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Performance Comparison of Differential 8-Ary Modulation Formats in High-Speed Optical Transmission Systems

Ekawit Tipsuwannakul, Pontus Johannisson, Mats Sköld, Erik Agrell, Magnus Karlsson, and Peter A. Andrekson, *Fellow, IEEE*

Abstract—This paper presents back-to-back and transmission performance comparisons between single-polarization 120 Gbit/s RZ-DQP-ASK and RZ-D8PSK formats in a single-wavelength system. In the back-to-back configuration, we determine the OSNR requirements of the two formats and compare the results with those obtained analytically and numerically. In the transmission experiments, we examine signal constellations to quantify the significance of intra-channel fiber nonlinearities and investigate the BER performance of the two formats over different reaches (up to 480 km). The results show that the performance of DQP-ASK is superior to D8PSK in back-to-back configuration but is inferior over long distances.

Index Terms—ASK, D8PSK, differential detection, DQP-ASK, DQPSK, fiber nonlinearities, IFWM, modulation format, optical transmission, SPM.

I. INTRODUCTION

D IFFERENTIAL detection is regarded as a scheme for relatively short-range high-speed transmission systems, e.g., metro-networks as it provides low receiver complexity and cost. The scheme is capable of detecting not only differential phase shift keying (DPSK) but also differential-phase and amplitude shift keying (DP-ASK) modulation formats and, at the same time, offers a feasible solution for near-term realization [1]–[9].

As a result, both DPSK and DP-ASK formats carrying (up to) 4 bit/symbol have been demonstrated at high symbol rates over the past several years. For instance, Gnauck *et al.* [1] reported a 1-bit/symbol format, binary DPSK (DBPSK), with the symbol rate of 43 Gbaud (corresponding to 86 Gbit/s in the polarization multiplexed system). Furthermore, B. Koch *et al.* [2], [3] presented 50 Gbaud quadrature DPSK (DQPSK) carrying 2 bit/symbol per polarization with the aggregate bit-rate of 200

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at http://ieeexplore.ieee.org. Digital Object Identifier 10.1109/JLT.2011.2163495 Gbit/s. Moreover, 3-bit/symbol formats, 8-ary DP-ASK (DQP-ASK) and 8-ary DPSK (D8PSK), were shown in [4]–[7], both achieving the same record bit-rate of 240 Gbit/s over a single wavelength with the corresponding symbol rate of 40 Gbaud. A higher-order format such as 16-level DP-ASK (4 bit/symbol) has also been reported but, due to its complexity, the symbol rate was limited to 10 Gbaud [8].

DQP-ASK and D8PSK are, in fact, similar in many ways. For instance, both formats carry 3 bit/symbol, occupy similar spectral width, and have comparable transmitter/receiver complexity. However, since the symbols of the two formats are distributed differently, it is difficult to speculate which format would provide the better performance after transmission limited by fiber nonlinear effects. On one hand, D8PSK is likely to suffer more from fiber nonlinearities since the angular distance between symbols (in the constellation) is half of that of DQP-ASK and thus more susceptible to nonlinear distortion. On the other hand, DQP-ASK is expected to experience severe nonlinear degradation as the format contains two different intensity levels. Evaluating the performance of the two modulation formats over various transmission distances is, thus, essential to determine the most appropriate one for certain applications.

In this paper, we comprehensively compare the back-to-back and transmission performances of single-wavelength, single-polarization 40 Gbaud return-to-zero (RZ)-DQP-ASK and RZ-D8PSK over various distances (up to 480 km experimentally). To our knowledge, this, together with [10], is the first direct comparison of two differential 8-ary formats and also the first study of the influence of fiber nonlinearities on DQP-ASK at 40 Gbaud. In the back-to-back configuration, we analytically, numerically, and experimentally quantify the required optical signal-to-noise ratio (OSNR) of the two formats and, in the case of DOP-ASK, further determine the ratio between the two intensity levels that gives the optimum system performance. For transmission limited by intra-channel nonlinear effects, we investigate the distortion of the two modulation formats using signal constellations obtained numerically and experimentally. We also quantify the optimal launch power (P_{L}) , which is a trade-off between noise and fiber nonlinearities, of the formats over various distances and plot the bit-error-rate (BER) (at the optimal launch power) as a function of the transmission reach. The results reveal that either format can be superior over different distances. It should be noted that the two signals evaluated here have an aggregated bit-rate of 120 Gbit/s,

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Fig. 1. 40 Gbaud RZ-DQP-ASK/D8PSK transmitter implemented in the experimental setup.

which is highly relevant for forthcoming 100 Gigabit Ethernet implementations.

This paper is organized as follows. In Section II, we describe the detailed setup of the transmitter, the receiver, and the transmission link used in the experiments. In Section III, we expound the numerical system implementation, which is generally modeled to replicate that implemented in the experiments. In Section IV, we derive the back-to-back performance of the two formats as a function of OSNR and compare with those obtained from the simulated and the actual systems. Finally, in Section V, we numerically and experimentally evaluate the influence of fiber nonlinearities on the two formats by means of signal constellations and the BER.

II. EXPERIMENTAL SETUP

As illustrated in Fig. 1, the RZ-DQP-ASK/RZ-D8PSK transmitter consisted of a 1 MHz linewidth distributed-feedback (DFB) laser, a 31 GHz I/Q modulator, a 35 GHz phase modulator (PM), and two chirp-free Mach-Zehnder modulators (MZMs). The I/Q modulator was driven by two of 40 Gbit/s binary data streams (D1 and D2), providing 80 Gbit/s DQPSK data at the output. The DQPSK signal was amplified with an Erbium-doped fiber amplifier (EDFA) and the amplified signal was fed into either an MZM or a PM that was driven by the third 40 Gbit/s binary data stream (D3). The former modulator added amplitude modulation while the latter created a $\pi/4$ phase shift onto DQPSK for DQP-ASK and D8PSK generation, respectively. Finally, an MZM was then driven by a sinusoid to generate a RZ format with 50% duty cycle. All data streams (D1, D2, and D3) used in this work were decorrelated pseudo random bit sequences (PRBSs) with the length of $2^{11} - 1$. The length of the PRBS was essentially limited by the programming capability of an error detector (ED). To obtain a fair comparison, the OSNR and the optical power of the two signals at the transmitter output were adjusted to be approximately 52 dB and -15 dBm, respectively. This was done by varying the optical power before and after the EDFA via variable attenuators. The measured constellations of the two modulation formats generated from the transmitter are depicted in Fig. 2 while the measured signal spectra are illustrated in Fig. 3. The larger spreading of symbol points seen in the experimental constellations (compared with those from the simulation) is due to the imperfections of the driving signals such as noise and data jitter (originating from signal generation) that were not accounted for in the simulations. Notice that the



Fig. 2. (left) Simulated and (right) measured signal constellationa of 40 Gbaud (top) RZ-DQP-ASK and (bottom) RZ-D8PSK signals from the transmitter. The measured contellations had the OSNR of the 52 dB and were capture with EXFO modulation analyzer PSO200.



Fig. 3. Simulated (top) and measured (bottom) signal spectra of 40 Gbaud RZ-DQP-ASK (dotted lines) and RZ-D8PSK (solid lines) signal from the transmitter.

experimental signal spectra plotted in Fig. 3 are broader than those obtained numerically. We believe it is because the duty cycle of the RZ format used in the experiment is slightly lower than 50%.

Fig. 4 illustrates the 480 km transmission link used in the experiment. The link was realized by six spans, each containing an 80 km standard single mode fiber (SMF) and double-stage EDFAs with a 12 km dispersion compensating fiber (DCF) in between. The average loss of the SMFs and DCFs in each span were measured to be 18 and 12 dB, respectively. The chromatic



Fig. 4. Transmission link block diagram.



Fig. 5. 40 Gbaund DQP-ASK/D8PSK receiver implemented in the experimental setup. OSA denotes an optical spectrum analyzer.

dispersion at the operating wavelength of the SMFs and the DCFs is found to be approximately 17 and -114 ps/(nm km), yielding small residual dispersion after each span. Short pieces of the SMF were then used after the link to achieve zero net dispersion. The launch power into the DCFs was also kept 5 dB lower than that into SMFs to reduce the impact of fiber nonlinearities in the DCF [11].

At the receiver (as shown in Fig. 5), an optical tunable filter (OTF) with the 3-dB bandwidth of 100 GHz was used to reduce the amplified spontaneous emission (ASE) noise and the filtered signal was split into two branches by a 3-dB coupler for amplitude and phase detection. For the phase detection, the signal was differentially demodulated by a delay line interferometer (DLI) with a free spectral range (FSR) of 43 GHz (non-ideal) and the demodulated signal was detected by a 50 GHz balanced detector (BD). The detected signals were then electronically demultiplexed by a 1:4 demultiplexer and fed into an ED, which was programmed with the expected differentially demodulated bit patterns due to the lack of a differentially pre-coder. Note that the use of the DLI with the non-ideal FSR gives rise to distortion of the differentially demodulated signal. However, such degradation has been shown to be negligible when the FSR differs less than 10% from the ideal value as is in this work [12].

For the amplitude detection, the signal was directly detected by a 50 GHz photodetector (PD) and the detected signal was fed into a 40 Gbit/s ED. The detected signal eye diagrams from the two branches in the back-to-back configuration are illustrated in Fig. 6. Note that the approximate 2 ps skew seen in the eye diagrams of the phase tributaries is caused by a signal path length mismatch of the BD.

III. NUMERICAL MODEL

In the transmitter, the DFB laser was modeled as an ideal light source while the influence of the modulator bandwidth was emulated by low-pass filtering the driving signals with the 5th-order Bessel filter with the bandwidth comparable to those of the modulators used in the experiment. Similarly to the experiment, the driving signals were decorrelated PRBSs with



Fig. 6. Experimentally delected signals from amplitude and phase tributaries of (top) 40 Gbaud RZ-DQP-ASK and (bottom) RZ-D8PSK signals.

 TABLE I

 LISTS OF FIBER PARAMETERS IMPLEMENTED IN THE SIMULATED SYSTEM

	SMF	DCF
γ [W ⁻¹ km ⁻¹]	1.41	2.83
<i>D</i> [ps/(nm km)]	16.5	-110
α [dB/km]	0.225	1.00
Length [km]	80.0	12.0

the length of $2^{11} - 1$. At the output of the transmitter, the OSNR and the power of the optical signal were adjusted to be 52 dB and -15 dBm, respectively. The constellations and the optical spectra of 40 Gbaud RZ-DQP-ASK and RZ-D8PSK signals simulated from this transmitter are depicted in Figs. 2 and 3.

To model light propagation in an optical fiber, we use the nonlinear Schrödinger equation

$$\frac{\partial A}{\partial z} + \frac{\alpha}{2}A + \frac{i\beta_2}{2}\frac{\partial^2 A}{\partial T^2} = i\gamma |A|^2 A \tag{1}$$

where A denotes the complex amplitude of the field envelope, α is the attenuation factor of the fiber, γ corresponds to the Kerr nonlinearity coefficient, and β_2 designates the group-velocity dispersion parameter. As explained in [13], this model neglects the influence of higher-order dispersion, fiber birefringence, intra-pulse Raman scattering, and self-steepening. The equation was solved using the split-step Fourier method.

In this simulation, we modeled the inline EDFAs as noise-free amplifiers and the ASE noise was later added directly before the receiver, which reduces the computational time significantly. By doing so, the nonlinear signal-noise interaction is ignored. However, this nonlinear process has been shown to be minor in the systems operating at high symbol rates and over short distances as is the case in this work [14]. The amount of noise added before the receiver was adjusted to be the same as is in the experiments. The fiber parameters used in the simulation are shown in Table I.

At the receiver, the optical filter was a 4th-order super-Gaussian function with the 3-dB bandwidth of 100 GHz. The FSR of the DLI is set to 43 GHz, similar to that used in the experiment. In addition, The BER of all signal tributaries was obtained from Monte Carlo simulations by direct error



Fig. 7. (top) Analytical, numerical and (bottom) experimental back-to-back performance of 40 Gbaud RZ-DQPSK/D8PSK signals as a function of the OSNR.

counting. It should be noted that the simulated system is assumed to be ASE noise-limited and we ignored the influence of thermal and shot noise. For the OSNR measurement, we take into account the ASE noise power from both orthogonal polarizations.

IV. BACK-TO-BACK PERFORMANCE

In this section, we first derive the theoretical limit of 40 Gbaud RZ-DQP-ASK and RZ-D8PSK, and then compare with the simulated and measured results. The analytical and numerical results of the two formats are plotted in Fig. 7(a) while those from the experiment are shown in Fig. 7(b). The BER performance of RZ-DQPSK at the same symbol rate is also included in the plots as a benchmark.

A. Analytical BER Performance

The SER for M-PSK with differential detection in the presence of additive white Gaussian noise is [15]

SER
$$(\gamma, M) = \frac{\sin(\pi/M)}{2\pi} \int_{-\pi/2}^{\pi/2} \frac{e^{-\gamma[1-\cos(\pi/M)\cos t]}}{1-\cos(\pi/M)\cos t} dt$$
(2)

where

$$\gamma = \langle E_s \rangle / N_0. \tag{3}$$

In these equations, $\langle E_s \rangle$ is the average energy per symbol and N_0 is the noise power spectral density (PSD). By assuming the use of Gray coding, we have

$$BER \approx SER/\log_2 M. \tag{4}$$

Assuming single polarization transmission, we can relate γ to the OSNR using the expression

$$OSNR = \frac{\langle E_s \rangle R_s}{2N_0 \Delta \nu_{0.1} \text{ nm}} = \frac{R_s}{2\Delta \nu_{0.1} \text{ nm}} \gamma$$
(5)

where R_s is the symbol rate and $\Delta \nu_{0.1 \text{ nm}}$ is the reference bandwidth (0.1 nm). With the bit-to-symbol mapping used here, a DQP-ASK symbol can be considered to carry two "phase bits" and one "amplitude bit". In order to find the BER for DQP-ASK, we treat these two cases, i.e., the DQPSK receiver and the direct-detection receiver, separately and then combine the two results to obtain the average BER.

As seen in Fig. 6, the differentially demodulated eye diagram is split up into 2×3 amplitude levels when detecting the phase bits of DQP-ASK. The dominating part of the errors is caused by the innermost levels and, in order to use (2), we need to use the reduced symbol energy that corresponds to this level. Denoting the two amplitude levels of DQP-ASK by a and b (with a < b), we obtain

$$\gamma_{\rm red} = \frac{\langle E_s \rangle}{N_0} \frac{a^2}{(a^2 + b^2)/2} = \frac{2\eta}{1+\eta}\gamma \tag{6}$$

where the intensity ratio is defined $\eta = a^2/b^2$. From this equation, we notice that $\gamma_{\rm red} \rightarrow \gamma$ as $\eta \rightarrow 1$. The detected current is on the innermost levels when two consecutive low-power symbols are transmitted, and on average this occurs in one case out of four. The SER for the phase bits is therefore

$$SER_{phase} = SER(\gamma_{red}, M = 4)/4.$$
(7)

Assuming Gray coding, we obtain

$$BER_{phase} \approx SER_{phase}/2.$$
 (8)

For optimal performance in the direct detection, we assume that a matched optical filter is used. The incoming optical field consists of a signal part and complex white Gaussian noise and since the detected current is proportional to the intensity, the current will have a noncentral chi-square distribution [16]. The optimal decision threshold for the current is the intersection of the probability density functions corresponding to the high and low amplitude levels, respectively, and can be found numerically. The cumulative distribution function is expressed using the Marcum Q function, see [16]. Using (6) and the fact that the noise variance is $N_0/2$ per real dimension, we obtain

$$BER_{amp} = [1 + Q(\sqrt{2\gamma_{red}}, \sqrt{\xi\gamma}) - Q(\sqrt{2\gamma_{red}/\eta}, \sqrt{\xi\gamma})]/2 \quad (9)$$

where the parameter ξ is chosen numerically to minimize BER_{amp} . The minimal BER_{amp} is affected by η , with optimum performance as $\eta \rightarrow 0$. This shows that the choice of the intensity ratio is a trade-off between the phase and amplitude bits. The average BER can be set up using BER_{phase} and BER_{amp} according to

$$BER = \frac{2}{3}BER_{phase} + \frac{1}{3}BER_{amp}.$$
 (10)

In Fig. 7, we have plotted the BER as a function of the OSNR at 40 Gbaud for DQPSK, D8PSK, and DQP-ASK. The intensity ratio that minimizes the OSNR requirement at BER = 10^{-3} has been used. It is found that the minimum OSNR is 17.8 dB and occurs for $\eta = 0.205$ (corresponding to 6.88 dB), For DQPSK and D8PSK, the required OSNR is 14.3 dB and 19.7 dB, respectively.

The optimum intensity ratio depends on the SNR and η will increase with the SNR. The asymptotic value for η at high SNR can be found by approximating the exact expression, but can also be found from single scaling arguments. Thus, in the limit of high SNR, we have [15]

$$BER_{phase} \propto \operatorname{erfc} \sqrt{a^2 [1 - \cos(\pi/4)]/N_0}.$$
 (11)

In the same limit [15]

$$BER_{amp} \propto \operatorname{erfc}[(b-a)/(2\sqrt{N_0})]. \tag{12}$$

By requiring the arguments of the erfc function to be equal, we directly obtain $\eta = 0.231$ (6.37 dB).

B. Discussion of the Results

We first computed/measured the error rates corresponding to binary decision thresholds of all amplitude and/or phase tributaries individually. Each phase tributary was measured separately by applying phase offsets to one arm of the DLI ($\pm \pi/4$ for DQP-ASK, and $\pm \pi/8$, $\pm 3\pi/8$ for D8PSK), yielding 3 (including the amplitude tributary) and 4 different error rates. By assuming that Gray coding is implemented and that symbol errors only occur between neighboring symbols, the BER of the system is then, assuming the average of these error rates in the case of DQP-ASK [3], [4] and the average multiplied by 4/3 in the case of D8PSK [17], [18].

As can be seen from Fig. 7(a), the numerical results of M-ary DPSK signals are consistent with the previous work [19] but approximately 0.6 dB worse than the analytical expectation (including DQP-ASK), which we attribute to non-matched filtering in the simulated receiver. In the case of DQP-ASK, the numerical optimum ratio of the two intensity levels obtained from the simulated system is found to be 6.8 dB, which is also in good agreement with the analytical solution. In addition, the numerical results show approximately 1.8 dB superior performance in the case of DQP-ASK to that of D8PSK for BER = 10^{-3} .

The experimental results shown in Fig. 7(b) also illustrate a similar difference (~ 2 dB) between the performance of DQP-ASK and D8PSK despite the fact that the measured required OSNR is higher than those from the simulated system. However, in the case of experimental DQP-ASK, the optimum ratio of the two intensity levels is found to be 4.7 dB. Although

TABLE II THEORETICAL, NUMERICAL, AND EXPERIMENTAL REQUIRED OSNR (IN DB) FOR BER = 10^{-3} of Three Different Formats at 40 GBaud

	Theoretical	Numerical	Experimental
RZ-DQPSK	14.3	14.9	17.0
RZ-DQP-ASK	17.8	18.5	22.5
RZ-D8PSK	19.7	20.3	24.5



Fig. 8. Simulated noise-free constellations of (a) 40 Gbaud RZ-DBPSK and (b) RZ-DQPSK signals over 320 km with (left) 2 dBm and (right) 8 dBm launch power.

approximately 2 dB deviated from the theory, it is consistent with that experimentally reported in [3], [4]. The difference between the analytical and experimental optimum ratio indicates that the experimental phase tributaries of DQP-ASK perform slightly worse than ideal. The reason is imperfections in the delay interferometer, the BD, and the electrical demultiplexer, causing an extra penalty on the phase tributaries.

Table II summarizes the analytical, numerical, and experimental OSNRs required for BER = 10^{-3} of the three modulation formats. In the case of DQPSK, the OSNR obtained experimentally is roughly 3 dB higher than that found analytically, which is mainly due to the amplitude distortion and data jitter associated with the electrical driving signal generation. This penalty increases to approximately 5 dB in the case of DQP-ASK and D8PSK, which we attribute, at least to a large extent, to the use of an additional driving signal in the transmitter. It should be noted that the predetermined BER = 10^{-3} can achieve the corrected BER = 10^{-15} , provided that the forward error correction overhead with enhanced Reed–Solomon with concatenation is applied [20].

V. TRANSMISSION PERFORMANCE

In this section, we evaluate the influence of fiber nonlinearities on 40 Gbaud RZ-DQP-ASK/D8PSK signals. Since the system is operated at a high symbol rate, we expect the influence of intrachannel nonlinearities, particularly intrachannel four-wave mixing (IFWM) to be dominant [21], [22]. IFWM originates from a nonlinear interaction induced by the overlapping pulses that are dispersively broadened during the



Fig. 9. Simulated noise-free constellations of (a) 40 Gbaud RZ-D8PSK and (b) RZ-DQP-ASK ($\eta = 6.88$ dB) over a 320 km link. The launch power was adjusted between 4 dBm 10 dBm.

propagation. Such an interaction give rises to nonlinear transfer of energy, of which the amplitude and phase are determined by those of the overlapping pulses. This transferred energy then interferes coherently with the existing pulses causing fluctuations in both phase and amplitude [23]. Here, we use the signal constellation and the BER to observe and quantify such degradation.

A. Signal Evolution in Nonlinear Transmission

To understand the significance of fiber nonlinearities on D8PSK and DQP-ASK signals, one should begin by observing the nonlinear evolution of the lower-order formats. Fig. 8 presents the evolution of the simulated noise-free 40 Gbaud RZ-DBPSK and RZ-DQPSK constellations in the transmission limited by fiber nonlinear effects. In this plot, the signals are transmitted over 320 km of the periodically compensated link as described in Section III with the launch power of 2 dBm and



Fig. 10. Measured constellations of 40 Gbaud (a) RZ-D8PSK and (b) RZ-DQP-ASK ($\eta = 4.7$ dB) over a 320 km link. The launch power was adjusted between 4 dBm with the corresponding OSNRs ranging from 27.4 dB to 33.1 dB

8 dBm. The plots illustrate the nonlinear distortion in both amplitude and phase directions due to intrachannel nonlinearities, which alter the symbol points of DBPSK into a "T" shape while spreading those of DQPSK more uniformly. The "T" shape in the case of DBPSK has previously been reported and discussed in [24]. The circular shape formed in the case of DQPSK is due to its additional phase states (compared with DBPSK), which in turn provide more degrees-of-freedom of the resultant phase and amplitude of the IFWM.

The uniform spreading of symbol points is also seen in the simulated noise-free 40 Gbaud RZ-D8PSK constellations plotted in Fig. 9(a). In this case, the spreading is rounder since the signal exploits twice the phase states compared to DQPSK.

A different spreading is however observed in Fig. 9(b), which depicts the simulated noise-free 40 Gbaud RZ-DQP-ASK constellations over 320 km with four different launch powers. In

a)



Fig. 11. Experimental BER as a function of the launch power of 40 Gbaud (top) RZ-D8PSK and (bottom) RZ-DQP-ASK over (up to) 6 spans.

these plots, the signal degradation caused by IFWM as well as significant phase distortion (compared to DQPSK) is clearly seen. We attribute such distortion to the additional amplitude modulation, that is, the symbols surrounded by many low-intensity neighbors will experience small spreading due to low nonlinear transfer of energy while those with many of high-intensity neighboring symbols will be severely distorted due to high nonlinear energy transfer.

The numerical observations are well supported by the measured 40 Gbaud RZ-D8PSK and RZ-DQP-ASK constellations over the same distance (320 km) from the actual system in Fig. 10. The results show high consistency to those obtained from the simulation, validating the accuracy of the simulated system. Compared with those from the simulation, the measured constellations of the two formats however exhibit larger phase and amplitude spreading, which is due to the accumulated ASE noise generated from the in-line EDFAs. It should be noted that, similarly to those in Fig. 2, the plots in Fig. 10 were coherently sampled constellations without applying equalization.

B. Experimental BER Results

The signal degradation due to fiber nonlinearities can also be observed from the BER. In Fig. 11, we plot the experimental BER of the 40 Gbaud RZ-D8PSK and RZ-DQP-ASK over (up to) 6 spans as a function of the launch power. Note that for the DQP-ASK transmission, the intensity ratio was kept equal to



Fig. 12. Experimental BER performance (at optimal launch power) as a function of the transmission distance.

the optimized values obtained in the back-to-back configuration (6.8 dB numerically and 4.7 dB experimentally).

As expected, each curve identifies an optimal launch power, which is a trade-off between noise and fiber nonlinearities. At low BER (< 10-5), a strong dependency of the optimal launch power on the number of spans is clearly seen. However, such a dependency is obscured at high BER by other sources of error such as noisy driving signals and receiver imperfections. In the case of D8PSK, we notice an approximate 2 dB higher optimal launch power than that of DQP-ASK. We also observe that the BER performance decreases more rapidly with the number of spans in the case of DQP-ASK. These findings indicate that, similarly to the constellation observation, D8PSK is more resilient against fiber nonlinearities.

To summarize the results in Fig. 11, we plot the minimum BER (at the optimal launch power) as a function of the transmission distance in Fig. 12. The plot shows that DQP-ASK outperforms D8PSK at short distances due to its superior back-to-back sensitivity. However, as the reach increases, its performance gradually approaches that of D8PSK due to nonlinear effects and eventually becomes worse at 480 km.

C. Numerical BER Results

Fig. 13 presents the numerical BER performance of the two signals as a function of the launch power over (up to) 20 spans. Compared to the experiment, however, the signals were evaluated over longer distances. This is because, as described in Section IV, the noise and data jitter originating from driving signal generation are not included in the simulated system. The curves, thus, illustrate a fundamental limit of the two signals in nonlinear transmission.

Nevertheless, regardless the difference in the distance, we observe similarities between the numerical curves and those (at high BER) obtained experimentally. Firstly, the optimal launch power in the case of DQP-ASK is approximately 2 dB lower than that of D8PSK. Secondly, the performance at the optimal launch decreases more rapidly with the number of span in the case of DQP-ASK.

Finally, a similar conclusion as from the experiment can be drawn from Fig. 14, that is, DQP-ASK gives a superior performance at shorter distances but becomes worse after a cer-



Fig. 13. Numerical BER as a function of the launch power of 40 Gbaud (top) RZ-D8PSK and (bottom) RZ-DQP-ASK over (up to) 20 spans.



Fig. 14. Numerical BER performance (at optimal launch power) as a function of the transmission distance.

tain distance (in this case, 1 500 km). It should be noted that although the numerical distance at which D8PSK outperforms DQP-ASK differs from that obtained experimentally by factor of 3.8, it is, indeed, consistent with the difference between the numerical and the experimental back-to-back OSNR requirements. This implies that if all imperfections of the driving signal are included in the numerical model, the same curves should be obtained from the simulation and the experiment.

VI. CONCLUSION

In this work, the first comprehensive performance comparison between 40 Gbaud RZ-D8PSK and RZ-DQP-ASK in back-to-back and nonlinear transmission is presented. We find that, in the experimental back-to-back transmission, DQP-ASK required approximately 2 dB lower OSNR than D8PSK for BER = 10^{-3} , which leads to superior performance over short transmission distances (up to 400 km experimentally). However, since D8PSK is more resilient to fiber nonlinearities, its BER performance eventually exceeds that of DQP-ASK over long distances (more than 400 km experimentally). Lastly, our experimental findings are consistent with the analytical and numerical solutions.

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