: Heat exchanger, Indirect heat pump, Flat tube, Round tube, Wavy fin, Plain fin, Fan noise level
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Preface

In this study, heat exchanger modeling has been made with the intent to minimize noise level, energy losses, and cost. The study has been carried out from June 2013 to January 2014.

Ola Gustafsson, industrial student at SP Technical Research Institute of Sweden, and Professor Jan-Olof Dalenbäck at Chalmers University of Technology have supervised the study. The work is part of a research project carried out by SP Technical Research Institute of Sweden, and has been carried out by Christopher Cinadr and Per Löved. During the work, Ola Gustafsson has been of great help and guided us skillfully at all times.

Gothenburg, January 2014

Christopher Cinadr
Per Löved
Notations

Roman upper case letters

\( A \) area, \( m^2 \)

\( A_c \) minimum free flow area, \( m^2 \)

\( A_t \) total heat transfer area, \( m^2 \)

\( A_{fr} \) frontal area, \( m^2 \)

\( C_1 \) heat capacity rate fluid 1, W/K

\( C_2 \) heat capacity rate fluid 2, W/K

\( C_r \) heat capacity flow rate ratio

\( D \) diameter

\( G \) mass velocity, kg/m²s

\( H \) height, m

\( L \) core length, m

\( NTU \) number of transfer units

\( P_1 \) temperature effectiveness

\( P_{1,p} \) temperature effectiveness per heat exchanger/pass

\( Pr \) Prandtl number

\( Q \) heat transfer rate, W

\( Q_{air} \) air flow, m²/h

\( R \) heat capacity ratio

\( Re \) Reynolds number

\( T \) temperature, °C

\( T_p \) tube pitch

\( U \) overall heat transfer coefficient, W/m² K

Roman lower case letters

\( c_p \) specific heat capacity, kJ/kg K

\( h \) heat transfer coefficient, W/m²K

\( j \) Colburn correction factor

\( k \) thermal conductivity, W/m K

\( l \) half wall spacing, m

\( \dot{m} \) mass flow, kg/s

\( n \) number of tubes

\( p \) pressure
Greek letters

\(\Delta\) difference
\(\varepsilon_p\) heat exchanger effectiveness per heat exchanger/pass
\(\eta_o\) surface efficiency
\(\delta\) Fin thickness, m
\(\rho\) density, kg/m\(^3\)
\(\sigma\) free flow area / frontal area

Subscripts

\(a\) air
\(b\) brine
\(f\) fin
\textit{flat} flat tube geometry
\(h\) hydraulic
\(i\) inner
\(lf\) laminar flow
\textit{max} maximal
\textit{min} minimum
\(o\) outer
\(r\) refrigerant
\textit{round} round tube geometry
\(s\) sensible
\(t\) transversal
\(tf\) turbulent flow
1 Introduction

To fully or partially satisfy a building’s demand for hot water for its radiator system and tap water, an air-to-water heat pump can often be used. Conventional heat pumps of this kind have a majority of their components placed outdoors, in a unit in close connection to the building that it serves. These are components such as a fan, a compressor and heat exchangers, which altogether comprise a noise generating unit, likely causing disturbance to both the residents of the building and people in the vicinity. Heat pumps causing minimal disturbance are naturally advantageous, especially in densely populated areas where less disturbance may even be crucial for heat pump market expansion. In turn, an increase in use of heat pumps is one of the measures that can be taken to reduce energy consumption on a large scale, particularly in areas where buildings generally are heated by electrical radiators.

Results from field measurements made by SP Technical Research Institute of Sweden indicate that the use of a so called indirect heat pump system has a potential to significantly reduce the noise level for different reasons. In such a system, most components of the heat pump are placed on the inside of the building, leaving an outdoor unit comprised of only an air-to-fluid heat exchanger and a fan. Assuming that the noise generated indoors, i.e. noise caused mainly by the compressor, is fully isolated to the inside of the building, it is in this case only the outdoor unit that generates a significant noise level and thereby causes disturbance to the surroundings.

The noise level caused by the outdoor unit in an indirect heat pump system has been shown to be highly influenced by the design of the air-to-fluid heat exchanger. It has been identified that it is mainly the flow of air delivered by the fan and the resulting pressure drop in the air flow across the heat exchanger that together influence the level of noise. Hence, in order to achieve an acceptable noise level, the heat exchanger needs to be of such a design that the necessary air flow and resulting pressure drop can be limited to a certain level. The heat exchanger design should also, if possible, be such that it makes the indirect heat pump compatible with different operating conditions, and have an energy performance comparable to that of a conventional heat pump.

1.1 Aim and purpose

The overall purpose of this study is to propose a design of an air-to-fluid heat exchanger for an indirect heat pump system that allows for a well performing system as well as a low level of noise and cost. The effects of different heat exchanger designs on performance and noise level in an indirect heat pump system will also be evaluated. Specific questions that are to be answered to fulfill the purpose are:

- Given a certain outdoor temperature and heat demand, how should the air-to-fluid heat exchanger be designed in order to achieve an acceptable level of noise and a heat pump energy performance at least as high as that of a comparable conventional heat pump?
- How can the design of the air-to-fluid heat exchanger be correlated to the noise generation of the outdoor unit?
How much does the optimized design of the heat exchanger, in terms of noise generation, correlate to the overall energy performance of the heat pump?

1.2 Limitations

Noise generated by components placed on the inside of the building is assumed to have no effect on noise levels on the outside of the building. The only noise of significance is assumed to be the noise generated outdoors, meaning only by the outdoor unit of the indirect heat pump system, i.e. the fluid-to-air heat exchanger and the fan.

The noise level caused by a heat pump may depend on if it is running at steady-state conditions or not, and if it is running a defrost process. In this study, it is the noise level of when the heat pump runs at normal steady-state conditions that is considered. I.e. it is the so called continuous noise level that is regarded during the design process. Also, only one temperature condition is included, which is more specifically described in following chapters.

The criteria for the outdoor unit are set by the performance of an already existing conventional heat pump with a certain capability of delivering heat, while generating an exceptionally low level of noise. This heat pump will be referred to as the reference heat pump and is of air-to-water type with a heat output similar to that of a heat pump normally installed in a typical one family residential building in Sweden. The design of the indirect heat pump system, apart from the outdoor unit, will not be subject to any optimization or modification.

Only four different types of heat exchangers will be designed and compared for suitability. Two are with round tubes and continuous fins, one is with flat tubes and plain fins, and one is with flat tubes and wavy fins. These are types of heat exchangers for which Kays & London (1984) have established correlations for heat transfer and pressure drop. Kays & London have done so for a number of specific geometries of each heat exchanger type, and it is exclusively these that will be included in this study.

In order to determine which heat exchanger is the least expensive, the assumption is that the volume of the unit is the only indicator. Other parameters such as manufacturing costs and material costs will not be regarded.

1.3 Methodology

As a starting point, it will be determined which criteria that need to be met by the proposed heat exchanger. For example, it will be stated which heat load that it should be capable of delivering at a certain outdoor temperature and what an acceptable noise level is. This is done by performing a heat pump market study in order to find one that is well performing from a noise perspective, and making this the reference heat pump from an energy performance standpoint as well. Afterwards, using relevant measurement data and literature on heat transfer and heat exchangers, the necessary size (height, width and depth) and air flow of the different heat exchangers will be calculated using Matlab, including the resulting noise level.
The heat exchangers that meet the criteria that were initially set will be compared to
each other from a simplified economic standpoint. As stated before, the assumption is
that the volume of the heat exchanger is the only indicator of which heat exchanger is
the least expensive. An analysis will be performed on parameters that have shown to
be of great importance of the final result.
2 Technical background information

The purpose of this chapter is to gather different crucial technical information needed to create sufficient understanding in areas that are relevant to this study. For instance, how an indirect heat pump system works is described, and which factors that cause noise generation is determined. The chapter also includes and describes a few assumptions that are made within these areas.

2.1 Indirect vs. direct heat pump systems

In this study, a direct heat pump system is what is referred to as a conventional system. This type of system is by far the most common among what is installed in residential buildings. Another system configuration, the one that this study focuses on, is the so called indirect heat pump system. Both of these types of systems and their differences are described in following subchapters.

2.1.1 Direct expanding systems

The conventional design of a heat pump for use in residential houses is the so called direct expanding system, where the refrigerant transports heat directly between the low-temperature medium to a high-temperature one (Thermodynamics, 2007). I.e. the system refrigerant undergoes direct expansion and heats water or air. The most common types of refrigerant, usually named working fluid, are different types of hydrofluorocarbon mixes. The main components of a direct expanding heat pump are seen in Figure 2.1.

![Figure 2.1 Schematics of a direct expanding heat pump system.](image-url)
Starting at the evaporator, the working fluid changes phase from liquid to gas through the evaporator by absorbing heat from the outdoor air and their by cooling the surrounding space. As the working fluid is phase changing in the evaporator the temperature is constant until it reaches gas state. After the evaporator, the compressor increases the pressure and temperature of the working fluid by electrical work input. The heat in the working fluid is transferred to the high-temperature side of the system by condensation from gas to liquid in the condenser unit. The working fluid is again changing phase, this time from gas to liquid. The pressure in the working fluid is then reduced by an expansion valve and lead back to the evaporator. At this point the cycle of the working fluid starts over. (Svenska Kyltekniska Föreningen, 2010)

2.1.2 Indirect systems

An indirect heat pump system has, instead of a direct expanding working fluid, one extra secondary circuit that absorbs heat from the low-temperature air side. The working fluid of the secondary loop shown in Figure 2.2 usually consists of water mixed with an anti-freezing agent, e.g. ethylene glycol. This mixture is commonly called brine. Two-phase liquid such as e.g. CO2 is also possible to use as heat transferring fluid. For the Scandinavian market of residential heat pumps, ethylene glycol is commonly added to a level so it can prevent freezing down to about -32 °C according to Thermia (2013). The brine circulating in the outdoor unit is not phase shifting like the hydrofluorocarbon in the indoor unit. The temperature levels are seen in Figure 2.3.

The evaporation temperature of the refrigerant in the indoor unit is constant, represented by the vertical line in the figure, as it goes from a liquid – vapor state to gas.

![Figure 2.2 Schematics of an indirect heat pump system.](image-url)
2.1.3 Advantages and drawbacks with indirect systems

When heating a house with a heat pump frost, depending on the surrounding temperature, builds up on the surface of the evaporator coil. According to Hrnjak (1997) the average surface temperature of the coil is higher in an indirect system which leads to less frost build up. The frost is also more uniformly distributed in an indirect system which allows for a greater fin density, that in turn allows for a larger heat transfer area confined in a smaller volume. Furthermore, the defrosting process, which can contribute to noise generation, is more efficient with a secondary fluid cycle than with a gas mix.

Another advantage with an indirect heat pump system for residential heating is that noise generating units as e.g. the compressor and the valve controlling the defrost cycles are placed indoors. This enables for easier and better noise isolation for these units. The only component to improve and modify on the outside of the resident is the air to brine heat exchanger and fan. I.e. there is a high flexibility of the system.

In a conventional, direct expanding, heat pump used for heating water there is a risk of freezing not only on the heat exchanger surface but also in the actual water system. In case of an e.g. power outage the water going to the condenser seen in Figure 2.1 may damage the flow pipes and the condenser unit as the water expands while freezing. In an indirect system the only affected liquid is the brine which can, by the ethylene glycol properties, withstand freezing down to very low outdoor temperatures.

Through personal communication with Ola Gustafsson, PhD student at Chalmers University of Technology, there are more advantages and drawbacks with indirect systems. Defrost technologies for indirect heat pump systems, can be more efficient and reduce disturbance and wear. As seen in Figure 2.2, a backup tank of hot brine can be used to defrost the outdoor unit. This results in that there is no need for a four
way valve to reverse the flow, which reduce chances for leakage as well as noise generation when the valve is operating.

However, there are some drawbacks with indirect systems. As seen Figure 2.2, there is a need for an extra heat exchanger between the brine and water, which will lead to temperature losses. This may also result in a higher total system cost. Furthermore, an extra circulation pump is needed for the brine cycle.

2.2 Sound

The motion or vibration of an object creates small pressure variations in the air around the static pressure of $10^5$ Pa, which, if large enough, the human ear perceives as sound. Sound levels are usually measured using the decibel scale, which is a logarithmic measure expressing the ratio of two sound pressures, intensities or powers.

Two different sounds at the same sound level are perceived differently, in terms of loudness, if the frequencies of the sounds are not the same. Loudness is a measure of the subjective impression of the magnitude of a sound. To measure loudness, an A-weighted filter is normally used so that the sound frequency is taken into account. The unit dBA indicates that such a filter is used, and although the correlation between dBA and loudness is approximate, the A-weighted level has become universally accepted as the simplest way of measuring noise that does give some correlation with human response. A 10 dBA increase is perceived as a doubling in loudness due to the logarithmic nature of the decibel scale. Smith (2011)

2.3 Noise generation in indirect heat pumps

In an indirect air-source heat pump system, the unit placed outdoors contains only a fan and a heat exchanger. Since this study concentrates solely on the noise generated outdoors, this subchapter describes which factors that cause the noise generated by such a unit, and how the noise level can be estimated.

The fan and the heat exchanger together generate noise. The purpose of using a fan is to generate a flow of air passing through the heat exchanger, creating forced convection, and thus increasing the heat transfer rate between the fluid and the air. This air flow through the heat exchanger induces an aero dynamical noise, in this case called direct noise, which depends on the heat exchanger design and the air velocity. There is also noise that is generated by the fan itself, which then can be called indirect noise. Preliminary unpublished studies made by SP Swedish Technical Research Institute have shown that when trying to reduce the overall noise level in a case like this, the reduction of the direct noise is much less of an issue compared to the reduction of the indirect noise generated by the fan.

The noise generation of a fan is dependent on the fan type, its design and the operating conditions. It is difficult to predict the noise level generated by a fan and the uncertainties are often large. A general rule is that a fan is quietest at its peak efficiency point. Performance curves of fans are often results of actual tests and can be used to find the peak efficiency point of a fan. According to ASHRAE (2009) Handbook, a simplified expression of the sound power level of a fan can be described using equation (2.1), with which the influence of the heat exchanger on the indirect
noise level can be evaluated. It shows that the sound power level depends on the fan’s own specific sound power level $K_W$, the air flow rate $Q_{air}$, the pressure $\Delta p$, the blade frequency increment $BFI$ and the efficiency correction $C_N$. ASHRAE (2009)

$$L_W = K_W + 10 \log Q_{air} + 20 \log(\Delta p) + BFI + C_N \quad (2.1)$$

Equation (2.1) provides the sound power level measured in dB, which is an inadequate indicator of how the sound is actually perceived by humans. In order to create an idea of how the noise is perceived, an A-weighted sound power level can be used, measured in dBA. One way of determining the A-weighted sound power level of an operating fan is to use its performance curve in which the fan manufacturer often has entered results from real sound measurements. The disadvantage of using this method is that it requires studying each particular case manually, which may become far too cumbersome and time consuming if many cases are to be compared. Also, the operating condition for which the fan manufacturer has performed sound measurements may very well not coincide closely enough with the operating conditions for which the sound power level is to be estimated in other cases. Another much less cumbersome method to use, if numerous cases need to be compared, is to theoretically apply an A-filter to the sound power level calculated using equation (2.1), thus providing a theoretical A-weighted sound power level. How to apply such filter is described in ASHRAE (2009), behind which the idea is that the perceived sound power level depends on the sound frequency. Table 2.1 shows how the filter is applied.

**Table 2.1 A-filter appliance for the different octave bands.**

<table>
<thead>
<tr>
<th>Octave band [Hz]</th>
<th>63</th>
<th>125</th>
<th>250</th>
<th>500</th>
<th>1000</th>
<th>2000</th>
<th>4000</th>
<th>8000</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K_W$ [dB]</td>
<td>51</td>
<td>48</td>
<td>49</td>
<td>47</td>
<td>45</td>
<td>45</td>
<td>43</td>
<td>31</td>
</tr>
<tr>
<td>$Q_{air}$ [dB]</td>
<td></td>
<td></td>
<td></td>
<td>10log$Q_{air}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Delta p$ [dB]</td>
<td>5</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$BFI$ [dB]</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$C_N$ [dB]</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>A-filter [dB]</td>
<td>-26.2</td>
<td>-16.1</td>
<td>-8.6</td>
<td>-3.2</td>
<td>0</td>
<td>1.2</td>
<td>1</td>
<td>-1.1</td>
</tr>
</tbody>
</table>

As can be read from Table 2.1, the noise is first divided into octave bands, i.e. eight different frequency intervals. Now, each octave band is assigned its own sound power level by using equation (2.1). The values of $K_W$ are taken from ASHRAE (2009) Handbook, where there are nominal values for axial propeller fans available. The efficiency correction is assumed to be equal to zero for each case and each octave band, thus also making the assumption that the fan being used is operating at peak efficiency. The A-filter is applied by adding the number of dB given in ASHRAE (2009) in each octave band. Then, the total sound power levels of all octave band are summed up, from which a single value is determined which describes the total A-weighted sound power level.
The values of $K_W$ in Table 2.1 are taken from ASHRAE (2009), but in this study they are slightly altered based on unpublished laboratory measurements made by SP Swedish Technical Research Institute. The somewhat different values that instead were used were derived from measurements of noise levels of fans in the same size and working range as fans in normal heat pumps. The simple reason for doing so is an attempt to acquire more accurate results. The new values are applied consistently in the study, meaning that using these values makes no difference when comparing case to case.

2.4 Psychrometrics

In calculations that in some way treat temperature change of air, consideration needs to be taken to air humidity. For instance, if the air is humid and its temperature decreases by passing through a heat exchanger, a portion of the heat transferred to the cold stream is latent and a portion is sensible. The latent portion is heat contained in the moisture in the air and will not be included if considering a change in dry bulb temperature only and a constant value of specific heat. Outdoor air in this study is considered humid, consideration therefore needs to be taken to both latent and sensible heat in order to obtain the correct heat transfer.

According to the standard testing conditions of air source heat pumps, described in Swedish Standards Institute (2011), the inlet air should have a wet bulb temperature of 6°C if the dry bulb temperature is 7°C. Given the two conditions, i.e. wet and dry bulb temperature, a complete knowledge of the state of the air can be obtained by using for example a Mollier diagram valid for atmospheric pressure. In the Mollier diagram in Figure 2.4, the state of the air when the inlet temperature is 7°C is indicated with a dot. In this study it is assumed that, as the air is cooled, the state changes along the arrow in the figure. The arrow first points vertically down to the saturation line where the relative humidity is 100%, and then follows the saturation line until the cooling stops. This means that the relative humidity of the air gradually increases until the temperature reaches the dew point, where after the humidity stays constant at 100% during the rest of the temperature decrease. The change in enthalpy between the inlet and outlet state, which can be observed using the Mollier diagram, will then include both latent and sensible heat, and can hence be used to determine the total heat transferred from the air to the fluid.
Another reason why it is important to take air humidity into account is the fact that the heat transfer rate between the air and the cold stream changes as water vapor in the air condensates on the cold heat transfer surfaces. This occurs since the heat transfer coefficient of the air side then changes, which leads to a changed overall heat transfer coefficient and therefore a changed heat transfer rate. According to Jacobi et al. (2005) and Jacobi and Xia (2005), the total heat transfer resistance under wet conditions can be expressed as shown in equation (2.2). What is introduced in this equation is a ratio between the total heat transfer rate $\dot{Q}_a$ and the sensible heat transfer rate $\dot{Q}_{a,s}$, as a factor that changes the resistance on the air side.

$$\frac{1}{(UA)_{tot}} = \frac{1}{\eta_{0,b} h_b A_b} + \frac{1}{\eta_{0,a} h_a (\dot{Q}_a / \dot{Q}_{a,s})} \quad (2.2)$$
3 Operating conditions and constraints

In order to find a suitable heat exchanger design, its operating conditions and a set of constraints must first be determined. A very important constraint is obviously which level of noise that is considered acceptable, and another is how large (length, height and width) the heat exchanger is allowed to be. It is also important to determine at which conditions the heat exchanger is operating, for example what the outdoor air temperature is. This chapter presents, explains and motivates all the different constraints and operating conditions that will be used when designing a suitable heat exchanger.

3.1 Level of noise

According to heat pump test results issued by the Swedish Energy Agency, the level of noise of 14 different air to water heat pumps, tested between 2010 and 2013, varies between 71 and 56 dBA. Since a purpose of this study is to find a design of a heat exchanger that allows for a low level of noise, the value of the noise level is aimed to be 56 dBA or lower. This is a soft target that should be held as low as possible so that it at the same time allows for a well overall performing system.

3.2 Outdoor air

The state of the outdoor air to be used in this study is set using the Swedish Standards Institute (2011) paper SS-EN 14511-2:2011 Table 12 - Air-to-water and air-to-brine units – Heating mode (Low temperatures). The outdoor air condition used in this study is the first point in the table, stating that the inlet dry bulb temperature is 7 ºC, the wet bulb temperature is 6 ºC, and the relative humidity is 86.66%. The reason for using this condition is that it is commonly used in standardized heat pump testing. More air conditions can be used, but only the one mentioned is considered in this study.

3.3 Brine properties

Just as it is necessary to decide at which outdoor air temperature the heat exchanger should operate, it is necessary to determine the temperature of the cold stream, i.e. the brine. The temperature difference between the hot and cold stream in a heat exchanger is a driving force for heat transfer, which is why the choice of temperature levels is of such importance. The state of the air at the inlet of the heat exchanger is accurately described by standards for testing heat pumps, however the state of the brine is not. Nevertheless, given the outdoor air temperature, and by making assumptions regarding e.g. minimum temperature differences in the heat exchangers in a reference heat pump running at these conditions, an estimate of expected brine temperature levels can be derived.

In order to estimate the brine temperature in an indirect heat pump, an approximate evaporation temperature $T_{r,i}$ of the refrigerant in a direct heat pump is first found. This is done partly by assuming that the minimum temperature difference $\Delta T_{min}$ between the streams is 5 K, and that the outlet air temperature $T_{a,o}$ is roughly 2.2 ºC.
as the inlet air temperature $T_{a,i}$ is 7.0 °C. The assumption regarding minimum
temperature difference is made after consulting Fredrik Karlsson, (researcher at SP)
and the air temperatures are assumed after having reviewed SP test measurements of a
heat pump comparable to the reference heat pump of this study. A third assumption
made is that the temperature of the refrigerant stream is constant, i.e. $T_{r,o} \approx T_{r,i}$. 
These assumptions lead to the conclusion that the evaporation temperature $T_{r,o}$ of the
refrigerant is approximately -2.8 °C, as shown in Figure 3.1, as the inlet air
temperature is 7.0 °C. For the efficiency of an indirect version of the direct reference
heat pump, it is now assumed that the evaporation temperature of the refrigerant is to
be the same in both types of heat pumps while running at identical conditions. The
additional heat exchanger needed between refrigerant and brine in the indirect version
has a minimum temperature difference of about 2 K, which again is an assumption
made after consulting Fredrik Karlsson about what can be expected from a fluid-to-
fluid heat exchanger in a heat pump.

Finally, the inlet brine temperature $T_{b,i}$, as the outdoor air temperature is 7.0 °C, can
be approximated to -0.8 °C as shown in Figure 3.2.

![Diagram 3.1](image1.png)

Figure 3.1 Figure describing inlet brine temperature for the reference heat pump.

![Diagram 3.2](image2.png)

Figure 3.2 Figure describing inlet brine temperature for an indirect heat pump.

In this study, the brine solution is assumed to sustain freezing down to -32 °C in
accordance with manufactured heat pumps for the Scandinavian market. In order to do
so, the solution is assumed to be 50:50 % (by volume) water to ethylene glycol
(MEGlobal, 2013). Data for the brine is taken from ASHRAE (2009).
3.4 Air flow

The air flow over a conventional heat exchanger for heating of residential buildings in the size of approximately 6-10 kW is about 2000 – 3500 m$^3$/h. (IVT, 2013) (Thermia, 2010) (Nibe, 2013) Theses direct heat pump systems often have a plate and tube design of the evaporator. Due to the intention of the study to test different designs, the value of the air flow is not constrained.

3.5 Fluid flow rate

According to E. Granryd (2007), the flow rate of the secondary loop fluid in an indirect system can be chosen rather freely. Larger brine flow rate results in a reduced temperature difference but acquires a higher work input for the pumping system and therefore reducing the total energy efficiency. Accordantly there are two system optima in a heat pump due the flow rate of the system. One giving maximum energy capacity and one resulting in minimum total energy input demand. However, changing the flow rate, and thereby the velocity in an already manufactured heat exchanger may result in a change from turbulent to laminar flow or vice versa. This can cause a major drop in the heat transfer capability if the heat exchanger is not designed for this new condition. In this study, a fluid mass flow rate of 1 kg/s will be tested and evaluated.

3.6 Fluid temperatures

The heat exchanger is investigated under heating mode while the inlet and outlet temperature of the water (at the heat pump condenser) is 30 °C and 35 °C respectively. This follows the SS-EN 14511-2:2011 standard for low temperatures. (Swedish Standards Institute 2011)

3.7 Dimensions

The permitted size of the outdoor unit is a difficult constraint to set since there are no standards or regulations as to how large it may be. Therefore, the dimensions of the outdoor unit of the heat pump with the lowest level of noise according to measurements made by the Swedish Energy Agency (a), the IVT Premium Line A Plus, are used as reference. This unit has a height of 152 cm, a width of 96 cm, and a depth of 115 cm. The heat pump with the smallest outdoor unit, but not lowest noise level, is the Invest Living LVE-09. This outdoor unit is also used for comparison and has a height of 70 cm, a width of 84 cm, and a depth of 32 cm.

The dimensions of the reference units do not have to be exactly matched, they are used mostly for the sake of comparison. If this study results in that the chosen heat exchanger and fan allow the outdoor unit of an indirect heat pump to be smaller, then that is considered an advantage. Hence, the dimensions of the outdoor unit are quite free to vary. An indirect constraining factor for the heat exchanger size, and thereby also the outdoor unit, may be that the fan must be large enough to supply enough surface of the heat exchanger with an air flow. For instance, a very small fan, in relation to the heat exchanger, would create an uneven airflow across the heat
exchanger heat transfer surface. For that reason, the necessary fan size may become an indirect constraint for the size of the outdoor unit.

3.8 Heat load

Between the year 2010 and 2013, 14 different heat pumps for residential heating were tested by the Swedish Energy Agency (a). The heat output, as the outdoor temperature was 7 °C and the water temperature output was 35 °C, varied between 7.6 - 11.2 kW. The unit with the lowest noise level according to the tests, IVT Premium Line A Plus, has an output of 9.4 at the air temperature of 7 °C, which are set as the desired output value of the condenser unit in this study. The COP-value at this point is 3.9.

3.9 Pump work

As an indirect system consists of an additional fluid pump, (seen in figure 2.2) to feed the heat exchanger that exchanges heat between the brine and the refrigerant, the pump work need to be kept as low as possible. If the pump work is too high, the overall efficiency of the heat pump will suffer. After consulting Caroline Haglund Stignor, the pump work was set to not exceed 100 W, as a level of limitation. The efficiency of the circulation pump is set to 25 % in accordance with the best preforming pump in the test carried out by the Swedish Energy Agency (b).
4 Heat exchanger types to be analyzed

Compact heat exchangers are commonly used to transfer heat between gas-to-gas and gas-to-liquid, and cover many different applications such as residential heating, refrigeration, food showcase and process industries. This study is regards heat transfer between liquid and gas. Two types of compact heat exchangers will be evaluated, one type with round tubes and continuous fins, and one with flat tubes and continuous fins.

The most common exchanger surface for modern residential heat pumps is the round tube with continuous fins, which can be seen in Figure 4.1. All of the heat pumps in the tests carried out by the Swedish Energy Agency (a) where configured in this way. Compared to a bare tube bank, this conventional design with circular tubes and continuous fins increases the heat transfer area. This is because the fins enable a second and larger heat transfer area. This is desirable in gas-to-liquid heat transfer applications as an optimum design tends to demand maximum heat transfer area according to Kays & London (1984).

![Figure 4.1 Schematics of a round tube heat exchanger design, d is the diameter for the tubes, T_pl is the longitudinal tube pitch and T_pt specifies the transversal tube pitch.](image)

The second evaluated heat exchanger type is the one with flat tube with continuous fins, seen in Figure 4.2. The tubes in these heat exchangers, in this study, are staggered.
One of the flat tube heat exchanger modeled in this study is equipped with wavy fins. The difference between wavy and plain fins is simply the wavy geometry which is intended to allow for a better mixture of the air and thus better heat transfer conditions.

Both heat exchanger types have a large number of fins, densely grouped together in order to increase the heat transfer area. The horizontal distance between the fins is called fin pitch and often given in number of fins per meter. The fin pitch is, especially in Nordic climate, an important parameter due to the risk of frost build up on the surface. As frost builds up on the heat exchanger surface, the heat transfer rate decreases. A small fin pitch will result in more frequent defrost cycles due to the fact that the air flow passage gets clogged more easily. The fin pitch of the evaluated round tube heat exchangers in this study is in line with the units manufactured for the Nordic market. The most common fin material for the residential heat pumps is aluminum. Dimensions for the modelled heat exchangers are seen in Appendix 1.

Another parameter is the number of passes that a heat exchangers has. It is simply how many times the fluid inside the tubes passes the heat exchanger coil. Figure 4.3 shows a heat exchanger seen from above, when the number of passes is four. As seen in the figure, the number of passes would be four as the fluid enters in the first row, turns in the u-bends, comes back in the second row, goes back into the third and finally exit into the fourth row. I.e. the number of passes in this study is equivalent with how many rows deep the heat exchanger is.
When referring to the number of circuits that any of the heat exchangers included in this study has, it basically describes the ratio between the number of rows that the heat exchanger is high, and the number of fluid inlets the unit has. For instance, if the heat exchanger has a fluid inlet on each row, the number of circuits is one. The number of circuits is increased by feeding the fluid to fewer inlets, for example to only half as many, thus forcing the fluid that enters an inlet to flow a longer distance. Figure 4.4 shows three examples where the number of circuits is one, two and three. The crossed circles represent tubes at which the fluid enters the heat exchanger. The fluid enters at an inlet and then always flows through all passes (see Figure 4.4). If the number of circuits is one, the fluid exits at the outlet after only four passes. If the number of circuits instead is more than one, the fluid will enter a new inlet after having exited at the outlet of the fourth pass.

Usually in heat exchangers with round tubes, a simple U-shaped bend is used to connect the passes to each other. In heat exchangers with flat tubes, the way the passes are connected is not as simple. Instead, manifolds are mounted on the sides of the heat exchanger, into which the fluid enters and then is distributed back to all tubes.

Using the heat exchanger in Figure 4.4 with three circuits as an example, the fluid would flow through four passes (since the unit four rows deep) and three rows, meaning a distance three times as long as the fluid would flow if the number of circuits instead were only one. A reason why this is done is that if the mass flow is kept constant, increasing the number of circuits will force the fluid to flow faster, thus affecting the heat transfer capacity on the fluid side. Having fewer inlets may also be preferable from a manufacturing point of view, although this is neglected in this study.
Figure 4.4 Schematic illustration of heat exchangers with different number of circuits.
5 Theory behind modelling of designs

In order to calculate the heat transfer rate $Q$ and pressure drop $Δp$ in a heat exchanger of a given type, geometry, flow rates and entry temperatures, and a number of steps are required. Using the P-NTU method, the heat transfer rate depends on the temperature effectiveness $P_1$ and $P_2$ of the heat exchanger according to equation (5.1)

$$Q = P_1C_1ΔT_{max} = P_2C_2ΔT_{max}$$  \hspace{1cm} (5.1)

where $C_1$ and $C_2$ is the heat capacity rate for the two fluids exchanging heat such as $C = \dot{m}c_p$. $ΔT_{max}$ is the maximum temperature difference, i.e. $ΔT_{max} = |T_{a,i} - T_{b,i}|$.

The temperature effectiveness $P_1$ is given in equation (5.2) from Shah and Sekulić (2003)

$$P_1 = \frac{\left(1 - R_1P_{1,p}\right)^n}{\left(1 - P_{1,p}\right)^n} - 1 \frac{1 - R_1P_{1,p}}{1 - P_{1,p}} - R_1$$  \hspace{1cm} (5.2)

where $n$ is the number of passes, $R_1$ is the heat capacity ratio and $P_{1,p}$ is the thermal effectiveness of each pass. The temperature effectiveness depends on the actual flow arrangement of the heat exchanger. In this study, all heat exchangers evaluated are of a cross-flow type and the numbers of passes are to be seen as identical in flow arrangement with identical individual NTU, which is further explained below.

The thermal effectiveness of each pass, $P_{1,p}$ is given by

$$P_{1,p} = ε_p \text{ if } C_1 < C_2$$  \hspace{1cm} (5.3)

else

$$P_{1,p} = ε_pC_r$$  \hspace{1cm} (5.4)

with the definition of

$$C_r = \frac{C_1}{C_2} \text{ if } C_1 < C_2$$  \hspace{1cm} (5.5)

else

$$C_r = \frac{C_2}{C_1}$$  \hspace{1cm} (5.6)

and

$$C_{min} = C_1 \text{ if } C_1 < C_2$$  \hspace{1cm} (5.7)

else

$$C_{min} = C_2$$  \hspace{1cm} (5.8)
The heat capacity rate $R_1$ is simply given by

$$R_1 = \frac{C_1}{C_2} \quad (5.9)$$

$\varepsilon_p$ introduced in equation (5.10) is the heat exchanger effectiveness from Incropera and DeWitt (2007)

$$\varepsilon_p = 1 - \exp \left[ \frac{1}{C_r} (NTU)^{0.22} \cdots \right] \left\{ \exp[-C_r(NTU)^{0.78}] - 1 \right\} \quad (5.10)$$

where $NTU$ is the number of transfer units. Equation (5.10) is valid for cross-flow, single pass and with both fluid unmixed. The fluid inside the tubes in a multiple-tube-row cross-flow exchanger is considered mixed at any cross section. However according to Shah and Seculic (2003) the fluid can be considered as unmixed as it is split and distributed between the tube rows. In practice a number of passes around four will give an unmixed characteristic. With less than four or five passes the fluid is partially unmixed or partially mixed. Because of the difficulties in interpreting exactly when Equation (5.10) is valid, it assumed to be valid for all number of passes in the range 2-12.

The number of transfer units, $NTU$, used in the equation (5.10) is given by Shah and Sekulic (2003) as

$$NTU = \frac{UA}{C_{min}} \quad (5.11)$$

where $U$ is the overall heat transfer coefficient. To determine the heat transfer area the surface area of all tubes and fins are calculated. The $U$-value is determined using equation (5.12) from Kays and London (1984)

$$\frac{1}{UA} = \frac{1}{\eta_{o,b} h_b A_B} + \frac{a}{(A_w/A_a)k} + \frac{1}{\eta_{o,a} h_a A_a \left( \frac{Q_b}{Q_{a,s}} \right)} \quad (5.12)$$

where the middle term, which represents the resistance for heat transfer through the tube wall, is neglected due to its very small contribution to the total resistance. $\eta_{o,a}$ and $\eta_{o,b}$ represent the overall surface effectiveness on the hot air and cold brine side respectively, $h_a$ and $h_b$ is the heat transfer coefficients. $\frac{Q_b}{Q_{a,s}}$ is the local sensible heat ratio.

As the brine side does not have any extended surface, $\eta_{o,b}$ is set to one. Equation (5.12) is therefore reduced to
\[
\frac{1}{UA} = \frac{1}{h_b A_b} + \frac{1}{n_{o,a} h_a A_a} \left( \frac{Q_b}{Q_{a,s}} \right) \]

(5.13)

The overall surface effectiveness on the air side \(\eta_{o,a}\), needs to be weighted. This is because the temperature gradient within the fins extending into the fluid is reducing the surface effectiveness. The surface effectiveness for the hot air side is given by the equation below form Kays and London.

\[
\eta_{o,a} = 1 - \frac{A_f}{A_t} (1 - \eta_f) \]

(5.14)

Where \(\eta_f\) is the fin efficiency given by equation (5.15)

\[
\eta_f = \frac{\tanh(ml)}{ml} \]

(5.15)

\(l\) is defined as half the wall spacing between the tubes, and \(m\) is given by

\[
m = \sqrt{\frac{2h_a}{k_f \delta}} \]

(5.16)

for thin sheets fins. \(k_f\) is the thermal conductivity of the fin material.

In accordance with Jacobi and Xia (2005) the local sensible heat ratio variation, correctly expressed as \(dQ_a/dQ_{a,s}\), is assumed to vary negligibly over the surface area and therefore equal to \(Q_b/Q_{a,s}\).

The air heat transfer coefficient is given by Kakaç, Liu and Pramanjaroenkij (2012) as

\[
h_a = \frac{j G_a c_{p,a}}{(Pr_a)^{\frac{2}{3}}} \]

(5.17)

where \(c_{p,a}\) is the specific heat capacity for air and \(Pr_a\) is the Prandtl’s number which is linear interpolated within the operating temperature range for the air side. \(j\) is the Colburn correction factor.

The Colburn correction factor \(j\) is given by data from Kays & London. For the heat exchangers with flat tubes with continuous fins table data from Kays & London where curve fitted through piecewise polynomial interpolation, so called spline, to get a small interpolation error in MATLAB. An example of this is to be seen in Figure 5.1. Graphical data for round tube with continuous fins where extracted by hand from figure 10.91 and 10.92 in Kays & London and again spline interpolated. This will give a somewhat larger error compared to table data, but is assumed to not affect the results noticeably. The Colburn factor is basically a modified Stanton number that account for variations in the fluids Prandtl number.

From the interpolated data, the \(j\) factor is a function of the Reynolds number on the air side.
where $D_h$ is the hydraulic diameter, $\mu$ the dynamic viscosity and $G$ is the mass velocity. Both equations from Kakaç, Liu and Pramuanjaroenkij.

$A_c$, used in equation (5.19), is the heat exchanger’s minimum free flow area and is determined according to the equation below.

$$A_c = \sigma A_{fr}$$  \hspace{1cm} (5.20)

where $\sigma$ is the free flow-frontal area ratio, which is readily available in Kays & London for each individual heat exchanger geometry. $A_{fr}$ is simply the frontal area, the area perpendicular to the air flow, formed by multiplying the heat exchanger’s height by its width.

![Graph](image)

**Figure 5.1 Example of the Colburn factor vs the Reynolds number for surface CF-7.34, table data from Kays and London spline interpolated in MATLAB.**

The specific heat capacity for the inside of the tubes, used in equation (5.13), depends on the geometry according to Incropera & DeWitt (2007)

$$h_b = \frac{Nu_a k}{D_h}$$  \hspace{1cm} (5.21)

Generally in literature, equations for flow inside ducts are for circular tube geometry. To adjust for rectangular geometry $D_h$ is defined, according to White, as
\[ D_h = \frac{4A}{\mathcal{P}} \]  

(5.22)

where \( \mathcal{P} \) is the wetted perimeter. This enables for the use of the same equations for the rectangular as with circular geometry.

The Nusselt number for laminar flow conditions inside the round tubes is taken from Gnielinski (1989) as

\[ Nu_{tf, round} = (3.66^3 + 0.7^3) + \left(1.615(x^*)^{\frac{1}{3}} - 0.7\right)^{\frac{1}{3}} \]  

(5.23)

where \( x^* \) is defined by the equation below

\[ x^* = \frac{L_{\text{tube}}}{D_h Re_b Pr_b} \]  

(5.24)

For turbulent flow conditions the Nusselt number inside the round tubes can be taken from two different correlations, Gnielinski (1989) and Dittus-Boelter.

The Gnielinski correlation

\[ Nu_{tf, round} = \left(\frac{f}{8}\right)(Re_b - 1000)Pr_r \]  

\[ \quad \left(1 + 12.7\sqrt{\left(\frac{f}{8}\right)\left(Pr_r^2 - 1\right)}\right) \]  

(5.25)

with \( f \) equal to

\[ f = (0.79 \ln Re_b - 1.64)^{-2} \]  

(5.26)

which is valid for \( Re_b > 2300 \).

The Dittus-Boelter correlation, quoted by Haglund Stignor (2009), is equal to

\[ Nu_{tf} = 0.023 (Re_b)^{0.8} (Pr_b)^{n} \]  

(5.27)

Gnielinski’s equation for Nusselt numbers for laminar flow is valid only for \( 50 < Re < 1700 \). For \( Re > 2300 \), equation (5.27) and (5.25) are found possible to use. In order to help make a decision on what to assume for the interval not covered by either equation, the equations are plotted for a range of Reynolds numbers. The curves for equation (5.23) and (5.25) intersect close to \( Re = 1500 \), relatively close to where the equation for laminar flow stops being valid, which can be seen in Figure 5.2. From the intersection of the curves and up, the curve for equation (5.25)is approximately linear. Hence, in order to avoid a sudden change in Nusselt number, it is therefore assumed that equation (5.23) is valid for \( Re \leq 1500 \) and equation (5.25) is valid for \( Re > 1500 \). Equation (5.27) is not used since it does not intersect as well with (5.23)where (5.23) stops being valid.
When calculating the liquid side pressure drop for laminar flow, the friction factor $f$ is determined using equation (5.30) according to Incorpera. According to Gnielinski (1989), equation (5.26) is to be used to calculate $f$ for turbulent flow, and is valid for $Re > 2300$. In order to avoid a sudden change in friction factor value, and to make consistent assumptions, it is assumed that the equation for laminar flow is valid for $Re < 1500$. In this case, there is no intersection at this point, why a perfectly linear equation is established stretching from the point where equation (5.30) stops being valid to where equation (5.26) starts being valid, i.e. at $Re = 2300$. For $Re > 2300$, the equation for turbulent flow is used. Both equations are plotted for a range of Reynolds numbers in Figure 5.3.
Figure 5.3 Friction factor vs. Reynolds number for Incorpera and Gnielinski correlation.

For the flat, rectangular tube geometry the Nusselt number is calculated by equation (5.28). The equation is constructed by linear interpolation from table data from Shah and London (1978) and is valid within a range of $40 < 1/x^* < 200$. In accordance with Haglund Stignor (2009), the curve fit is done for thermodynamically developing flows with assumed constant wall temperature.

$$Nu_{tf,flat} = 6.5276 + 0.02024 \left( \frac{1}{x^*} \right)$$  \hspace{1cm} (5.28)

The work input of the brine circulation pump during turbulent flow conditions results in rather high values. This is due to the resulting larger pressure drop, compared with laminar conditions, which will in turn lower the total energy efficiency of the heat pump. Therefore, in cases where turbulent flow is present inside the tubes the design is not desired and discarded.

To calculate the pressure drop on the fluid side equation number (5.29), given by White (2011), is used.

$$\Delta p = \rho \frac{v^2}{2} \left( f \frac{L_{tube}}{D_h} + Kn_{bends} \right)$$  \hspace{1cm} (5.29)

The friction factor $f$ for laminar flow conditions is equal to
\[ f = \frac{64}{Re_t} \]  

(5.30)

which is valid in the range for single phase flow, circular tube, and a Reynolds number of \( Re_t < 2300 \).

For turbulent flow conditions i.e. \( Re_t > 2300 \) equation (5.26) is valid.

The coefficient \( K \) describes resistance from different shapes such as e.g. valves, elbows and tees. It is often, in literature, correlated to the raw size of the pipe and not with the Reynolds numbers or roughness of the surface. Furthermore the value of \( K \) is often provided from different manufacturers in the literature, and reported for turbulent flow conditions. Different forge and molding techniques give somehow different loss coefficients and can therefore vary quite much for the same tube diameter. With this in mind, the uncertainty of the \( K \) value is rather high. (White)

Because of the uncertainties, the same \( K \) value is used for both types of heat exchangers.

In accordance with Haglund Stignor (2002) the \( K \)-value is set to 2.28 and multiplied with the numbers of bends, \( n_{bends} \).

Finally, to determine the air side pressure drop between the inlet and the outlet, equation (5.31) is used from Kakaç, Liu and Pramuanjaroenkij (2012).

\[
\Delta p = \frac{G_a^2}{2 \rho_i} \left( f \frac{A_t}{A_c} \frac{\rho_{i,a}}{\rho_{o,a}} + (1 + \alpha^2) \left( \frac{\rho_{i,a}}{\rho_{o,a}} - 1 \right) \right) \]  

(5.31)

\( \rho_{i,a} \) and \( \rho_{o,a} \) represent air density at the inlet and outlet respectively. \( f \) is the friction factor.

\[ \frac{A_t}{A_c} \] is correlated according to

\[
\frac{A_t}{A_c} = \frac{4 L_a}{D_h} \]  

(5.32)

\( L_a \) is the air flow length, i.e. the depth of the core.

\[
L_a = T_{p,l} (n_l - 1) + D \]  

(5.33)

The friction factor \( f \) is, as with the Colburn factor, extracted by using spline interpolation from table data for flat tubes with continuous fins. Again, graphical data were extracted by hand from the upper curves in figure 10-91 and 10-92 in Kays and London (1984).
6 Calculation method

All equations and correlations regarding for example heat transfer rate and noise levels, needed to determine the necessary size of a heat exchanger of a specific type, was presented in the previous chapter. What follows here is a description of the approach taken to determine a necessary heat exchanger size, explaining the way constraints, such as noise level and heat transfer rate, are taken into account.

The computer software Matlab was used as a tool to perform all necessary calculations and generate desirable results. The reason why Matlab was identified as a suitable tool is that it makes possible using the method of trial and error in a time efficient manner. The first step in the Matlab script design was naturally to enter all relevant equations and data for the type of heat exchanger to be evaluated. Secondly, it was selected which dimension of the heat exchanger to vary, i.e. either its frontal area or depth. At this point, the program first assumed a specific frontal area and a specific air flow. Knowing the exact geometry of the unit and the air flow, the heat transfer rate could be determined using the different correlations. In case it turned out that the resulting heat transfer rate was below the constraint, the air flow was increased by another ten m$^3$/h. Using this increased air flow, and if the heat transfer rate again turned out to be below the constraint, another ten m$^3$/h was added, and so on, until the sufficient heat transfer rate finally was reached. By this time, the necessary air flow had been determined for one specific frontal area of one specific heat exchanger type. Given the air flow and the resulting pressure drop, the noise level could be calculated.

The next step was to increase the frontal area, and repeat the same procedure as before to determine the necessary air flow and resulting noise level for the heat exchanger of slight larger size. As the targeted noise level was reached, the size increase would stop. At all times when varying the frontal area, both height and width were varied equally, meaning that a quadratic frontal area always was formed as can be seen in Figure 6.1. When varying the frontal area, the depth was held constant. Similarly, the frontal area was kept constant when the impact of a change in depth was studied. The same Matlab script, with only minor modifications, was applied for all heat exchanger types and for when the depth was varied instead of the frontal area.
Figure 6.1 Stepwise increase in frontal area.
Modelling results and parameter evaluations

After having modelled all four heat exchangers, results have been acquired that indicate the difference in suitability between them. This chapter first presents a comparison of all heat exchangers, with the purpose to highlight which single one that is superior to all others, letting small volume be the deciding factor. As previously explained, small volume is assumed to be related to low cost. The results are then analyzed and explained by comparing the different types, and finally an evaluation of parameters is made. The evaluation is made regarding only the best performing heat exchanger in order to attempt to further optimize its design.

7.1 Heat exchanger ranking

When determining which one of the four different modeled heat exchangers that is considered to be the best, the noise level and heat output requirements were set to equal values in all cases. More specifically, as a heat output of 7 kW was fulfilled by a heat exchanger, while causing no more or less than a noise level of 56 dBA, the necessary heat exchanger volume was noted. The methodology to reach this result is more accurately described in chapter 6.

When ranking the heat exchangers, the depth of each one is four rows, while the width and height are equal so that the frontal area is quadratic. The reason why a depth of four rows was chosen is that it is a common feature of heat exchangers in heat pumps. Figure 7.1 shows the necessary volumes of the different heat exchangers for when they all reached the same targeted noise level as well as heat output. In order to abbreviate the descriptions of the heat exchangers, the flat tube plain fin heat exchanger is called FFT1, the flat tube wavy fin is called FFT2, the round tube with the smaller tube diameter is called FCT1 and the fourth is called FCT2. It can be seen that FFT1 is the smallest, and for that reason, FFT1 is also presumably also the cheapest.

It is however not by much that FFT1 defeats FFT2. In fact, the difference in necessary volume between the two is so small that it may even be negligible. Why a difference can be seen at all is described later in this chapter. If now studying the two round tube heat exchangers in Figure 7.1, it is obvious that both need to be considerably larger than any of the flat tube heat exchangers. The necessary volume of FCT1 is even about twice that of FFT1, while FCT2 in turn needs to be about three times larger in volume than FCT1. It should be noted that the depth measured in millimeters is not the same for all heat exchangers, i.e. it is not only the frontal area that differs between them. It is true all heat exchangers are four rows deep, but since their tube geometries differ, their depths differ as well. All measurements, including the differences in depth, can be seen in Table 7.1. The reason why the numbers presented in the figure are that precise is that they are measurements directly based on number of rows. In a way, the calculations cannot be considered accurate enough to determine necessary height, width, and depth that exactly.
Figure 7.1 Necessary volume for the heat exchangers modeled.

Table 7.1 Result of the modeled heat exchangers that reach the targeted noise level.

<table>
<thead>
<tr>
<th>Heat exchanger</th>
<th>Height [mm]</th>
<th>Width [mm]</th>
<th>Depth [mm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flat tubes - FFT1</td>
<td>701</td>
<td>701</td>
<td>79</td>
</tr>
<tr>
<td>Flat tubes - FFT2</td>
<td>729</td>
<td>729</td>
<td>79</td>
</tr>
<tr>
<td>Round tubes - FCT1</td>
<td>1102</td>
<td>1102</td>
<td>76</td>
</tr>
<tr>
<td>Round tubes - FCT2</td>
<td>1263</td>
<td>1263</td>
<td>151</td>
</tr>
</tbody>
</table>

To summarize the ranking of the four different heat exchangers, FFT1 is decided to be considered the one that shows signs of being the most preferable one from a noise perspective. It is very closely followed by FFT2, but since there apparently is some difference, it is only FFT1 that will be analyzed further in chapter 7.2. Both round tube heat exchangers show signs of being considerably less preferable than any of the flat tube heat exchangers, especially FCT2. In depth explanations as to why there are differences in necessary volume between the heat exchanger types follow next.
7.1.1 Discussion - round tube vs. flat tube heat exchangers

When comparing the best performing heat exchanger with round tubes (FCT1) to the best performing with flat tubes (FFT1), it is evident that FFT1 is superior due to the fact that it is smaller, while still achieving sufficient heat transfer rate as well as causing a noise level of no more than 56 dBA. The difference in size is significant since FCT1 displaces more than twice the volume. The reason why this is the case, i.e. why FFT1 is more suitable from a noise perspective, partly has to do with the fact that the heat transfer resistance on the tube side of FFT1 is about half of the resistance on the tube side of the FCT1, as can be seen in Table 7.2. If the resistance on the tube side is low, the resistance on the outside does not need to be lowered as much by a high air flow, and thus the air pressure drop and noise level do not rise. The most contributing factor to why the tube side resistance for FFT1 is lower is that the tube side heat transfer resistance on the tube side of FFT1 is about half of the resistance on the tube side of the FCT1, as can be seen in Table 7.2. If the resistance on the tube side is low, the resistance on the outside does not need to be lowered as much by a high air flow, and thus the air pressure drop and noise level do not rise. The most contributing factor to why the tube side resistance for FFT1 is lower is that the tube side heat transfer coefficient is more than twice as high. Another contributing factor is the difference tube side heat transfer area, but Table 7.2 indicates that this difference is very little. The heat transfer coefficient differs between the two heat exchangers depending on the Nusselt number and hydraulic diameter of the inside of the tubes.

The Nusselt number differs only little, as can be seen in Table 7.2, but there is a significant difference in hydraulic diameter. A smaller hydraulic diameter is preferable to achieve a high heat transfer coefficient, thus the FFT1 has less heat transfer resistance on the tube side. Intuitively it makes sense that a flat tube has less resistance on the fluid side since more fluid is in contact with the tube walls than in a round tube. It may be tempting to draw the conclusion that the tube side heat transfer resistance for FCT1 can be lowered simply by decreasing the hydraulic diameter its tubes. However, doing so at the same time decreases the tube side heat transfer area, which causes the resistance to rise. Therefore, FFT1 has preferable heat transfer properties on the tube side, leading to less required air flow on the air side, and thus less noise generation. Nevertheless, it is important to stress the fact that Table 7.2 shows that the pump work on the tube side is significantly larger for FFT1. The pump work is however still below 100 W, which is assumed to be the level of limitation.

On the air side, there is a difference in heat transfer capacity as well. In fact, according to Kays and London (1984), the friction factor has a tendency to often be lower for FCT1. Also, the Colburn factor is often higher for FCT1. These are actually advantageous properties from a noise perspective, since they are synonymous with low pressure drop and heat transfer rate resistance. However, since the heat transfer resistance on the tube side is so much lower for FFT1, the advantageous properties on the air side that FCT1 possesses do not make big enough of a difference.
Table 7.2 Properties of FCT1 and FFT1.

<table>
<thead>
<tr>
<th></th>
<th>FCT1</th>
<th>FFT1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rows high</td>
<td>44</td>
<td>51</td>
</tr>
<tr>
<td>Rows deep</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Volume [m³]</td>
<td>0.093</td>
<td>0.039</td>
</tr>
<tr>
<td>Tube side heat transfer coeff. [W/K*m²]</td>
<td>357</td>
<td>756</td>
</tr>
<tr>
<td>Air side heat transfer coeff. [W/K*m²]</td>
<td>52</td>
<td>49</td>
</tr>
<tr>
<td>Nusselt number</td>
<td>9.5</td>
<td>8.2</td>
</tr>
<tr>
<td>Tube side heat transfer area [m²]</td>
<td>5.730</td>
<td>5.852</td>
</tr>
<tr>
<td>Tube side heat transfer resistance [K/W]</td>
<td>4.89*10⁻⁴</td>
<td>2.26*10⁻⁴</td>
</tr>
<tr>
<td>Air side heat transfer resistance [K/W]</td>
<td>1.30*10⁻⁴</td>
<td>3.13*10⁻⁴</td>
</tr>
<tr>
<td>Tube side pump work [W]</td>
<td>15</td>
<td>81</td>
</tr>
<tr>
<td>Tube hydraulic diameter [mm]</td>
<td>9.4</td>
<td>3.8</td>
</tr>
<tr>
<td>Friction factor</td>
<td>0.029</td>
<td>0.029</td>
</tr>
<tr>
<td>Colburn factor</td>
<td>0.011</td>
<td>0.009</td>
</tr>
<tr>
<td>Noise [dBA]</td>
<td>56</td>
<td>56</td>
</tr>
</tbody>
</table>

7.1.2 Discussion - round tube heat exchangers

If comparing the two circular tube heat exchangers by setting the frontal area, numbers of row deep, and desired heat transfer rate to the same in both cases, the resulting parameters such as air flow, pressure drop and noise level differ significantly. What follows here in an analysis of why that is the case.

The two round tube heat exchangers are quite different regarding geometrical parameters. For instance, the outside diameter of the tubes of FCT1 is 10.2 mm and 17.17 mm for FCT2. In order to set the frontal area of the two heat exchangers to the same number, they need to be 45 and 30 rows high, which can be seen in Table 7.3. This is done in order to more easily make comparisons. Because of the larger tube diameter, the heat transfer area is much larger for the FCT2 heat exchanger.
Table 7.3 Dimensions for finned circular tubes.

<table>
<thead>
<tr>
<th></th>
<th>FCT1</th>
<th>FCT2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tube diameter [m]</td>
<td>0.0102</td>
<td>0.017</td>
</tr>
<tr>
<td>Rows high [nr]</td>
<td>45</td>
<td>30</td>
</tr>
<tr>
<td>Rows deep [nr]</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Frontal Area [m$^2$]</td>
<td>1.272</td>
<td>1.259</td>
</tr>
<tr>
<td>Depth [m]</td>
<td>0.076</td>
<td>0.151</td>
</tr>
<tr>
<td>Air flow [m$^3$/h]</td>
<td>6500</td>
<td>9800</td>
</tr>
</tbody>
</table>

The Colburn factor for the FCT2 heat exchanger is smaller at all Reynolds numbers compared to FCT1 exchanger. This empirical relationship between Reynolds number and Colburn factor forces the airflow to be higher for the FCT2 heat exchanger in order to achieve a higher heat transfer coefficient. As the air flow increases, the Colburn factor declines but at the same time the mass flux increases, and at a stronger rate which results in a higher heat transfer coefficient.

As with the Colburn factor, the friction factor is lower at all Reynolds number for FCT2. The corresponding pressure drop for the air is anyhow larger for FCT2 as the mass flux is considerably larger and in square in the pressure drop equation (5.31), seen in chapter 5. As the two round tube heat exchangers have different geometrical outlines the total depth is not equal at the same row depth. The total depth of FCT2 is twice as deep as the FCT1, as seen in Table 7.3, due to the fact that the diameter of the tubes and the tube pitch are larger.

A deeper core increases the pressure drop as the contribution in the equation on the air side is a factor of four times the core depth divided by the hydraulic diameter, as seen in equation (5.32).

As the FCT2 heat exchanger has a deeper core, the total volume and heat transfer area is larger compared to FCT1. This is good in the view of heat transfer as the $UA$-value increases but at the cost of a higher pressure drop as stated above. The noise generation of the fan due to the operating conditions is highly dependent on the pressure drop as seen in equation (2.1), Chapter 2.3. I.e. the larger $UA$-value of the FCT2 is considered good for the heat transfer rate but makes the heat exchanger suffer a quite large noise penalty.

Another factor that highly contributes to the noise level is the air flow rate. As the Colburn factor for the FCT2 is lower compared to the FCT1, the air flow needs to be higher in order to enhance the mass velocity. In the same time, increasing air flow cause higher Reynolds number that lowers the Colburn factor.
7.1.3 Discussion - flat tube heat exchangers

When ranking the four heat exchangers, it was seen that the difference in necessary volume between the two flat tube heat exchangers was very little, possibly even negligible. However, a difference did exist and in the reason why is explained here.

The two flat tube heat exchangers calculated in the model only differ in fin geometry as FFT1 has plain fins while FFT2 has wavy fins. As when comparing the round tube heat exchangers, the Colburn factor for the two flat heat exchangers differs. FFT2 has higher Colburn factor value for the corresponding Reynolds value. This inherent property forces the air flow to be higher for the FFT1 with plain fins, seen in Table 7.4.

*Table 7.4 Dimensions for finned flat tubes.*

<table>
<thead>
<tr>
<th></th>
<th>FFT1-(2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tube dimensions [m]</td>
<td>0.0187x0.0025</td>
</tr>
<tr>
<td>Rows high [nr]</td>
<td>53</td>
</tr>
<tr>
<td>Rows deep [nr]</td>
<td>4</td>
</tr>
<tr>
<td>Frontal Area [m²]</td>
<td>0.531</td>
</tr>
<tr>
<td>Depth [m]</td>
<td>0.079</td>
</tr>
<tr>
<td>Air flow [m³/h]</td>
<td>4900 (4700)</td>
</tr>
</tbody>
</table>

A high air flow may intuitively signal that the noise level is higher, both since the noise level depends directly on the air flow and indirectly through the fact that the mass velocity \( G_a \), which is a component in the pressure drop equation, is higher. However, when comparing FFT1 with FFT2 is can be seen that the \( f \)-factor is lower for the plain FFT1. As the friction factor is lower the corresponding pressure drop is lower for FFT1.

The wavy fins of the FFT2 has the prerequisites for better heat transfer due to the larger heat transfer area and a larger Colburn factor for the corresponding Reynolds number. However, the lower \( f \)-factor for the FFT1 causing a lower pressure drop makes the heat exchanger a more preferable choice from a noise perspective.

7.2 Evaluation of design parameters

This chapter has the purpose to quantify and explain the impacts of changes in different important design parameters such as heat exchanger frontal area, depth, number of parallel circuits, and fluid mass flow. As previously described, it is the heat exchanger with flat tubes and plain fins that proved to have preferable properties, why only this heat exchanger is subject to all analysis in this chapter.
Figure 7.2 describes how the noise level depends on the frontal area of the heat exchanger. It intuitively makes sense that the noise level decreases as the frontal area increases, since the heat transfer area is increased, so that in turn less forced convection (i.e. air flow and resulting pressure drop) is needed to generate sufficient heat transfer rate. Also, as the area increases, the air velocity decreases, which is a contributing factor to pressure drop and hence also to noise level. The change in pump work due to the growth in frontal area is negligible.

![Graph showing noise level and air flow as a function of heat exchanger frontal area.](image)

*Figure 7.2 Noise level as a function of heat exchanger frontal area.*

The number of circuits is increased by feeding the fluid to fewer inlets on the heat exchanger, thus forcing the fluid that enters an inlet to flow a longer distance as long as the combined length of all tubes is kept unchanged. For example, when increasing the number of circuits from one to two, the fluid is fed to half as many inlets and therefore needs to flow twice the distance. Doing so has several effects on the fluid dynamics and the heat transfer capacity on the fluid side. As the number of circuits is increased and the fluid mass flow kept constant, the fluid velocity is forced to rise, which in turn causes the fluid’s Reynolds number to increase. This causes an increase in both fluid side pressure drop and Nusselt number. A direct effect of the change in pressure drop is that more work is required to be done by the fluid side circulation pump, and the effect of a larger Nusselt number is that the fluid side heat transfer resistance decreases. For this reason, there is a tradeoff between a high and a low number of circuits.

When in Figure 7.3 observing the necessary volume of the flat tube heat exchanger, it is apparent that less is needed the higher the number of circuits is. The reason why only one, two and three circuits are tested is the resulting large increase in pump work, which is presented in Figure 7.4. It is worth noticing that if the number of circuits is increased from one to two, or from two to three, the necessary heat exchanger volume is decreased by very little.
Figure 7.3 Necessary heat exchanger volume as a function of number of circuits, while frontal area is constant.

Figure 7.4 Required pump work as a function of number of circuits, while frontal area is constant.
Figure 7.5 shows, as expected, how the fluid’s Reynolds number grows as the number of circuits increases. This in turn leads to a higher heat transfer coefficient on the fluid side.

![Graph showing fluid's Reynolds number as a function of number of circuits, while frontal area is constant.](image)

**Figure 7.5 Fluid's Reynolds number volume as a function of number of circuits, while frontal area is constant.**

As can be seen in Figure 7.6 where the heat transfer resistances on the fluid side and air side, as well as their sum are presented, the resistance on the fluid side has a tendency to be lower than the resistance on the air side. This is the explanation to why the necessary size does not decrease as significantly for the flat tube heat exchanger, as the number of circuits is increased. The preferable measure to take is to decrease the highest resistance, which happens to be the opposite of what occurs in this case. Increasing the number of circuits does however bring some effect, but at a large expense of pump work as can be seen in Figure 7.4 above. If assuming that the pump work should be kept below 100 W, in order for the pump not to be a significant contributing factor to large energy consumption, the only viable choice is to have one single circuit.
When studying the effects of increasing the depth of the heat exchanger, it becomes apparent that a minimum in noise generation occurs at a certain depth. This occurrence is shown in Figure 7.7, which indicates that the noise level is lowest when the heat exchanger is around six rows deep. The reason why this happens naturally has to do with air flow and pressure drop. Figure 7.8 shows both the air flow and pressure drop, while Figure 7.9 shows the heat transfer resistances on both sides of the heat exchanger. Together, these two figures help explain the occurrence of a minimum in noise level.

When studying Figure 7.9, it is evident that the resistance on the tube side is significantly larger than that on the air side when the heat exchanger is only a couple of rows deep. The resistance on the tube side is high when the depth is low due to the fact that the tube side area is small. Hence, the air side resistance needs to be much lower in order for sufficient heat transfer rate to be reached between the streams. This is achieved by increasing air flow, directly causing a high pressure drop and noise level. As the tube side heat transfer area increases when increasing depth, the tube side resistance therefore decreases. Consequently, the air flow is allowed to decrease, thereby also causing a decrease in air pressure drop. From this point and on, i.e. when the number of rows depth wise is three or larger, the resistance on the air side is constantly higher than that on the tube side and both resistances decrease steadily.

This may lead to the conclusion that the pressure drop decreases similarly, however the pressure drop also depends directly on the core depth, as described in chapter five. Therefore, as the rate with which the decrease in resistances has stabilized, the effect of the direct relationship between pressure drop and core depth starts showing, explaining the stable increase in air pressure drop to the right of the minimum.

\[ K/W \]

\[ Fluid \ side \ heat \ transfer \ resistance \]

\[ Air \ side \ heat \ transfer \ resistance \]

\[ 1/UA \]

Figure 7.6 Heat transfer resistances volume as a function of number of circuits, while frontal area is constant.
Figure 7.7 Noise level as a function of number of rows deep, while frontal area is constant.

Figure 7.8 Pressure drop and required air flow as a function of number of rows deep, while frontal area is constant.
Increasing the depth of a heat exchanger also increases the length of the tubes through which the fluid flows, and an increase in tube length is synonymous with an increase in pressure drop on the fluid side, as described by equations in chapter five. Figure 7.10 shows a seemingly linear relationship between the required pump work due to fluid pressure drop and the number of rows deep the heat exchanger is. According to the assumption that a pump work of above 100 W is unacceptable, the number of rows is not allowed to be more than four. Choosing four rows, according to Figure 7.7, fortunately coincides relatively well with the minimum in noise level. Should the pump work be allowed to be as much as 125 W, the heat exchanger could be as deep as six rows, which is as close as possible to the minimum in noise generation. In that case the noise level would be close to 1 dBA lower compared to when the depth is four rows.

**Figure 7.9 Heat transfer resistances on tube and air side.**
The mass flow of brine has in each model consistently been kept at 1 kg/s. This may however not necessarily be the case, and for that reason it is shown in Figure 7.11 what the impact on noise level is if the mass flow is changed. The figure shows that it makes a significant difference in noise level what the mass flow is set to be. In fact, as a result of the reduction in heat transfer resistance on the fluid side as a consequence of a higher mass flow, the noise level can be reduced about 2 dBA if the mass flow is increased from 1 to 1.5 kg/s. An even larger difference in noise level is seen when comparing a case where the mass flow is 0.5 and the case where it is 1 kg/s, as can be observed in Figure 7.11. However, increasing the fluid mass flow has a significant impact on the required pump work, evident in Figure 7.12. To stay below 100 W of pump work, choosing a mass flow of 1 kg/s appears to be a suitable decision.
Figure 7.11 Noise level as a function of fluid mass flow.

Figure 7.12 Required pump work as a function of fluid mass flow.
7.3 Contingency analysis

The results of this study are based on a number of assumptions, meaning that there is good chance of a different outcome of the heat exchanger modeling if the assumptions were to be made differently. A selection of two assumptions has been made and will be subject to analysis in order to determine their impact on the results. One is the way the inlet temperature of brine is determined, and the other is the way the noise level is theoretically calculated. These two were chosen since they were suspected of having a large impact on the results.

In the chapter where it is described how to theoretically calculate the noise level, it is mentioned that a number of so called $K_W$ values given in ASHRAE (2009) are swapped for values that have been found in unpublished laboratory measurements. The numbers given in ASHRAE (2009) are higher than the numbers that were used to replace them, why if using the numbers given in ASHRAE (2009), the calculated noise levels would have a tendency to be higher. For this reason, all modeled heat exchangers would need to be larger, since air flow and pressure drop would need to be lower in order for the noise level not to exceed the limit of 56 dBA. The same $K_W$ values were used in all cases, and for that reason it makes no difference when ranking the four heat exchangers which $K_W$ values are used. However, in absolute values it does make a difference which $K_W$ values that are chosen. If running the model and instead using the values of ASHRAE (2009), the necessary volume of the FFT1 heat exchanger is around 0.06 m$^3$, which is actually about 40% to 50% larger than the volume presented in the result. The $K_W$ values taken from the laboratory tests are seen as better valid for the working range and for the specific application, thus using these is assumed to give the more accurate result.

As stated in chapter 3.3, assumptions were made in order to determine the inlet temperature of the brine that needed to be used in the model. One of the assumptions was the minimum temperature difference between the air and refrigerant in the reference heat exchanger that affects the brine inlet temperature. If the inlet brine temperature would be assumed to be higher, the resulting necessary heat exchanger volume would be larger. Similarly, if the inlet temperature would be assumed to be lower, the resulting necessary volume would be smaller. The early assumptions about brine temperature therefore impact the results of the heat exchanger ranking. All four heat exchangers are however modeled under the same assumption, which mitigates the effects of the inlet brine temperature when determining which one considered to be the best. To give an idea of how large the difference would be in absolute numbers, if the inlet brine temperature was set 1 °C higher, the resulting volume was about 20 % larger for the FFT1 heat exchanger. If the inlet temperature was set 1 °C lower, the resulting volume was about 13 % smaller for FFT1.
8 Conclusions

This chapter contains a list of conclusions drawn from having made this study. The list contains only brief statements, and more in depth motivations and explanations are found in previous chapters.

- From a noise perspective, the two heat exchangers with flat tubes are significantly more preferable than both heat exchangers with round tubes, since they do not need to be as large in size, and therefore are assumed to also be less expensive. More specifically, the two flat tube heat exchangers can, at a lower cost, be used to achieve the same heat transfer rate while still not generating more noise than any of the round tube heat exchangers.

- Out of the two heat exchangers with flat tubes, the one with plain fins is preferable from a noise perspective. Wavy fins increase the heat transfer rate, but at the expense of noise generation. Thus, plain fins are preferable if low noise and small size is desired. However, the difference it makes using one type of fin geometry or the other is relatively small and in fact possibly negligible.

- If keeping all dimensions except frontal area of the heat exchanger with flat tubes and plain fins constant, the noise generation decreases noticeably and steadily as a function of increase in frontal area. If the heat exchanger is 4 rows deep, the noise level is expected to decrease by about 1 dBA per every 0.017 m² that is added to the frontal area. In order not to exceed a noise level of 56 dBA, the frontal area needs to be at least 0.49 m².

- As for the heat exchanger with flat tubes and plain fins, in order not to exceed the limit of 100 W of required pump work on the fluid side, the number of circuits should not be more than one. Increasing the number of circuits has only minor positive effects from a noise perspective, however happens at a large expense of required pump work on the fluid side.

- When analyzing the impact on noise generation as a function of using a heat exchanger with flat tubes and plain fins that is two to twelve rows deep, there is a minimum in noise generation at around four rows. Hence, having fewer or more rows than four is not preferable from a noise perspective.

- If the fluid flowing through the heat exchanger with flat tubes and plain fins is kept at a mass flow of 1 kg/s, the fluid pump work is kept below 100 W. If the mass flow is increased by 50 %, the noise level is expected to decrease noticeably, but at a large expense of pump work. Decreasing the mass flow with 50 % will decrease the pump work, but also significantly increase the noise level. For that reason, a mass flow of 1 kg/s is concluded to be suitable.

Taking all conclusions above into consideration, it can be concluded that, out of the four different heat exchangers tested, it is the one with flat tubes and plain fins that is preferable given all the conditions. The unit should be 44 rows high (701 mm), 4 rows deep (79 mm), have a width of 701 mm, one circuit, and be fed with a mass flow of brine of 1 kg/s.
9 Recommendations for further studies

To further evaluate flat and round tube heat exchangers for indirect heat pump systems, one parameter to elaborate is the outdoor air condition. As in the paper Swedish Standards Institute (2011) there are other standardized temperatures to test and evaluate. A higher number of test points, and thereby results, would be useful to the depth of the study.

As the investigated heat exchangers are parts in a larger heat pump system, constructed for the residential building market, an in-depth price investigation would give a more complete picture of the possibilities to implement flat tube heat exchangers. Parameters to be investigated would for example be development and manufacturing cost for each different design.

Furthermore to validate the results, laboratory measurements can be carried out and compared to the computer modeled outcome.
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Swedish Energy Agency (b), *Cirkulationspumpar* (In Swedish) (Circulation pumps) Available at: http://www.energimyndigheten.se/Hushall/Testerresultat/Testresultat/Cirkulationspumpar/?tab=2 [Accessed 1th of July 2013].


Appendix

Heat exchanger geometry

**Fixed, heat exchanger specific, geometry from Kays & London (1984):**

**FCT1. Surface 8.0 – 3/8T:**
- Tube outside diameter: $D_O = 10.2\ mm$
- Tube inside diameter: $D_i = 6.2\ mm$
- Hydraulic diameter: $4r_h = 3.6\ mm$
- Transversal tube pitch: $T_{pt} = 25.4\ mm$
- Longitudinal tube pitch: $T_{ptl} = 22\ mm$
- Fin pitch: $p_f = 3.2\ mm$
- Fin thickness: $d_{fin} = 0.3\ mm$
- Free flow area/frontal area-ratio: $\sigma = 0.534$
- Wall thickness: $w_t = 0.4\ mm$

**Fixed, heat exchanger specific, geometry from Kays & London (1984):**

**FCT2. Surface 7.75 – 5/8T:**
- Tube outside diameter: $D_O = 17.2\ mm$
- Tube inside diameter: $D_i = 16.4\ mm$
- Hydraulic diameter: $4r_h = 3.5\ mm$
- Longitudinal tube pitch: $T_{pt} = 44.5\ mm$
- Transversal tube pitch: $T_{ptl} = 38.1\ mm$
- Fin pitch: $p_f = 3.2\ mm$
- Fin thickness: $d_{fin} = 0.40\ mm$
- Free flow area/frontal area-ratio: $\sigma = 0.481$
- Wall thickness: $w_t = 0.4\ mm$
Fixed, heat exchanger specific, geometry from Kays & London (1984):

FFT1. Surface 9.1 – 0.737-S
Tube height: \( a = 2.5 \text{ mm} \)
Tube length: \( b = 20 \text{ mm} \)
Hydraulic diameter: \( 4r_h = 4.2 \text{ mm} \)
Transversal tube pitch: \( T_{pt} = 11.4 \text{ mm} \)
Longitudinal tube spacing: \( T_{pl} = 15.2 \text{ mm} \)
Fin pitch: \( p_f = 2.8 \text{ mm} \)
Fin thickness: \( d_{fin} = 0.10 \text{ mm} \)
Free flow area/frontal area-ratio: \( \sigma = 0.788 \)
Wall thickness: \( w_t = 0.2 \text{ mm} \)

Fixed, heat exchanger specific, geometry from Kays & London (1984):

FFT2. Surface 9.29 – 0.737-SR
Tube height: \( a = 2.5 \text{ mm} \)
Tube length: \( b = 20 \text{ mm} \)
Hydraulic diameter: \( 4r_h = 4.1 \text{ mm} \)
Transversal tube pitch: \( T_{pt} = 11.4 \text{ mm} \)
Longitudinal tube spacing: \( T_{pl} = 15.2 \text{ mm} \)
Fin pitch: \( p_f = 2.7 \text{ mm} \)
Fin thickness: \( d_{fin} = 0.1 \text{ mm} \)
Free flow area/frontal area-ratio: \( \sigma = 0.788 \)
Wall thickness: \( w_t = 0.2 \text{ mm} \)