Parameter Identification of a Permanent Magnet Synchronous Motor

Master’s Thesis in Systems, Control & Mechatronics

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To my family Kerstin, Ulf, Sarah, Gustav, Jonathan and Marita
ABSTRACT

In this thesis, two identification methods for time varying electrical permanent magnet synchronous motor (PMSM) parameters are studied and compared. The Recursive Least Square (RLS) with forgetting factor and the Normalized Projection Algorithm (NPA) are applied to a salient PMSM model in $dq$-coordinates. The stator resistance and the stator inductances are identified both online and offline. The simulation results illustrate the efficiency of the two methods. It is shown that both algorithms are capable to identify the parameters both online and offline, but compared to the NPA, the RLS tracks the parameter variations much better.

Computational time per iteration is also estimated and it is shown that the NPA is approximately three times faster than the RLS.

By experimental verification from real motor data it is shown that the algorithms do not convergence to the same parameter values.

The stator resistance and the stator inductances have also been measured directly on the motor windings and compared with the identified parameter values from the algorithms. It is shown that they deviate more than expected. Analysis of the obtained estimates indicates that the parameter values could have been fitted to some disturbance in the measured motor currents and/or that the applied voltages to the motor deviate from the reference voltages used as input to the algorithms.
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Chapter 1

Introduction

In this chapter, a motivation for parameter identification in permanent magnet synchronous motor drives is given. The concept of offline and online parameter identification in motor drives is introduced and a brief overview of different methods found in the literature is presented. The focus is put on parameter identification methods useful for motor control. The outline of the thesis, as well as scientific contributions, are also presented.

1.1 Motivation of Parameter Identification in Permanent Magnet Synchronous Motor Drives

A permanent magnet synchronous motor (PMSM) is frequently used in the industry due to its high efficiency and quick mechanical dynamics. To design high performance control systems it is important to have accurate knowledge about the motor parameters. The data sheet, containing the motor parameters, that comes from the manufacturer of an electrical motor is not always
available, and when a new PMSM should be installed in an application, it is therefore desirable to be able to identify the parameters automatically with parameter identification. This is also more time efficient compared to manually changing the parameter values. Even when the data sheet is available, it does not usually take into account that some parameters tend to vary during different operation points. Classical motor control techniques such as Vector Control (see Chapter 3) require a position sensor to control the PMSM, and in such case the parameter information from the data sheet is normally sufficient. But since a sensor brings high cost and sometimes low reliability, it is desirable to remove the sensor [18] which will require more advanced control techniques. Many position sensorless control methods are reliable on an accurate motor model and by introducing online parameter identification in such drive systems, it is possible to improve the control performance (see section 1.3 for explanation of the concept online parameter identification).

1.2 Offline Parameter Identification

Techniques for determine motor parameters in standstill or in rotation without any load are called "offline parameter identification methods". The offline methods can further be categorized in self-commission and commission [1]. In self-commission all required motor parameters suitable for control are determined without any previous knowledge about the parameter values. In commission some previous information about the parameter values is known.
1.3 Online Parameter Identification

The techniques that adapt the motor parameters during the drive operations are called "online parameter identification methods"\[1\]. Many online identification algorithms with different nature have been proposed in earlier literature and they can be categorized in four groups:

**Spectral Analysis**

In spectral analysis techniques the motor parameters are determined from a measured response from a deliberate injection test signal or an existing characteristic harmonic in the voltage/current spectrum \[1\]. The stator current and/or voltage are sampled and analysed with spectral analysis and the motor parameters are then derived.

**Observer Based System**

The well known Extended Kalman Filter (EKF) can be used as an observer for online parameter identification of a PMSM and is especially suitable in a noisy environment. Other observers can also be used but the most frequently used observers today seem to be based on the Kalman Filter. The full order EKF is sometimes replaced by a reduced order system due to the fact the the full order version is very computationally demanding \[1\]. The Recursive Least Square (RLS) algorithm that we are going to discuss in detail in Chapter 5 is a special case of the Kalman Filter.
Model Reference Adaptive System

This method is based on principles of model reference adaptive control. The Model reference adaptive system (MRAS) techniques are relatively simple to implement and are not as computationally demanding as other methods. Because of this the MRAS has attracted the most attention in the literature [1]. The principle is built on the fact that some quantities can be calculated in two ways. The first are calculated from a model and the others from measured signals. A few parameters are assumed to be known in the model and the difference between the quantities calculated from the model and the measured ones is assigned to the parameter errors from the unknown parameters in the model. The errors in the output signals are then used to drive an adaptive mechanism that provides a correction of the unknown parameters. Figure 1.1 illustrates a plant and control system in MRAS based identification of PMSM parameters. The drawback is that the method is only suitable in stationary operation where the other parameters that are not going to be adapted can be assumed to have constant known values. The method does not work well in standstill and with low torque. In [2], a MRAS based method is proposed for online identification of PMSM parameters. Online estimation of the rotor resistance with MRAS is successfully applied to a sensorless control algorithm in [3]. A comparison between the MRAS and EKF is treated in [4, 5, 6]. The conclusion from those papers is that a MARS method using decoupling of the stator currents has the best characteristics and the executing time is also much shorter compared to the EKF.
Other Methods

There are a number of other methods for identification of PMSM parameters and many of them come from the field of artificial intelligence (AI). In MRAS the adapting mechanism is mostly linear and for parameter identification in a non-linear system neural networks (NN) have shown to give good results. A MRAS algorithm using NN in the adaptation mechanism is proposed in [7]. Another paper that proposes a NN based algorithm is [8]. Particle swarm optimization based parameter identification applied to PMSM is proposed in [9] and a fuzzy hybrid swarm optimization algorithm is presented in [10].

1.4 Outline of Thesis

In this thesis, two identification methods for time varying electrical permanent magnet synchronous motor (PMSM) parameters are studied and compared. The RLS with forgetting factor and the Normalized Projection
Algorithm (NPA) are applied to a salient PMSM model in $dq$-coordinates. The stator resistance and the stator inductances are identified both online and offline.

In the second chapter, mathematical modelling of PMSMs for control purposes is derived for both salient and non salient PMSMs. The idea is to describe the salient model, derived from the non model, of the motor that is used in the parameter identification algorithms in the following chapters. In order to give the reader some crucial background knowledge, this chapter starts with introducing the concept of three phase systems and space vectors.

In the third chapter, the concept of vector control within motor drives is introduced. The intention is to give an overview of the PMSM control system used in this thesis, as well as present applications of online parameter identification within vector control.

In Chapter 4, the non salient model is discretized and transformed into a linear regression model. This makes the model suitable for standard parameter identification algorithms.

The fifth chapter presents and derives the two algorithms used later in the thesis to estimate the motor parameters, namely the RLS with forgetting factor and the NPA. The intention is not only to present the algorithms, but also give the reader some background knowledge of how the algorithms can be derived.

The sixth chapter concerns simulations of the RLS with forgetting factor and the NPA used for estimations of the motor parameters. First, the simulation procedure is described and then the results from the simulations are presented.

In order to further verify the performance of the proposed identification methods, in Chapter 7, recorded data from a testbed PMSM drive sys-
tem similar to the simulation set-up in Chapter 5 have been used in MATLAB/SIMULINK together with the algorithms. A complexity analysis of the RLS with forgetting factor and the NPA have also been done to investigate if the algorithms are suitable for implementation in existing DSP:s at Aros electronics AB.

In the last chapter, the conclusions from the thesis are presented, and some future work is suggested.

1.5 Contributions

The main scientific contribution in the thesis, is in the comparison of the parameter identification algorithms RLS with forgetting factor and the NPA within PMSM drives. The general properties of the RLS and the NPA are well treated and compared in [11]. The RLS with forgetting factor for identification of synchronous reluctance motor parameters is proposed in [12, 13, 14]. In this thesis, the RLS with forgetting factor is compared with the NPA for tracing electrical PMSM parameters both online and offline.
Chapter 2

Modelling of Permanent Magnet Synchronous Motors

In this chapter, mathematical modelling of PMSMs for control purposes is derived for both salient and non salient PMSMs. The idea is to describe the salient model, derived from the non salient model, of the motor that is used in the parameter identification algorithms in the following chapters. In order to give the reader some crucial background knowledge, this chapter starts with introducing the concept of three phase systems and space vectors.

2.1 Three Phase Systems

Three phase systems are very common for powering electronic motors [15]. The basic idea is to use three sinusoidal AC voltages separated by 120° for each phase [16]. Figure 2.1 shows the phase currents of an ideal three phase system. For an ideal symmetric system the sum of the instantaneous values are zero and the power is constant. The three phase currents have the
2.2 Space Vectors

It is possible to describe the phase currents by introducing a space vector. The coordinate system for the space vector is called $\alpha\beta$ coordinates [15] . The relation between the three phase currents and space vector is as follows:

$$i_s(t) = i_{sa}(t) + ji_{sb}(t) = \frac{2}{3}[i_{sa}(t) + i_{ab}(t)e^{j\gamma} + i_{sc}(t)e^{j2\gamma}] \quad \text{with} \quad \gamma = \frac{2\pi}{3}$$

(2.2)

Figure 2.2 illustrates how this is done. Now we have a complex vector circulating with the stator frequency $\omega_s$ that is a projection of the three physical
Figure 2.2: Construction of a current space vector.

phase currents. Other three phase quantities are obtained in a similar way by introducing space vectors. The space vector can equally be represented on matrix form as:

\[
\begin{bmatrix}
i_{sa}(t) \\
i_{sb}(t) \\
i_{sc}(t)
\end{bmatrix} =
\begin{bmatrix}
\frac{2}{3} & -\frac{1}{3} & -\frac{1}{3} \\
0 & \frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{3}} \\
\end{bmatrix}
\begin{bmatrix}
i_{s\alpha}(t) \\
i_{s\beta}(t) \\
\end{bmatrix}
\]

(2.3)

The backward transformation from the space vector to the three phase quantities is given by:

\[
\begin{bmatrix}
i_{sa}(t) \\
i_{sb}(t) \\
i_{sc}(t)
\end{bmatrix} =
\begin{bmatrix}
\frac{2}{3} & -\frac{1}{3} & -\frac{1}{3} \\
0 & \frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{3}} \\
\end{bmatrix}
\begin{bmatrix}
i_{s\alpha}(t) \\
i_{s\beta}(t) \\
\end{bmatrix}
\]
2.2 Space Vectors

\[
\begin{bmatrix}
i_{sa}(t) \\
i_{sb}(t) \\
i_{sc}(t)
\end{bmatrix}
= \begin{bmatrix}
1 & 0 \\
-\frac{1}{2} & \frac{\sqrt{3}}{2} \\
-\frac{1}{2} & -\frac{\sqrt{3}}{2}
\end{bmatrix}
\begin{bmatrix}
i_{sa}(t) \\
i_{sb}(t)
\end{bmatrix}, \quad (2.4)
\]

If we have a symmetric three phase system with the currents as

\[
\begin{bmatrix}
i_{sa}(t) \\
i_{sb}(t) \\
i_{sc}(t)
\end{bmatrix}
= \begin{bmatrix}
\hat{I}_s \cos(\omega_s t + \phi) \\
\hat{I}_s \cos(\omega_s t - 2\pi/3 + \phi) \\
\hat{I}_s \cos(\omega_s t - 4\pi/3 + \phi)
\end{bmatrix}, \quad (2.5)
\]

the space vector will then be

\[
I_s = \hat{I}_s e^{j\omega_s t + \phi} \quad (2.6)
\]

which corresponds to a rotating phasor aligned with phase \(a\).

When it comes to control the speed and torque in a PMSM drive system, the three phase motor currents need to be controlled somehow with the help of the three phase voltages fed to the PMSM. By projecting the three phase voltages and currents into space vectors, and then introducing a new rotating coordinate system called \(dq\) coordinates [16], rotating with the stator frequency \(\omega_s\), the quantities will not be seen to rotate at all. The three phase currents and voltages transformed into \(dq\) coordinates can be seen as DC components in steady state.
With

\[ \theta_s = \int_0^t \omega_s dt \]  

(2.7)

the equation for the \( dq \) transformation is given by

\[ i_s = e^{-j\theta(t)} i_s^q = i_{sq}(t) + j i_{sq}(t) \]  

(2.8)

and the reverse transformation back to \( \alpha\beta \) coordinates is then

\[ i_s^q = e^{j\theta(t)} i_s = i_{s\alpha}(t) + j i_{s\beta}(t). \]  

(2.9)

It is not always possible to use complex space vectors when it comes to digital implementation of the control algorithms (and also when modelling a salient PMSM as we will do later on). The corresponding real valued vector to \( i_s^q \) is donated as \( i_s^a \) and we have the following equality:

\[ i_s^a = i_{s\alpha}(t) + j i_{s\beta}(t) \iff i_s^q = \begin{bmatrix} i_{s\alpha}(t) \\ i_{s\beta}(t) \end{bmatrix}. \]  

(2.10)

By introducing a matrix

\[ J = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \]  

(2.11)

that corresponds to the imaginary unit \( j \), the equation for the \( dq \) transformation is then given by

\[ i_s = e^{-J\theta(t)} i_s^q \]  

(2.12)

and the reverse transformation back to \( \alpha\beta \) coordinates is then

\[ i_s^q = e^{J\theta(t)} i_s. \]  

(2.13)
2.3 Modelling of a non salient PMSM

We also have that

\[ e^{-J\theta(t)} = \begin{bmatrix} \cos \theta_s & \sin \theta_s \\ -\sin \theta_s & \cos \theta_s \end{bmatrix} \]

(2.14)

and

\[ e^{-J\theta(t)} = \begin{bmatrix} \cos \theta_s & -\sin \theta_s \\ \sin \theta_s & \cos \theta_s \end{bmatrix} \]

(2.15)

The matrices \( T_{dq}(\theta_s) \) and \( T_{\alpha\beta}(\theta_s) \) are frequently used in Digital Signal Processors (DSPs) when doing the \( dq \) transformation.

2.3 Modelling of a non salient PMSM

The stator voltage to the non salient PMSM is given by

\[ v_s^s = R_s + \frac{d\psi_s^s}{dt} \]

(2.16)

and the equation for the stator flux is

\[ \psi_s^s = L_s i_s^s + \psi_m^s. \]

(2.17)

\( \psi_m^s \) is the rotor flux linkage vector and is given by

\[ \psi_m^s = \psi_m e^{j\theta_r} \]

(2.18)

where the \( \psi_m \) is the rotor flux linkage from the permanent magnets, \( \theta_r \) is the electrical rotor angle and \( L_s \) is the stator inductance. By assuming that the linkage inductance and the flux linkage from the permanent magnet are
varying slowly [16], the derivative of the stator flux is then

\[
\frac{d\psi_s^s}{dt} = L_s \frac{di_s^s}{dt} + j\omega_r \psi_m e^{j\theta_r}
\] (2.19)

where \( \omega_r \) is the electrical rotor frequency. Putting equation (2.19) into (2.16) gives

\[
L_s \frac{di_s^s}{dt} = v_s^s - (R_s + j\omega_r L_s) i_s^s - j\omega_r \psi_m e^{j\theta_r}
\] (2.20)

Assuming perfect field orientation, the equation (2.20) in the \( dq \) coordinates is then

\[
L_s \frac{di_s}{dt} = v_s - (R_s + j\omega_r L_s) i_s - j\omega_r \psi_m
\] (2.21)

Splitting up equation (2.21) in \( d \) and \( q \) directions gives

\[
u_{sd} = R_s i_{sd} + L_s \frac{di_{sd}}{dt} - \omega_r L_s i_{sq}
\] (2.22)

\[
u_{sq} = R_s i_{sq} + L_s \frac{di_{sq}}{dt} + \omega_r L_s i_{sd} + \omega_r \psi_m
\] (2.23)

In the next section, the salient PMSM model equations are derived from 2.22 and 2.23.

### 2.4 Modelling of a salient PMSM

For a salient PMSM the stator inductance is not equal around the airgap. The coordinates of a salient PMSM are illustrated in Figure 2.3. In \( dq \) coordinates the stator inductance is equal to \( L_d \) on the \( d \) axis and equal to \( L_q \) on the \( q \) axis [16].
2.4 Modelling of a salient PMSM

Figure 2.3: Coordinates of a salient PMSM.

\( u_{sd} \) and \( u_{sq} \) can therefore be modelled as:

\[
\begin{align*}
  u_{sd} &= R_s i_{sd} + L_d \frac{di_{sd}}{dt} - \omega_r L_q i_{sq} \quad (2.24) \\
  u_{sq} &= R_s i_{sq} + L_q \frac{di_{sq}}{dt} + \omega_r L_d i_{sd} + \omega_r \psi_m. \quad (2.25)
\end{align*}
\]

Equation 2.24 and 2.25 describe the electrical subsystem for a salient PMSM model and this subsystem can also be represented by dynamic equivalent circuits showed in Figure 2.4.

Equation 2.24 and 2.25 can also be written in state space form as

\[
\begin{align*}
  \frac{d}{dt} \begin{bmatrix} i_d \\ i_q \end{bmatrix} &= \begin{bmatrix} -\frac{R_s}{L_d} & \frac{\omega_r}{L_d} \\ -\frac{\omega_r}{L_q} & -\frac{R_s}{L_q} \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} + \begin{bmatrix} \frac{1}{L_d} & 0 \\ 0 & \frac{1}{L_q} \end{bmatrix} \begin{bmatrix} u_d \\ u_q - \omega_r \psi_m \end{bmatrix}. \quad (2.26)
\end{align*}
\]
The electrical torque $T_e$ is given by [16] as

$$T_e = \frac{3n_p}{2} [\psi_m i_{sq} + (L_d - L_q)i_{sd}i_{sq}]$$  \hspace{1cm} (2.27)

where $n_p$ is the number of pole pairs of the motor (which is well described in [17]). According to [16] the speed of the rotor can further be expressed as

$$\frac{J_{ml} \, d\omega_r}{n_p} = T_e - T_L.$$  \hspace{1cm} (2.28)

$J_{ml}$ here represents the inertia of the motor plus load, and the motor load $T_L$ is given by

$$T_L = \frac{B_{ml}}{n_p} \omega_r + T_{L,\text{extra}}.$$  \hspace{1cm} (2.29)

$B_{ml}$ is the viscous friction of the motor and load and $T_{L,\text{extra}}$ is the load connected to the motor.

Figure 2.4: Dynamic equivalent circuits for the salient PMSMs electrical subsystem.
Chapter 3

Speed and Current Vector Control

In this chapter, the concept of vector control within motor drives is introduced. The intention is to give an overview of the PMSM control system used in this thesis, as well as present a motivation of online parameter identification within sensorless vector control.

3.1 Vector Control

Vector control is today the most common ac machine control technique and can be applied for both induction machines (IM) and synchronous machines (SM). The method is widely used in high performance industrial application of electric drives. The basic idea is to force the AC machine to behave dynamically as a DC machine by the use of field orientation and feedback control [16]. A PMSM can be seen as a DC motor turned inside out and after field orientation is obtained the control design for a DC motor can be used.
The procedure for transforming the PMSM model into $dq$ coordinates is as follow:

- Measures the three phase currents and projects them into a space vector in the $\alpha\beta$-reference frame.
- Transforms the current vector in the $\alpha\beta$-reference frame in to the $dq$-reference frame.
- Transforms the desired $dq$-frame stator voltage in to the $\alpha\beta$-reference frame.
- Transforms the $\alpha\beta$-frame stator voltage to three phase voltages. The three phase voltages are then used to form the control signal to the pulse with modulation (PWM) of the inverter (power electronic amplifier).

This transformation of the PMSM model into $dq$ coordinates without considering the inverter and PWM, is illustrated in Figure 3.1 (theory of inverters and PWM can be found in [16, 15]). The decoupling of flux and torque is
3.1 Vector Control

Figure 3.2: Vector control system with cascaded current and speed control loops.
done by letting the $d$-axis be aligned with $\psi_m$ (see Figure 2.3). Now, the input and output to the drive system are in the $dq$-frame and the PMSM behaves as a DC motor in steady state. All torque lies in the $q$-axis direction and by varying the stator current component $i_q$, the torque can be changed. The flux is changed by varying the current component $i_d$. The control system to the PMSM can now be designed with inner model control techniques. First a current control loop is added and then cascade coupled with a speed control loop as in Figure 3.2

3.2 Motivation for Online Parameter Identification within Sensorless Vector Control

The basic vector control algorithms require a position sensor to control the motor currents, and since a sensor brings high cost and sometimes low reliability it is desirable to remove the sensor [18]. The concept of sensorless vector control is basically vector control without any speed or position sensor. In this control strategy, the speed and position need to be determined by an observer [1]. In salient PMSM drives the observer is normally built on the electrical motor equations (2.24) and (2.25). This means that if the electrical PMSM parameters do not match the actual values, a speed and position error will occur which affects the control performance of the PMSM. By introducing online parameter identification of electrical PMSM parameters it is possible to design accurate adaptive speed and position observers to sensorless vector control systems. Figure 3.3 illustrates control and system plant for a sensorless vector control PMSM system based on an adaptive speed and position observer with online identification of electrical PMSM parameters.
3.2 Motivation for Online Parameter Identification within Sensorless Vector Control

Figure 3.3: Online identification of electrical PMSM parameters within sensorless vector control.
Chapter 4

Discretization and Linear Regression Models

In this chapter, the non salient model is discretized and transformed into a linear regression model. This makes the model suitable for standard parameter identification algorithms.

4.1 Discretization

Since the control system is implemented in a digital signal processor (DSP), a discretized model of the PMSM is necessary. If a general continuous time invariant system given in the state space form

\[
\begin{align*}
\frac{dx}{dt} &= Ax(t) + Bu(t) \\
y(t) &= Cx(t)
\end{align*}
\]

is zero-order-hold (ZOH) sampled with period \( h \), the system equation will then be
4.1 Discretization

\[ x(kh + h) = A_d(kh) + B_d u(kh) \]  
\[ y(kh) = C_d x(kh) \]  

(4.2)

where

\[ A_d = e^{Ah} \]

\[ B_d = \int_0^h e^{As} ds B \]  

(4.3)

\[ C_d = C. \]

It is necessary to approximate the matrices \( A_d \) and \( B_d \). One way to do that is to introduce a matrix \( \Psi \) [19] defined as

\[ \Psi = \int_0^s h^A s ds \simeq \sum_{i=0}^n \frac{A^i h^{i+1}}{(i+1)!} \]  

(4.4)

and then calculate \( A_d \) and \( B_d \) as

\[ A_d = I + A \Psi \]

\[ B_d = \Psi B. \]  

(4.5)

When \( n \) goes to infinity the approximation error will go to zero. The approximation where \( n = 0 \) is equal to the Euler Forward difference and corresponds to replacing the derivatives with

\[ \frac{dx(t)}{dt} \simeq \frac{x(t + h) - x(t)}{h}. \]  

(4.6)

Now, by writing the electrical space equation (4.7) for the salient PMSM as

\[ \frac{d}{dt} \begin{bmatrix} i_{sd} \\ i_{sq} \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{12} & a_{22} \end{bmatrix} \begin{bmatrix} i_{sd} \\ i_{sq} \end{bmatrix} + \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix} \begin{bmatrix} u_{sd} \\ u_{sq} \end{bmatrix} \]  

(4.7)
where
\[ A = \begin{bmatrix} a_{11} & a_{12} \\ a_{12} & a_{22} \end{bmatrix} = \begin{bmatrix} -\frac{R_{sa} L_d}{L_q} & \frac{\omega_r L_q}{L_d} \\ -\frac{\omega_r L_d}{L_q} & -\frac{R_{sq} L_q}{L_d} \end{bmatrix}, \]
\[ B = \begin{bmatrix} b_{11} & b_{12} \\ b_{12} & b_{22} \end{bmatrix} = \begin{bmatrix} \frac{1}{L_d} & 0 \\ 0 & \frac{1}{L_q} \end{bmatrix}. \]

\( \overline{u}_{sq} = u_{sq} - \omega_r \psi_m \)

the discretization model with Euler Forward difference gives
\[
\begin{bmatrix} i_{sd}(t+1) \\ i_{sq}(t+1) \end{bmatrix} = \begin{bmatrix} a_{11d} & a_{12d} \\ a_{12d} & a_{22d} \end{bmatrix} \begin{bmatrix} i_{d}(t) \\ i_{q}(t) \end{bmatrix} + \begin{bmatrix} b_{11d} & b_{12d} \\ b_{21d} & b_{22d} \end{bmatrix} \begin{bmatrix} u_d(t) \\ \overline{u}_{sq}(t) \end{bmatrix}
\]

\[ (4.9) \]

were
\[
A_d = \begin{bmatrix} a_{11d} & a_{12d} \\ a_{12d} & a_{22d} \end{bmatrix} = \begin{bmatrix} a_{11d} h + 1 & a_{12d} h \\ a_{12d} h & a_{22d} h + 1 \end{bmatrix} = \begin{bmatrix} -\frac{R_{sa} L_d}{L_q} h + 1 & \frac{\omega_r L_q}{L_d} h \\ -\frac{\omega_r L_d}{L_q} h & -\frac{R_{sq} L_q}{L_d} h + 1 \end{bmatrix}
\]
\[
B_d = \begin{bmatrix} b_{11d} & b_{12d} \\ b_{12d} & b_{22d} \end{bmatrix} = \begin{bmatrix} b_{11d} h & b_{12d} h \\ b_{12d} h & b_{22d} h \end{bmatrix} = \begin{bmatrix} \frac{1}{L_d} h & 0 \\ 0 & \frac{1}{L_q} h \end{bmatrix}
\]

\[ (4.10) \]

### 4.2 Linear Regressions

The model structure
\[ y(t) = \varphi(t)^T \theta \]

\[ (4.11) \]

is well known in the statistic as linear regressions, assuming that (4.11) is linear in \( \theta \). The vector \( \varphi(t) \) is named linear regression vector, and the elements in \( \varphi(t) \) are called regressors [20]. The name comes from the fact that we try to calculate/describe \( y(t) \) by going back (regress) to \( \varphi(t) \). The vector \( \theta \) is
4.2 Linear Regressions

called parameter vector and is used to parametrize the model. \( \theta \) consists of model parameters. For the multivariable case \( \theta \) is a matrix. The algorithms for parameter identification that are going to be used later need to have the discretized motor model on linear regression from. Time shifting equation (4.9) one step backwards in time gives:

\[
\begin{bmatrix}
    i_{sd}(t) \\
    i_{sq}(t)
\end{bmatrix}
= \begin{bmatrix}
    a_{11_d} & a_{12_d} \\
    a_{21_d} & a_{22_d}
\end{bmatrix}
\begin{bmatrix}
    i_{sd}(t - 1) \\
    i_{sq}(t - 1)
\end{bmatrix}
+ \begin{bmatrix}
    b_{11_d} & b_{12_d} \\
    b_{21_d} & b_{22_d}
\end{bmatrix}
\begin{bmatrix}
    u_{sd}(t - 1) \\
    u_{sq}(t - 1)
\end{bmatrix}.
\] (4.12)

This model can then be written on linear regression from as:

\[
\begin{bmatrix}
    i_{sd}(t) \\
    i_{sq}(t)
\end{bmatrix}
= \begin{bmatrix}
    i_{sd}(t - 1) \\
    i_{sq}(t - 1)
\end{bmatrix}
+ \begin{bmatrix}
    u_{sd}(t - 1) \\
    u_{sq}(t - 1)
\end{bmatrix}
\begin{bmatrix}
    a_{11_d} & a_{12_d} \\
    a_{21_d} & a_{22_d}
\end{bmatrix}
\begin{bmatrix}
    \varphi^T(t) \\
    \phi^T(t)
\end{bmatrix}.
\] (4.13)

With Euler Forward difference, the motor parameters can be driven from \( \theta \) as:

\[
R_s = \frac{2 - a_{11_d} - a_{22_d}}{b_{11_d} + b_{22_d}},
\]

\[
L_d = \frac{h}{b_{b_{11}}}.
\]

\[
L_q = \frac{h}{b_{b_{22}}}.
\] (4.14)
Chapter 5

Recursive Parameter Estimation

This chapter presents and derives the two algorithms used later in the thesis to estimate the motor parameters, namely recursive least square algorithm with forgetting factor and the normalized projection algorithm. The intention is not only to present the algorithms, but also give the reader some background knowledge of how the algorithms can be derived.

5.1 The Least Square Method

Assume that the model is written on linear regression form and that we want to estimate the parameter matrix $\theta$ from the measured variable vector $y(t)$ and the regression vector $\varphi(t)$ in the sense of least squares. Then we can introduce a loss function

\[
V(\theta, t) = \frac{1}{2} \sum_{i=1}^{t} (y(i) - \hat{y}(i))^2 = V(\theta, t) = \frac{1}{2} \sum_{i=1}^{t} (y(i) - \varphi^T(i)(\theta))^2. \tag{5.1}
\]
5.2 Recursive Least Square Algorithm

By minimizing $V(\theta, t)$ with respect to $\theta$ we get the least square error. This can be done in many ways. One way is to set the derivative to zero due to the fact that $V(\theta, t)$ is quadratic in $\theta$ [20]. This gives

$$0 = \frac{d}{d\theta} V(\theta, t) = \sum_{i=1}^{t} \varphi(t)(y(i) - \varphi^T(i)\theta) \quad (5.2)$$

and then we have

$$\hat{\theta} = \left[ \sum_{i=1}^{t} \varphi(i)\varphi^T(i) \right]^{-1} \sum_{i=1}^{t} \varphi(i)y(i) \quad (5.3)$$

were $\hat{\theta}$ is the estimated parameter matrix. Equation (5.3) can then be solved by numerical algorithm from recorded data containing $\varphi(t)$ and $y(t)$ over a time interval. It is also possible to make the computations recursively in real time.

5.2 Recursive Least Square Algorithm

For identification of parameters in real time, the algorithm is done recursively. Measurement from time $t-1$ is used to predict parameters at time $t$. By introducing a new matrix $P(t)$ [20] defined as

$$P^{-1}(t) = \sum_{i=1}^{t} \varphi(i)\varphi^T(i) = \sum_{i=1}^{t-1} \varphi(i)\varphi^T(i) + \varphi(t)\varphi^T(t), \quad (5.4)$$

equation (5.3) can be expressed as

$$\hat{\theta}(t) = P(t) \sum_{i=1}^{t} \varphi(i)y(i) = P(t) \left( \sum_{i=1}^{t-1} \varphi(i)y(i) + \varphi(t)\varphi^T(t) \right). \quad (5.5)$$
From equations (5.3) and (5.4) we also have that
\[ \sum_{i=1}^{t-1} \varphi(i)y(i) = P^{-1}(t-1)\hat{\theta}(t-1) = P^{-1}(t)\hat{\theta}(t-1) - \varphi(t)\varphi(t)^T\hat{\theta}(t-1). \] (5.6)

And the parameter matrix \( \hat{\theta}(t) \) can then be written as
\[ \hat{\theta}(t) = \hat{\theta}(t-1) + P(t)\varphi(t)(y(t) - \varphi(t)^T\hat{\theta}(t-1)) = \hat{\theta}(t-1) + L(t)\epsilon(t) \] (5.7)
where
\[ L(t) = P(t)\varphi(t) \] (5.8)
\[ \epsilon(t) = y(t) - \varphi(t)^T\hat{\theta}(t-1). \] (5.9)

To calculate \( P(t) \) from \( P(t-1) \) the matrix inversion lemma is used [11]:
\[ (A + BCD)^{-1} = A^{-1} - A^{-1}B(C^{-1} + DA^{-1}B)^{-1}DA^{-1}. \] (5.10)

Equation (5.4) implies that
\[ P(t) = (P^{-1}(t-1) + \varphi(t)\varphi^T(t))^{-1} = (P^{-1}(t-1) + \varphi(t)I\varphi^T(t))^{-1}, \] (5.11)
and applying the matrix inversion lemma gives
\[ P(t) = P(t-1) - P(t-1)\varphi(t)(I + \varphi^T(t)(P(t-1)\varphi(t))^{-1}\varphi^T(t)P(t-1). \] (5.12)
By combining equations (5.8) with (5.12) and applying the matrix inversion lemma again, \( L(t) \) can be calculated as

\[
L(t) = P(t)\varphi(t) = P(t-1)\varphi(t)(I + \varphi(t)^TP(t-1)\varphi(t))^{-1}
\]

which implies that

\[
P(t) = (I - L(t)\varphi^T(t))P(t-1).
\]

The recursive scheme to calculate the parameter matrix is given below:

1. \( \varepsilon(t) = (y(t) - \varphi^T(t)\hat{\theta}(t-1)) \)
2. \( L(t) = P(t-1)\varphi(t)(I + \varphi(t)^TP(t-1)\varphi(t))^{-1} \)
3. \( P(t) = (I - L(t)\varphi^T(t))P(t-1) \)
4. \( \hat{\theta}(t) = \hat{\theta}(t-1) + L(t)\varepsilon(t) \)
5. \( t = t + 1 \)
6. Go to step 1.

5.3 Recursive Least Square with Forgetting Factor

In the scheme (5.15) the parameter matrix \( \theta \) is assumed to be time invariant and for the case where we have time varying parameters, the algorithm needs to be extended. Recursive least square with forgetting factor is an extended version that can handle slow time varying parameters [11]. The idea is to weight data depending on how old it is. The most recent data will have the highest weight and the oldest data will have the lowest weight. This can be
done by replicating the loss function (5.1) with
\[
V(\theta, t) = \frac{1}{2} \sum_{i=1}^{t} \lambda^{t-i}[y(i) - \varphi^T(i)(\theta)]^T[y(i) - \varphi^T(i)(\theta)].
\] (5.16)

This loss function also includes the multivariable case. The variable $\lambda$ is called the forgetting factor and is in the range $[0, 1]$. Now, the most recent data is weighted with $\lambda$ and data that is $n$ units old is weighted with $\lambda^n$.

With the same approach as for the non multivariable case without forgetting factor a recursive scheme can be obtained. A recursive scheme including the multivariable case and forgetting factor is given below:

1. $\varepsilon(t) = [y(t) - \varphi^T(t)\hat{\theta}(t - 1)]$
2. $L(t) = P(t - 1)\varphi(t)[\lambda I + \varphi(t)^TP(t - 1)\varphi(t)]^{-1}$
3. $P(t) = \frac{1}{\lambda}[P(t - 1) - L(t)\varphi^T(t)P(t - 1)]$
4. $\hat{\theta}(t) = \hat{\theta}(t - 1) + L(t)\varepsilon(t)$
5. $t = t + 1$
6. Go to step 1.

(5.17)

### 5.4 Normalized Projection Algorithm

In the RLS algorithm the updating of the $P$ matrix takes most computational effort. Several simplified algorithms that do not need to update the $P$ matrix are proposed in the literature. In this way the computational effort decreases. One of the algorithms is called normalized projection algorithm (NPA) or simply projection algorithm [11]. The estimate $\hat{\theta}(t)$ is here chosen so that $||\hat{\theta}(t) - \hat{\theta}(t - 1)||$ is a minimized subject to the constraint $y(t) = \varphi^T(t)\hat{\theta}(t)$. The constraint can be handled by introducing a Lagrangian multiplier $\bar{\alpha}$. 
The loss function that is going to be minimized is given by

\[
V = \frac{1}{2} [\hat{\theta}(t) - \hat{\theta}(t - 1)]^T [\hat{\theta}(t) - \hat{\theta}(t - 1)] + \bar{\alpha}[y(t) - \varphi(t)^T \hat{\theta}(t)]. \tag{5.18}
\]

Putting derivatives with respect to \( \hat{\theta}(t) \) and \( \bar{\alpha} \) to zero and solving the equations gives the updating formula

\[
\hat{\theta}(t) = \hat{\theta}(t - 1) + \frac{\varphi(t)}{\varphi^T \varphi} [y(t) - \varphi^T(t) \hat{\theta}(t - 1)] \tag{5.19}
\]

Multiplying the nominator with a factor \( \gamma \) and replace the denominator \( \varphi^T \varphi \) to \( \varphi^T \varphi + \alpha \) makes it possible to change the step length of the parameter adjustment and potential problem with \( \varphi = 0 \) is avoided. These changes to the updating formula (5.19) gives the final NPA as

\[
\hat{\theta}(t) = \hat{\theta}(t - 1) + \frac{\gamma \varphi(t)}{\alpha + \varphi(t)^T \varphi(t)} [y(t) - \varphi^T(t) \hat{\theta}(t - 1)] \tag{5.20}
\]

where \( \alpha \geq 0 \) and \( 0 < \gamma < 2 \) to get the algorithm stable. The recursive scheme to calculate the parameter matrix with the NPA is given below:

1. \( \varepsilon(t) = [y(t) - \varphi^T(t) \hat{\theta}(t - 1)] \)
2. \( \hat{\theta}(t) = \hat{\theta}(t - 1) + \frac{\gamma \varphi(t)}{\alpha + \varphi(t)^T \varphi(t)} \varepsilon(t) \) \tag{5.21}
3. \( t = t + 1 \)
4. Go to step 1.
Chapter 6

Simulations

This chapter concerns simulations of the RLS with forgetting factor and the NPA used for estimations of the motor parameters. First, the simulation procedure is described and then the results from the simulations are presented.

6.1 Simulation procedure

A three phase PMSM with salient poles is simulated in MATLAB/SIMULINK to investigate the performance of the RLS with forgetting factor and NPA algorithms applied to the electrical motor parameter identification. In the simulation, the controller to the PMSM drive system with cascaded PI-controllers as in Figure 3.2 is used. A similar drive system is used in the implementation presented in chapter 5. The mechanical parameters of the simulated PMSM are chosen identical to the test motor data sheet parameters. The nominal electrical motor parameters $L_d$, $L_q$ and $R_s$ that are identified in the simulations are measured direct on the motor windings. $\psi_m$ is also measured and assumed to be known in all simulations.

Figure 6.1 shows the inner current loop of the vector control system to-
6.1 Simulation procedure
gether with the identification part. $u_{sq,x}$ and $u_{sd,x}$ represent the identification signals. In order to identify the electrical motor parameters, the identification signals must ensure that $u_{sq}^*$ and $u_{sd}^*$ satisfy the condition of persistent excitation [20]. The identification signals are here binary signals that switches between $\pm 5V$ ($\simeq \pm 30\%$ of the voltage limit to the motor) with a probability of 20 percent in each sample. The measured disturbances are represented in the simulation by $n_d$ and $n_q$. They are created from Gaussian noise signals with variance 1 multiplied with 1.5 percent of the actual current values. In all simulations the sampling time $h = 0.25\text{ms}$. The initiated P matrix and $\lambda$ for the RLS are selected as follows:

$$
\lambda = 0.99;
$$

$$
P = \begin{bmatrix}
0.1 & 0 & 0 & 0 \\
0 & 0.1 & 0 & 0 \\
0 & 0 & 0.1 & 0 \\
0 & 0 & 0 & 0.1
\end{bmatrix}
$$

(6.1)

For the NPA $\gamma$ is chosen to:

$$
\gamma = 0.01
$$

(6.2)
Figure 6.1: Inner current loop of the vector control system together with the identification part.
6.2 Simulation Results

All combinations of start positions of the parameter matrix $\theta$ with

$$R_{s0} = (1 \pm 0.5)R_s$$
$$L_{d0} = (1 \pm 0.5)L_d$$
$$L_{q0} = (1 \pm 0.5)L_q$$

have been tested with the two algorithms used as commission offline parameter identification methods. The motor is in standstill with non load and in each case both algorithms converge. The efficiency is quite clear, but it can be seen that the NPA is less efficient than the RLS as expected. The settling time for the NPA is about 1.2 seconds and for the RLS 0.02 seconds, so the RLS is 6 times faster. Both methods converge to nearly the same parameter values, but the NPA gives a large overshoot or undershoot when estimating $R_s$. Figure 6.2 illustrates simulation results where the start position of $\theta$ is chosen so that $R_{s0} = 0.5R_s$, $L_{d0} = 0.5L_d$ and $L_{q0} = 0.5L_q$.

Figure 6.3 illustrates simulation results when the rotor speed $\omega_r = 600\text{[rpm]}$ instead, the same results are obtained. Table 6.1 shows the magnitude mean errors for the estimated parameters that are valid for both algorithms. Figure

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Mean Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L_d$</td>
<td>$\leq 5%$</td>
</tr>
<tr>
<td>$L_q$</td>
<td>$\leq 4%$</td>
</tr>
<tr>
<td>$R_s$</td>
<td>$\leq 0.7%$</td>
</tr>
</tbody>
</table>

Table 6.1: Magnitude mean error for the parameters when RLS and NPA are used as commission offline parameter identification methods

6.4 illustrates a simulation where the algorithms are used as online parameter estimation methods. $R_s$, $L_d$ and $L_q$ are here defined as variables of
times that change sinusoidally. The PMSM is loaded with a constant torque $T_L = 0.3Nm$. The RLS tracks the parameter variations much better compared to the NPA and especially when it comes to $R_s$. Table 6.2 shows the maximal magnitude of the parameter error for the two algorithms in this simulation. Figure 6.5 shows a simulation were the load torque and parameters are changed with a step during the simulation. After 0.3s $T_L$ increases from 0.3Nm to 0.5Nm by a step, $L_d$ decrease with 5%, $L_q$ decrease with 50% and $R_s$ increase with 40%. The settling time is around 0.08s for both algorithms after the steps are introduced. The two algorithms do not converge to the same parameter values when estimating $L_q$ and $R_s$. NPA also gives a very noisy estimate of $R_s$. Table 6.3 shows the steady state mean value of the parameters after the first step at 0.3s. Figure 6.6 shows a simulation quite similar to Figure 6.5, but now $T_L$ decrease from 0.3Nm to 0.1Nm by a step, $L_d$ increase with 5%, $L_q$ increase with 10% and $R_s$ decrease with 20% instead.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>RLS (Max Error)</th>
<th>NPA (Max Error)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L_d$</td>
<td>$\leq 18%$</td>
<td>$\leq 42%$</td>
</tr>
<tr>
<td>$L_q$</td>
<td>$\leq 16%$</td>
<td>$\leq 32%$</td>
</tr>
<tr>
<td>$R_s$</td>
<td>$\leq 12%$</td>
<td>$\leq 70%$</td>
</tr>
</tbody>
</table>

Table 6.2: Maximal magnitude of the parameter error for the RLS and NPA when the parameter changes sinusoidally

<table>
<thead>
<tr>
<th>Parameter</th>
<th>RLS (Mean Error)</th>
<th>NPA (Mean Error)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L_d$</td>
<td>$\leq 6%$</td>
<td>$\leq 6%$</td>
</tr>
<tr>
<td>$L_q$</td>
<td>$\leq 10%$</td>
<td>$\leq 71%$</td>
</tr>
<tr>
<td>$R_s$</td>
<td>$\leq 0.5%$</td>
<td>$\leq 4.7%$</td>
</tr>
</tbody>
</table>

Table 6.3: Steady state mean value of the parameters after the first step at 0.3s of simulation in Figure 6.5. $T_L$ increases from 0.3Nm to 0.5Nm, $L_d$ decrease with 5%, $L_q$ decrease with 50% and $R_s$ increase with 40%
In this case, both algorithms convergence and the mean parameter errors in steady state are nearly the same. Table 6.4 shows the steady state mean value of the parameters after the first step at 0.3s for this simulation. The reason way the RLS convergence much slower when the parameters change stepwise during the time is because we have same memory stored from old parameter values in the covariance matrix $P(t)$ and the step size $L(t) = P(t) \varphi(t)$ is now much smaller compared to the initialization. RLS with forgetting factor is based of the assumption that the behaviour of the algorithm is homogeneous in time [11] and step changes in the parameters are therefore less suitable. If the forgetting factor $\lambda$ is decreased, the algorithm will be faster due to the fact that $P(t)$ contains less information of previous date. The cost of that is noisier parameter estimation. In a situation with step changing (or very fast changing) parameters, it is more appropriate to reset the $P(t)$ to a large value matrix when the parameter changes occur. The problem here will be to detect the step changing in the parameters. Figure 6.6 illustrate a simulation similar to Figure 6.6, but now the the covariance matrix $P(t)$ is reset when a step change in the parameters occur. The mean parameter error after convergence is more or less the same, but settling time for the RLS is equally fast as for the offline case.

In Figure 6.8 and Figure 6.9 angular errors of the rotor flux position are introduced in the vector control system to investigate the robustness of
the algorithms when the exact rotor flux position is not known. It can be seen that if 5% angular error is introduced the parameter errors from the RLS nearly do not change at all. For the NPA we also have good performance, but the estimation of $R_s$ becomes more noisy and the mean error changes from $-0.4\%$ to $-1.5\%$ (in same simulation the mean error of $R_s$ does not change at all). Generally, for both algorithms, when the angular error increases the absolute value estimation error of $R_s$ increases and becomes more noisy. Table 6.5 shows the mean parameter errors when the angular error is as much as 40%.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>(Mean Error)$_{RLS}$</th>
<th>(Mean Error)$_{NPA}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L_d$</td>
<td>12%</td>
<td>14%</td>
</tr>
<tr>
<td>$L_q$</td>
<td>-5%</td>
<td>0.5%</td>
</tr>
<tr>
<td>$R_s$</td>
<td>-8%</td>
<td>-3%</td>
</tr>
</tbody>
</table>

Table 6.5: Mean parameter errors when an angular rotor flux error of 40% is introduced in the vector control system
6.2 Simulation Results

Figure 6.2: RLS and NPA used as commission offline parameter identification methods in stand still. The start values are: \( L_d^0 = 0.5L_d, L_q^0 = 0.5L_q, R_s^0 = 0.5R_s \)
Figure 6.3: RLS and NPA used as commission offline parameter identification methods in speed 600[rpm] and no load. The start values are: 

- \( L_{d0} = 0.5L_d \), \( L_{q0} = 0.5L_q \), \( R_{s0} = 0.5R_s \)
Figure 6.4: Simulations when the algorithms are used as online parameter estimation methods. $R_s$, $L_d$ and $L_q$ are here defined as variables of times that changes sinusoidal.
Figure 6.5: A simulation where the load torque and parameters are changed with steps. After 0.3s $T_L$ increases from 0.3Nm to 0.5Nm by a step, $L_d$ decrease with 5%, $L_q$ decrease with 50% and $R_s$ increase with 40% in the first step.
6.2 Simulation Results

Figure 6.6: A simulation were the load torque and parameters are changed with steps. After 0.3s $T_L$ decrease from 0.3Nm to 0.1Nm by a step, $L_d$ increase with 5%, $L_q$ increase with 10% and $R_s$ decrease with 20%.
Figure 6.7: A simulation were the load torque and parameters are changed with steps similar to Figure 6.6, but now the covariance matrix $P(t)$ is retested when a step change in the parameters occur.
Figure 6.8: A simulation where an angular rotor flux error is introduced in the vector control system. The angular error increments from 0° to 10°.
Figure 6.9: A simulation were an angular rotor flux error is introduced in the vector control system. The angular error increments from $10^\circ$ to $40^\circ$. 
Chapter 7

Implementation

In order to further verify the performance of the proposed identification methods, recorded data from a testbed PMSM drive system similar to the simulation set-up in Chapter 5 have been used in MATLAB/SIMULINK together with the algorithms. A complexity analysis of the RLS with forgetting factor and the NPA have also been done to investigate if the algorithms are suitable for implementation in existing DSP:s at Aros electronics AB.

7.1 Implementation complexity

To investigate the implementation complexity of the two methods, the number of operations that are needed for each algorithm has been calculated. Table 7.1 shows the number of operations that are needed for implementation of the RLS and the NPA.

Computational time for both methods has been estimated from the number of operations that are required. Table 7.2 shows the estimated computational time for two DSP:s at Aros electronics AB.
7 Implementation

<table>
<thead>
<tr>
<th>Multiplications</th>
<th>Additions</th>
<th>Divisions</th>
</tr>
</thead>
<tbody>
<tr>
<td>NPA</td>
<td>36</td>
<td>14</td>
</tr>
<tr>
<td>RLS</td>
<td>104</td>
<td>72</td>
</tr>
<tr>
<td>Parameter Calculations</td>
<td>0</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 7.1: Number of operations that are needed for implementation of the RLS and the NPA.

<table>
<thead>
<tr>
<th></th>
<th>DSP1</th>
<th>DSP2</th>
</tr>
</thead>
<tbody>
<tr>
<td>NPA + Parameter Calculations</td>
<td>24µs</td>
<td>4µs</td>
</tr>
<tr>
<td>RLS + Parameter Calculations</td>
<td>66µs</td>
<td>11µs</td>
</tr>
</tbody>
</table>

Table 7.2: Estimated computational time for RLS and NPA.

7.2 Implementation Set-up

Figure 7.1 illustrates the implemented vector control system together with the identification signals. The inputs and outputs are recorded and stored in a memory. The recorded data are then used in MATLAB/SIMULINK together with the two algorithms.
Figure 7.1: Vector control system together with the identification signals implemented in a DSP. The inputs and outputs are recorded and stored in a memory.
7 Implementation

7.3 Experimental Results

In the experimental results, the recorded data from the realizations is used in MATLAB/SIMULINK in order to test the algorithms. The parameter variations due to different working points are assumed to be in the range

\[0.8 R_{s,m} < R_s < 1.4 R_{s,m}\]
\[0.95 L_{d,m} < L_d < 1.05 L_{d,m}\]
\[0.5 L_{q,m} < L_q < 1.1 L_{q,m}\]

(7.1)

where \( R_{s,m} \), \( L_{d,m} \) and \( L_{q,m} \) correspond to the measured values.

Figure 7.2 shows the result from a realization where the identification signals \( u_{sq,x} \) and \( u_{sd,x} \) switches between \( \pm 4V \) (\( \simeq \pm 24\% \) of the voltage limit to the motor) with an approximate probability of 20 percent in each sample. The motor is non loaded and the mechanical rotor reference speed \( \omega_{m,ref} \) is set to zero. The algorithms are here used as commission offline parameter identification methods. In this realization the loss function (5.1) converges to zero, so the quadratic error is therefore minimized. A theoretical parameter matrix \( \theta \) has been calculated in MATLAB from equation (4.7) with the expected parameter values. The discretization method was ZOH \( (n \to \infty \) in equation (4.4)) in order to minimize the approximation error. By comparing the estimated parameter matrix \( \hat{\theta} \) with the theoretical \( \theta \), it is shown that all elements that are expected to be zero are close to zero and that the other elements have the right sign. Nothing here indicates bad quality of \( \hat{\theta} \).

In order to test the algorithms as online methods, a realization were the \( \omega_{m,ref} = 600[RPM] \) and \( T_{L,extra} = 0.5[Nm] \) has further been done. The same identification signals \( u_{sq,x} \) and \( u_{sd,x} \) have been used as in the first realization (Figure 7.2). Results can be seen in Figure 7.3. In this realization, the loss
function (5.1) also converges to zero, but by comparing $\hat{\theta}$ with the theoretical $\theta$ (calculated in a similar way as in the first realization), it is shown that one of the elements has the opposite sign and that one of the other elements is close to zero which it should not be. This could indicate that $\hat{\theta}$ is fitted to some disturbance in the measured three phase currents and/or that the applied tree phase voltages to the motor deviate from the reference voltages used as input to the algorithms (the three phase voltages are not measured).

Figure 7.4 illustrates another realization were $T_{L,extra} = 0.1[Nm]$, $\omega_{m,ref} = 600[RPM]$ and $u_{sq,x}$, $u_{sd,x}$ switch between $\pm3V$ ($\pm18\%$ of the voltage limit to the motor) with a approximate probability of 6 percent in each sample. Also here the loss function (5.1) converges to zero. Comparing $\hat{\theta}$ with the theoretical $\theta$ (calculated in a similar way as in the first realization) gives similar results as in the realisation illustrated in Figure 7.3 and the same conclusions can be drawn.
Figure 7.2: Result from a realization were $u_{sq,x}$ and $u_{sd,x}$ switches between $\pm 4V$ with a approximately probability of 20 percent in each sample. $T_{L,extra} = 0$ and $\omega_{m,ref} = 0$
7.3 Experimental Results

Figure 7.3: Result from a realization were $u_{sq,x}$ and $u_{sd,x}$ switches between $\pm 4V$ with an approximately probability of 20 percent in each sample, $T_{L,extra} = 0.5[Nm]$ and $\omega_{m,ref} = 600[RPM]$. 

![Graph of Inductance vs Time](image)

- $L_d(npa) = 0.49897$, $\delta_{npa} = 46.7552\%$
- $L_d(rls) = 0.46524$, $\delta_{rls} = 36.8356\%$

![Graph of Inductance vs Time](image)

- $L_q(npa) = 1.1728$, $\delta_{npa} = 183.9789\%$
- $L_q(rls) = 0.60832$, $\delta_{rls} = 47.2918\%$

![Graph of Resistance vs Time](image)

- $R_s(npa) = 0.25086$, $\delta_{npa} = 109.0477\%$
- $R_s(rls) = 0.21416$, $\delta_{rls} = 78.4657\%$
7 Implementation

Figure 7.4: Result from a realization were \( u_{sq,x} \) and \( u_{sd,x} \) switches between \( \pm 3V \) with a approximately probability of 6 percent in each sample, \( T_{L,extra} = 0.1[Nm] \) and \( \omega_{m,ref} = 600[RPM] \).
Chapter 8

Conclusion and Future Work

In this chapter, the conclusions from the thesis are presented, and some future work is suggested.

8.1 Conclusion

In this thesis, two identification methods for electrical PMSM parameters are studied and compared. The RLS with forgetting factor and the NPA are applied to the salient PMSM model in $dq$-coordinates. The electrical stator parameters $R_s$, $L_d$ and $L_q$ are identified both online and offline. The rotor flux linkage $\psi_m$ is assumed to be known.

The following summarizes the most important conclusions of the simulations in chapter 6.

- It is shown that for the commission offline parameter identification case, both algorithms converge to the same parameter values, but the RLS is about 6 times faster and the NPA gives a large overshoot or undershoot when estimating $R_s$. The magnitude mean error of the
estimated parameter $L_d$ is lower than 5% and for $L_q$ lower than 4%. When it comes to $R_s$ the magnitude mean error is lower than 0.7%.

- Both algorithms are capable of tracking time varying PMSM parameters, but the RLS tracks the parameter variations much better compared to the NPA and especially when it comes to $R_s$.

- The NPA gives noisier parameter estimations in general.

- Both algorithms are robust to angular error in $\psi_m$ lower then 5%.

The following summarizes the most important conclusions from chapter 7, Implementation.

- Computational time for both methods has been estimated from the number of operations that are required and it is shown that the NPA is about 3 times faster compared to the RLS. The fastest DSP today at Aros electronics AB can approximately execute the NPA in 4 $\mu$s and the RLS in 11 $\mu$s. It is important to clear out that this is a rough approximation.

- Experimental verification from real motor data has shown that the algorithms do not convergence to the same parameter values. The NPA estimates the parameter higher than the RLS and especially $L_q$.

- The stator resistance and the stator inductances have been measured directly on the motor windings and compared with the identified parameter values from the algorithms. It is shown that they deviate more than expected. Analysis of the obtained estimates indicates that the parameter values could have been fitted to some disturbance in the measured motor currents and/or that the applied voltages to the motor deviate from the reference voltages used as input to the algorithms.
8.2 Future Work

This thesis has considered parameter identification algorithms for electrical PMSM parameters. As always, much more aspects could be considered. The following gives some proposed future work to the thesis.

- It is a time delay from the reference voltage to the voltage applied to the motor. This time delay is not considered in this thesis. It would be interesting to investigate the impact of the time delay on the parameter identification algorithms.

- More investigations could be done to verify that the recorded motor data and the measured currents are correct.

- When the algorithms work properly on the recorded data the next step would be to implement one or both algorithms in real time.

- By identifying parameter variation in real time it is possible to detect drive faults. A lot of research has been done in this area and it would be interesting to investigate how well the algorithms work for drive fault diagnosis.
Bibliography


